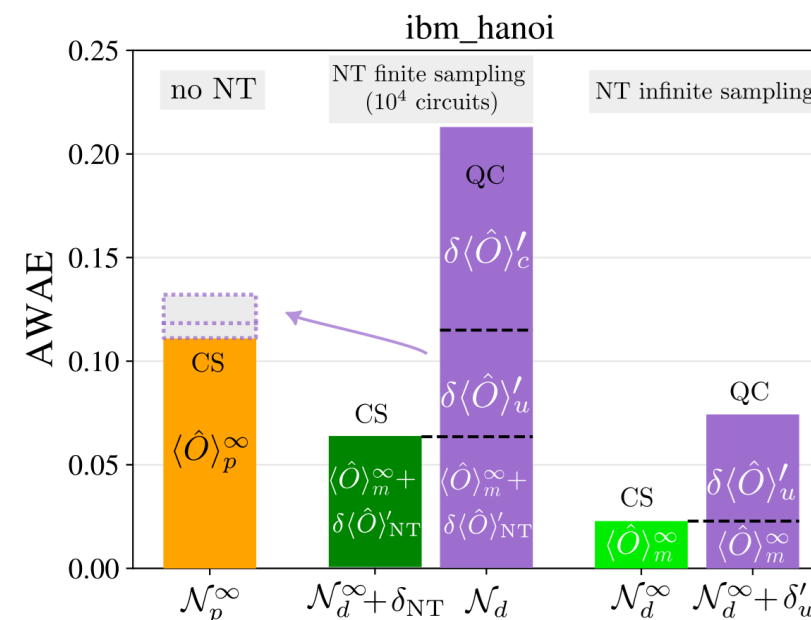




Kyrylo Snizhko
CEA Grenoble

Noise tailoring for error mitigation and for diagnosing quantum computers

TQCI seminar on Quantum Benchmarks
24.06.2025, Paris



Noise in quantum computers is detrimental

Mitigating crosstalk errors by randomized compiling: Simulation of the BCS model on a superconducting quantum computer

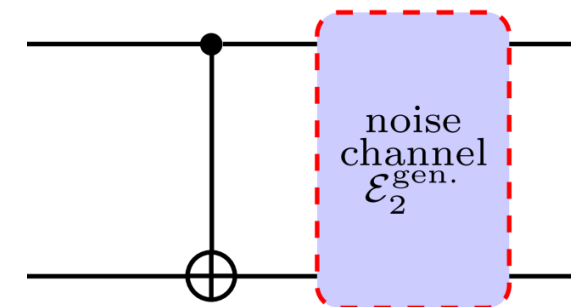
Hugo Perrin^{1,*}, Thibault Scoquant^{1,*}, Alexander Shnirman^{1,2}, Jörg Schmalian^{1,2} and Kyrylo Snizhko³

¹Karlsruhe Institute of Technology, Institut für Theorie der Kondensierten Materie, TKM, 76049 Karlsruhe, Germany

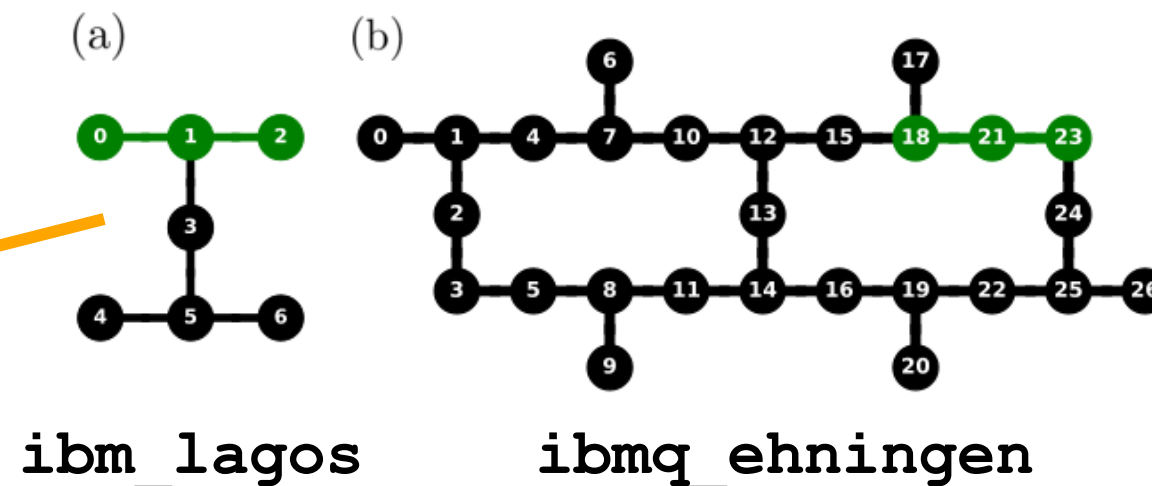
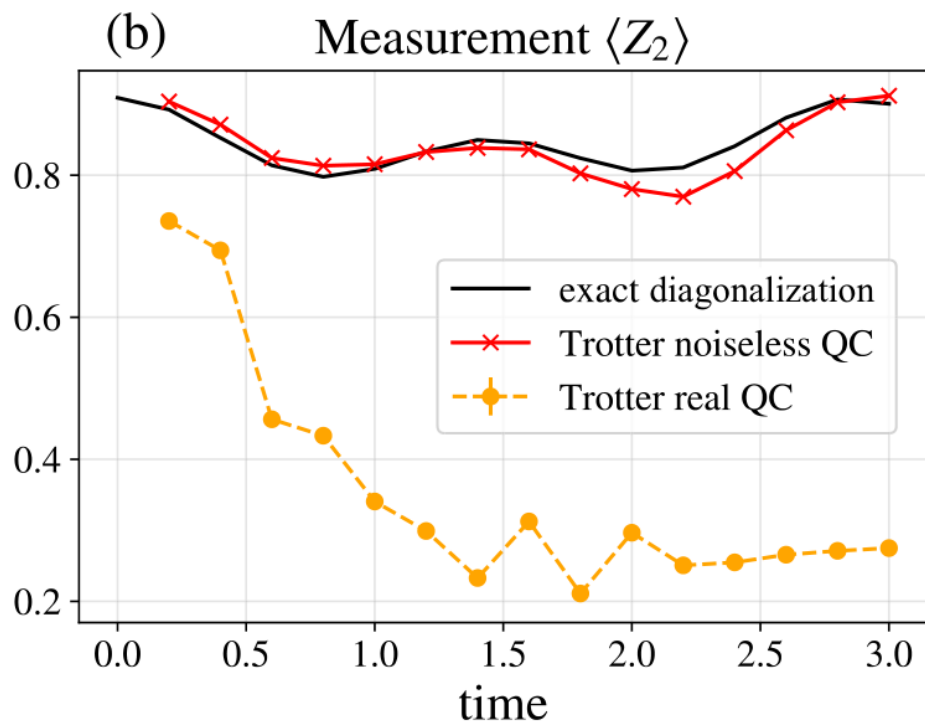
²Karlsruher Institut für Technologie, Institut für Quantenmaterialien und Technologien, IQMT, 76021 Karlsruhe, Germany

³Univ. Grenoble Alpes, CEA, Grenoble INP, IRIG, PHELIQS, 38000 Grenoble, France

PRResearch 6, 013142 (2024)



$$\hat{H}_{\text{BCS}} = - \sum_{j=0}^{L-1} \left(\epsilon_j - \frac{g}{2} \right) \sigma_j^z - \frac{g}{2} \sum_{\substack{i,j=0 \\ i < j}}^{L-1} \left(\sigma_i^x \sigma_j^x + \sigma_i^y \sigma_j^y \right)$$

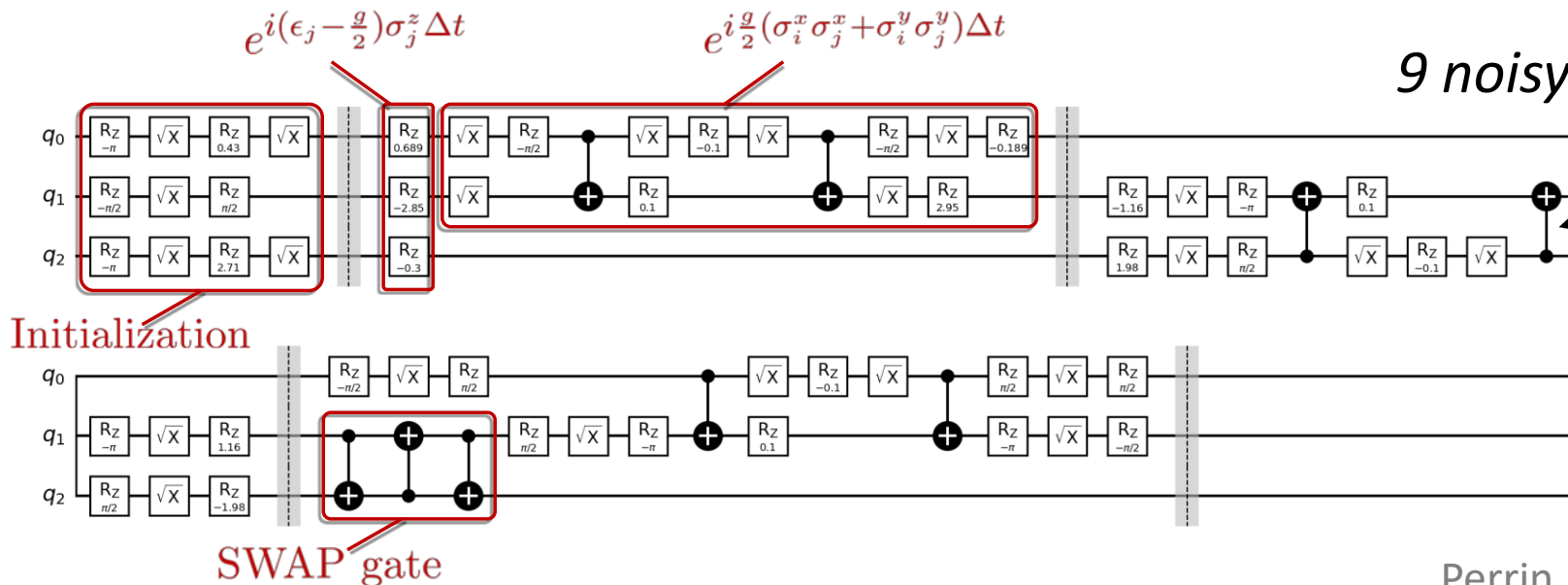


Simulating quench dynamics in the BCS model

$$\hat{H}_{\text{BCS}} = - \sum_{j=0}^{L-1} \left(\epsilon_j - \frac{g}{2} \right) \sigma_j^z - \frac{g}{2} \sum_{\substack{i,j=0 \\ i < j}}^{L-1} (\sigma_i^x \sigma_j^x + \sigma_i^y \sigma_j^y)$$

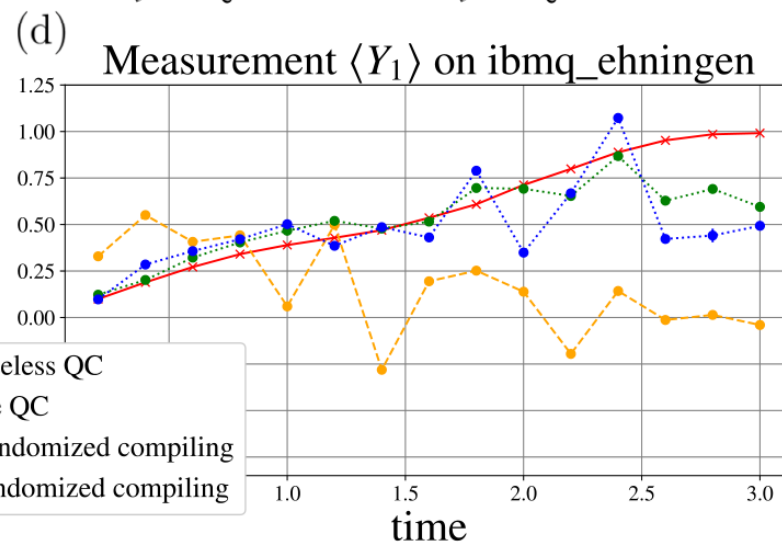
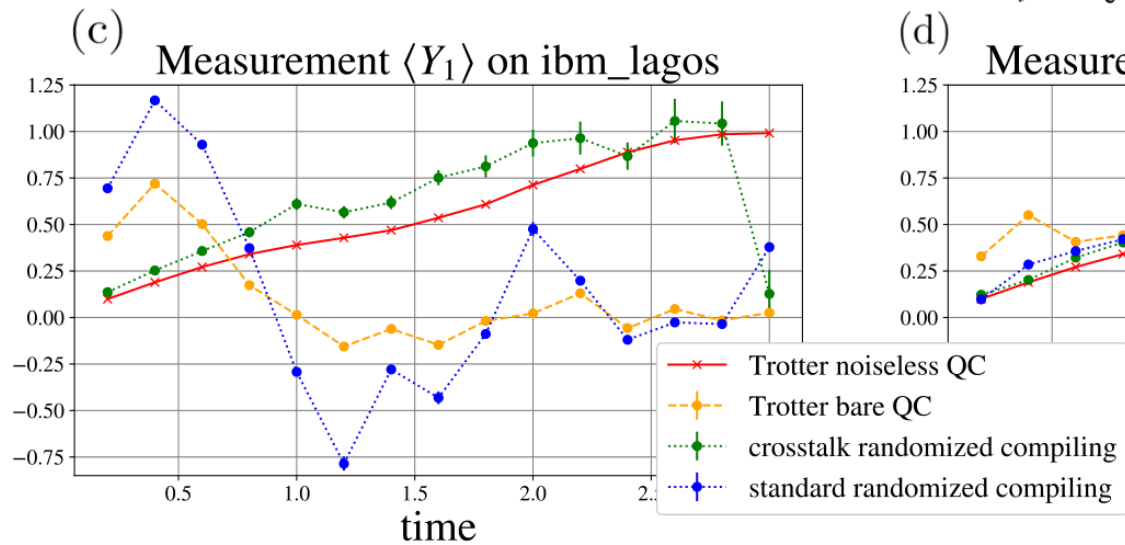
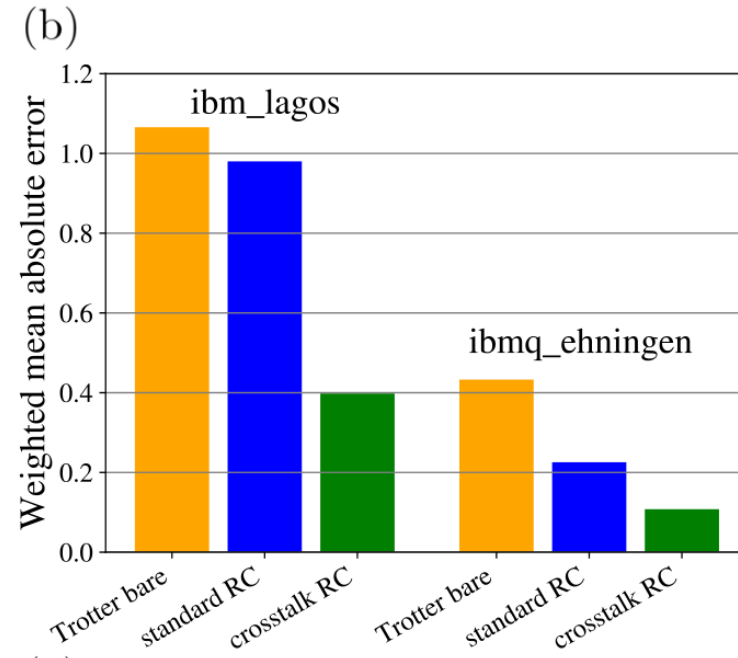
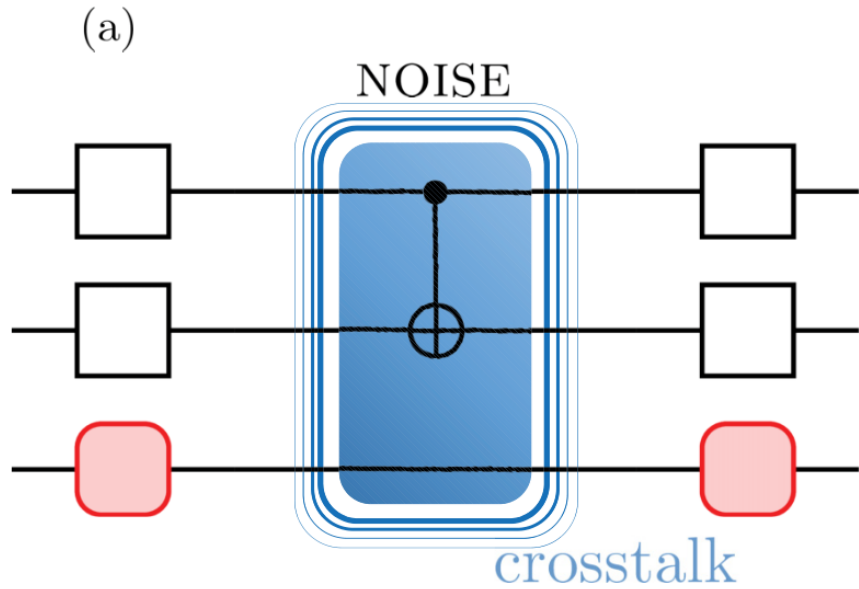
$L = 3$ qubits/Cooper pairs

$$\hat{U}_{\text{BCS}}(\Delta t) \simeq \prod_j e^{i(\epsilon_j - \frac{g}{2})\sigma_j^z \Delta t} \prod_{i < j} e^{i\frac{g}{2}(\sigma_i^x \sigma_j^x + \sigma_i^y \sigma_j^y) \Delta t}$$



99% accurate CNOTs
 $\Rightarrow$ 1% error per CNOT
 $\Rightarrow$ 9% error per Trotter step
 $\Rightarrow$ **expect complete noise after ~11 steps**

Mitigating the noise and seeing the crosstalk



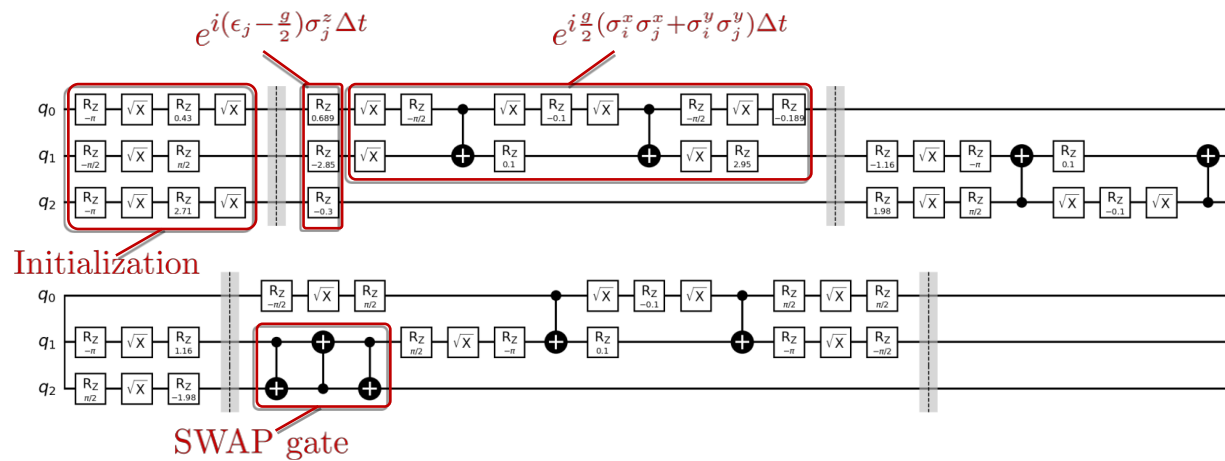
⇐ expect complete noise
after ~11 steps

Mitigation: noise estimation circuit (NEC)

Example: Assume N -qubit, **global** depolarizing noise:

$$\mathcal{E}_n^{\text{glob.}}(\rho) = (1 - \lambda_{\text{glob.}})\rho + \lambda_{\text{glob.}} \frac{\mathbb{I}}{2^N} \longrightarrow \langle \mathcal{O} \rangle_{\text{noisy}} = (1 - \lambda_{\text{glob.}})^{n_{\text{CNOT}}} \langle \mathcal{O} \rangle_{\text{noiseless}}$$

Multiplicative error removed by running circuits with only the CNOT skeleton:

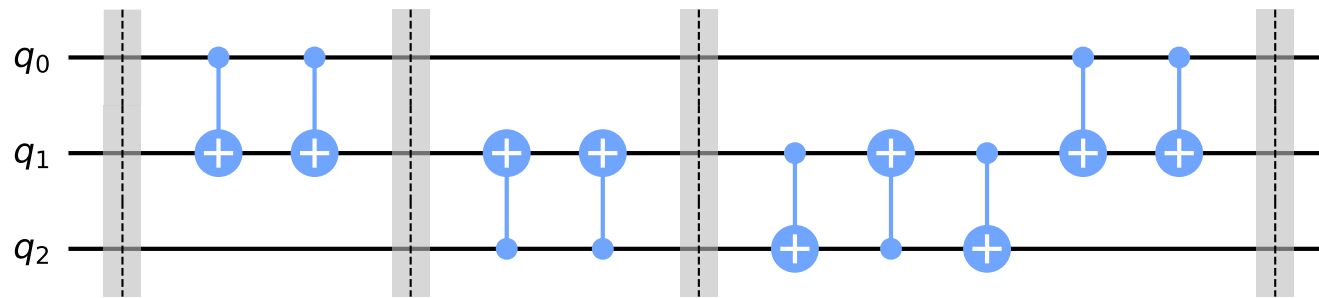


Mitigation: noise estimation circuit (NEC)

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Multiplicative error removed by running **circuits with only the CNOT skeleton:**



Noise estimation circuit

=

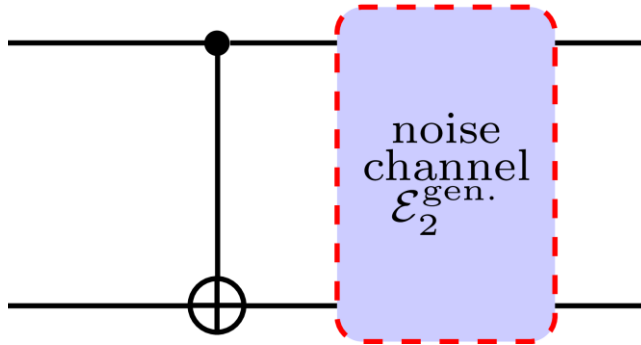
Trotter step circuit without single qubit gates

$$\langle \hat{O} \rangle_{\text{mitigated}} = \frac{\langle \hat{O} \rangle_{\text{measured}}}{\mathcal{F}_{\text{NEC}}} \sim \frac{\langle \hat{O} \rangle_{\text{measured}}}{\langle 1 \rangle_{\text{measured}}}$$

Simplifying the noise structure:

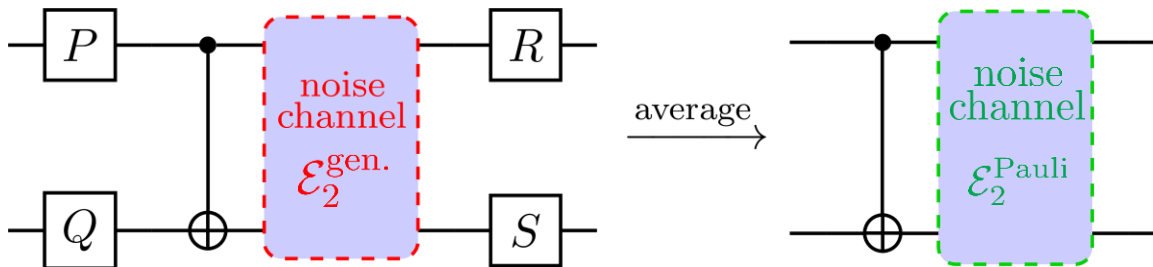
randomized compiling (RC)

- General noise:



$$\mathcal{E}_2^{\text{gen.}}(\rho) = \sum_{i,j,k,l=0}^3 p_{ijkl}(\sigma^i \otimes \sigma^j) \cdot \rho \cdot (\sigma^k \otimes \sigma^l)$$

- Randomized compiling to get Pauli noise



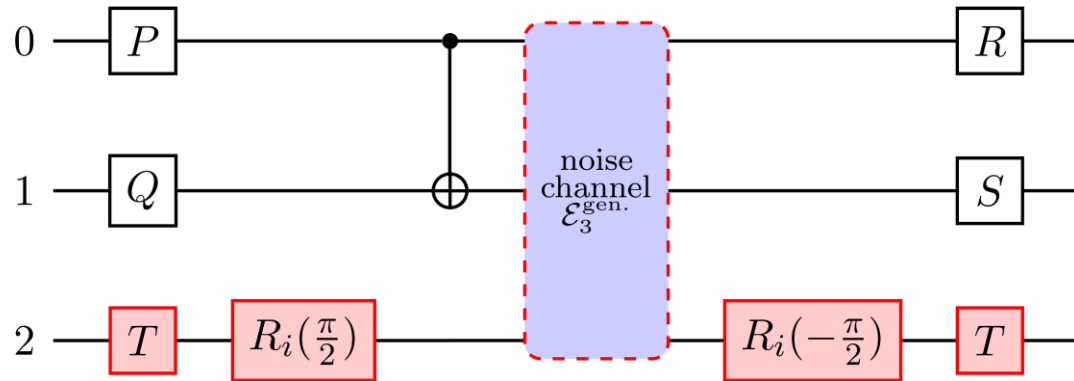
$$\mathcal{E}_2^{\text{Pauli}}(\rho) = \sum_{i,j=0}^3 p_{ij}(\sigma^i \otimes \sigma^j) \cdot \rho \cdot (\sigma^i \otimes \sigma^j)$$

Kern et al., Eur. Phys. J. D **32**, 153 (2005)

Wallman, Emerson, PRA **94**, 052325 (2016)

Hashim et al., PRX **11**, 041039 (2021)

Crosstalk!

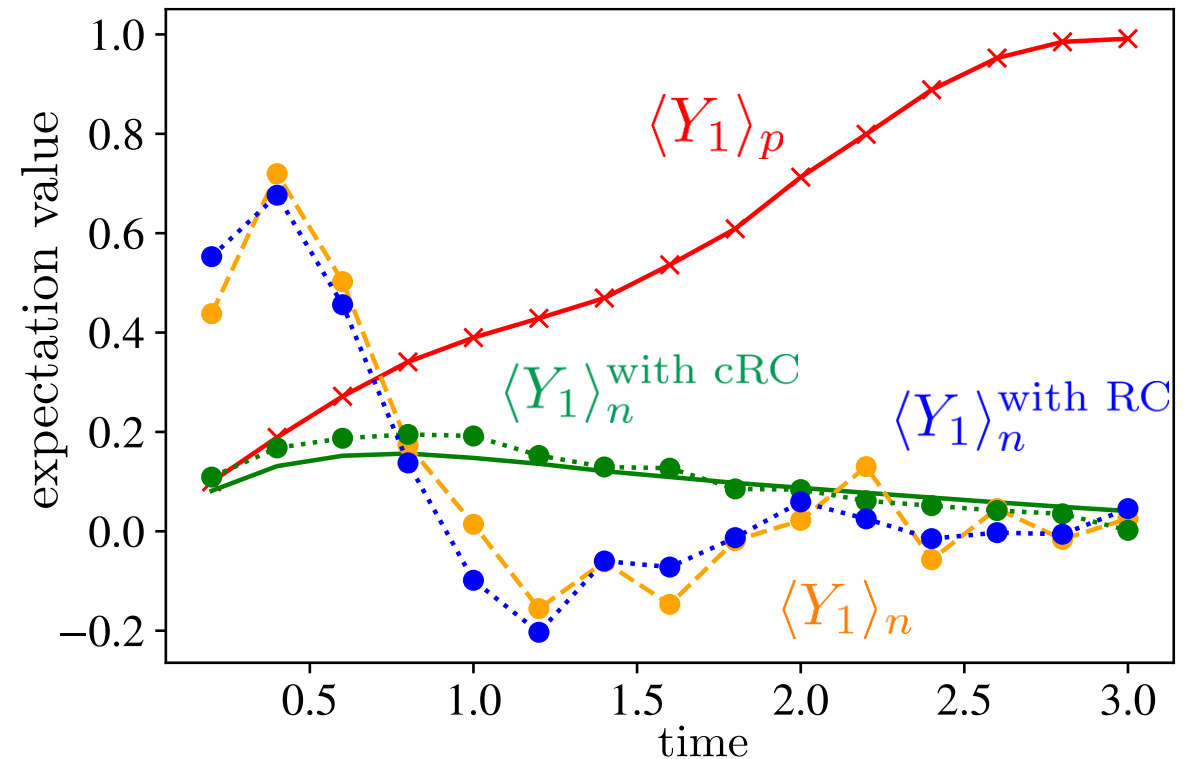


Crosstalk RC (cRC) average

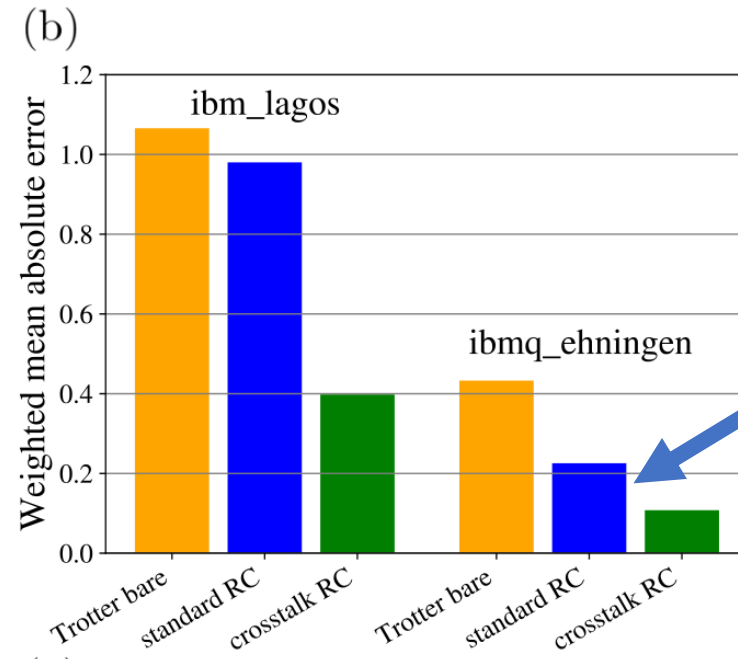
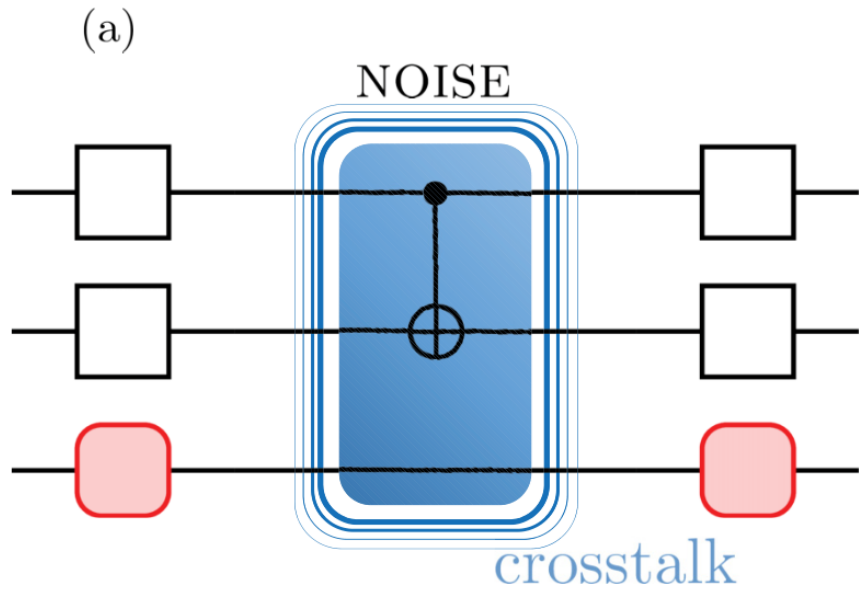
$$\mathcal{E}_1^{\text{dep.}}(\rho) = (1 - \lambda') \rho + \lambda' \frac{\mathbb{I}_2}{2}$$

Yields **depolarizing noise** on the **neighbouring qubit** !

RC (no NEC):

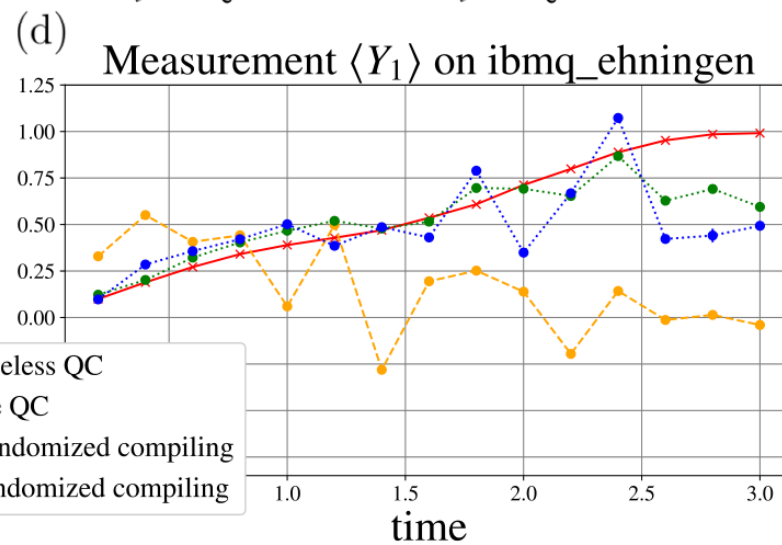
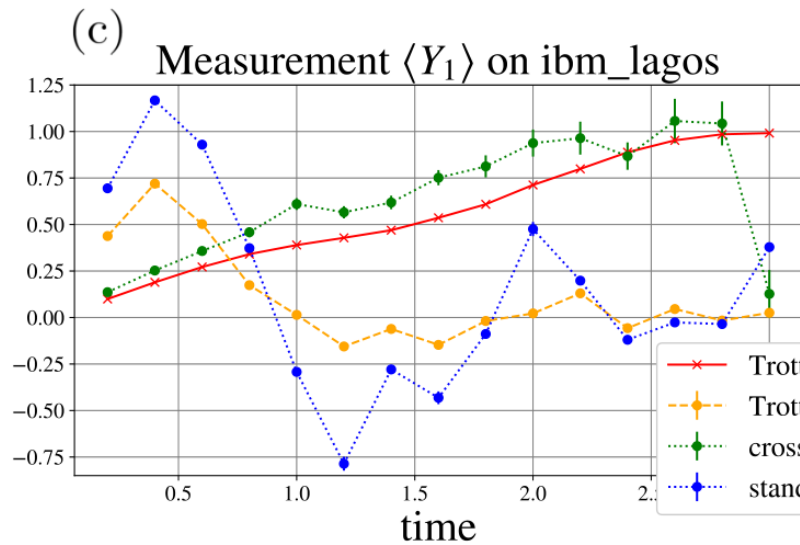


RC + NEC = improved results + error characterization



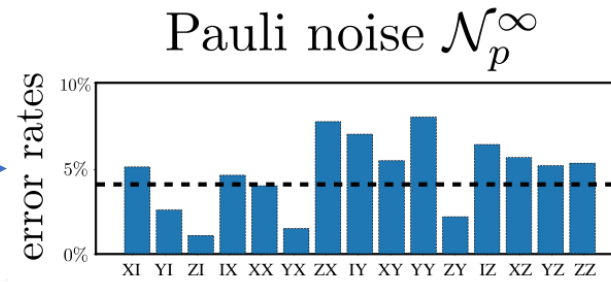
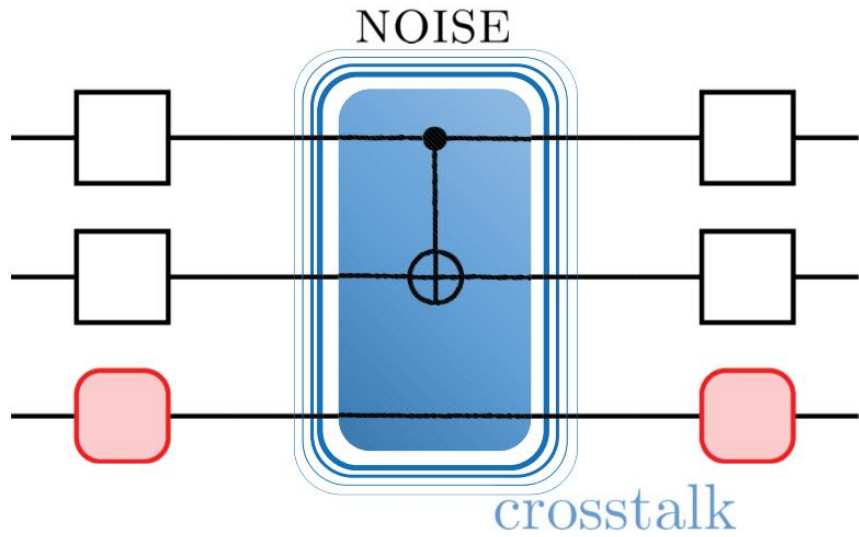
Stack of techniques

*Direct estimation
of spillover crosstalk
by RC vs cRC*

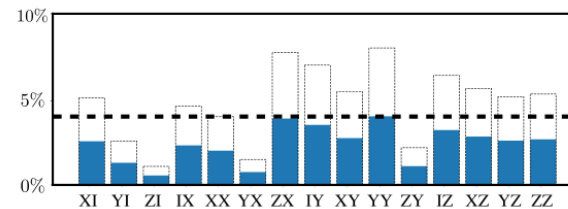


⇐ NEC used for all curves

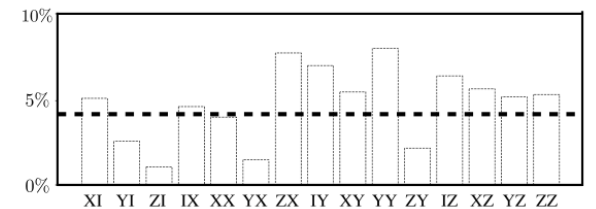
Probabilistic error cancellation (PEC) reduction (PER)



PER

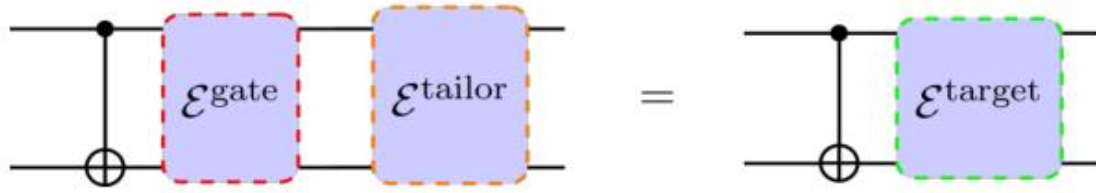


PEC

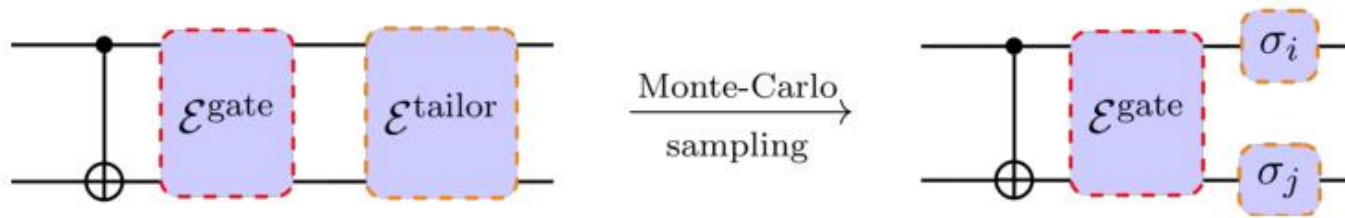


How do PEC and PER work?

(a)



(b)

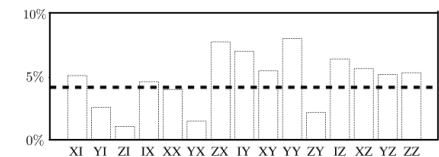
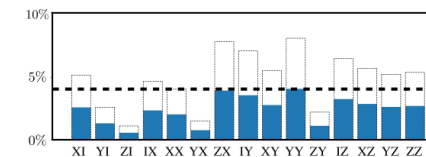


Sample $(\sigma_i, \sigma_j) = P_a$

Get target noise channel

PER

PEC

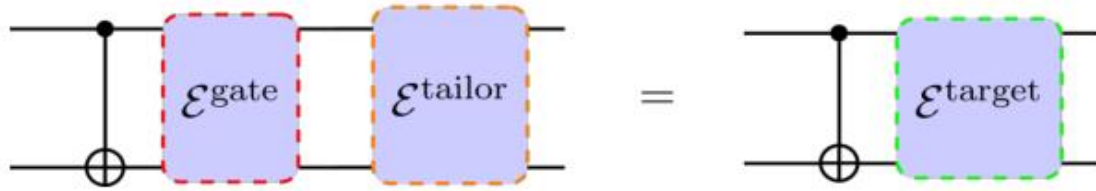


Temme, Bravyi, Gambetta, PRL **119**, 180509 (2017)

Berg, Mineev, Kandala, Temme, Nature Physics **19**, 1116 (2023)

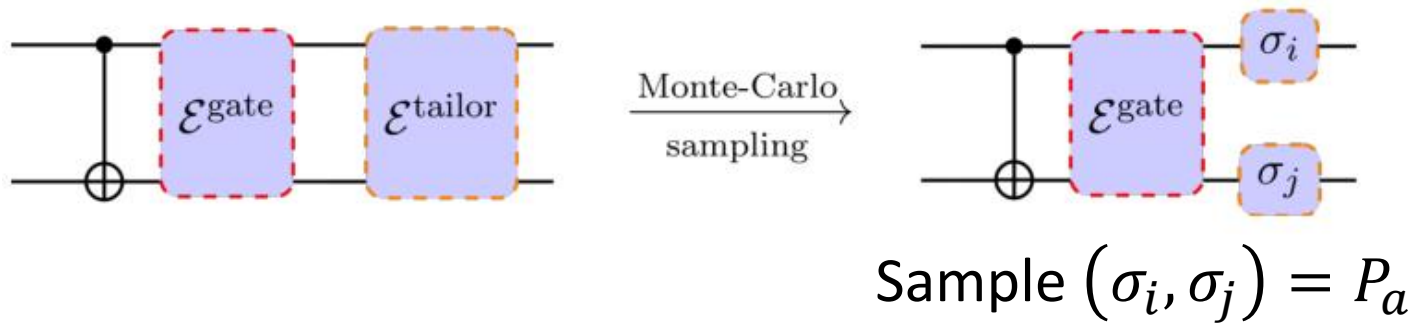
How do PEC and PER work?

(a)



Problem: need to sample quasiprobability distribution q_a^{tailor}

(b)



Sample:

$$\tilde{p}_a^{\text{tailor}} = \frac{|q_a^{\text{tailor}}|}{\gamma},$$
$$\gamma = \sum_a |q_a^{\text{tailor}}| > 1$$

Take the sign q_a^{tailor} into account when calculating the Monte-Carlo average

Multiply the average by $\gamma^{n_{\text{CNOT}}}$

$\Rightarrow$ exponentially costly to keep a fixed error bar (sign problem)

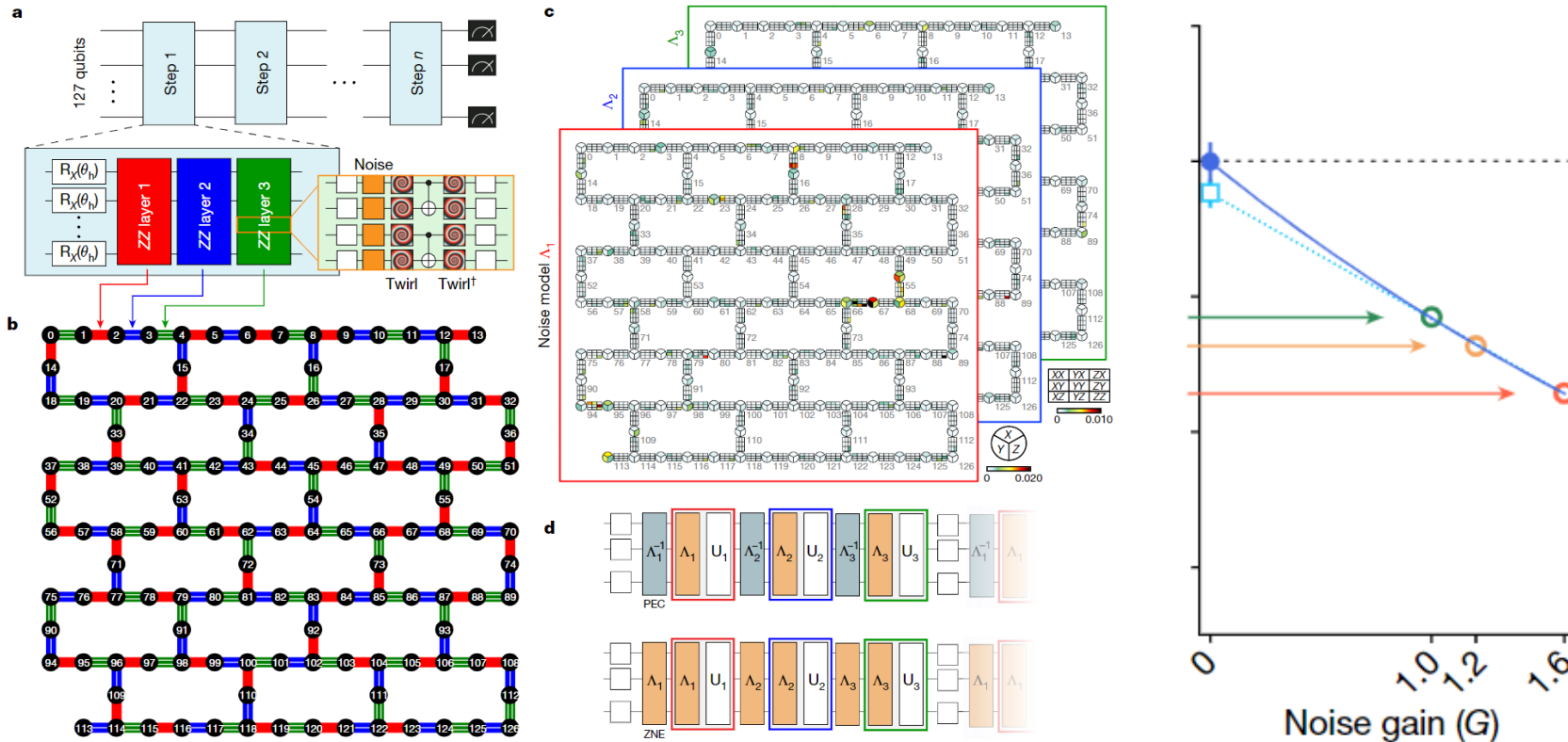
How do PEC and PER work?

Multiply the average by $\gamma^{n_{\text{CNOT}}}$

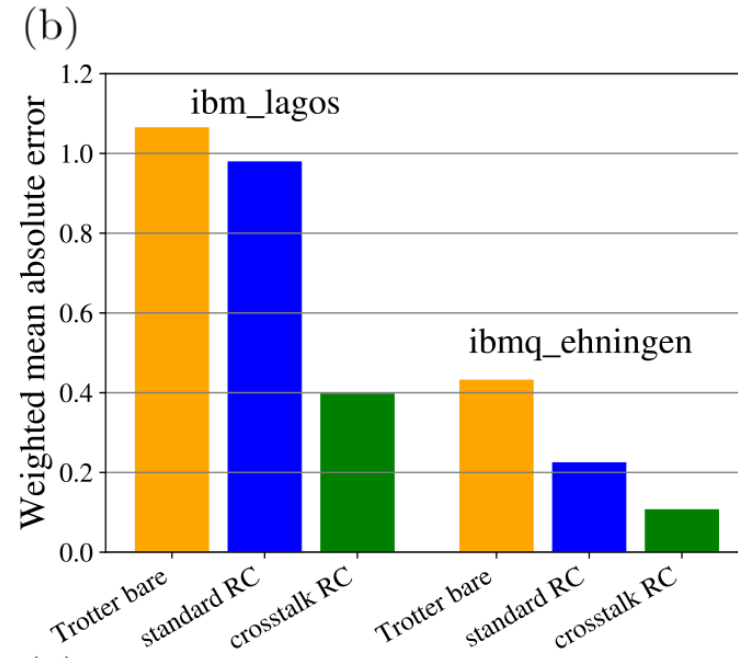
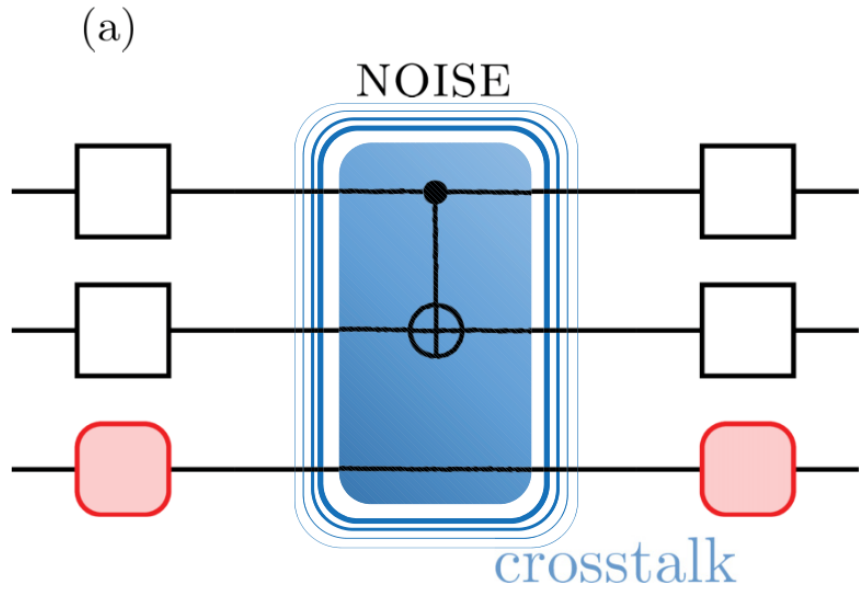
⇒ exponentially costly when reducing noise

Possible solution: increase noise (avoid quasiprobability distributions!)

E.g., IBM “quantum utility” experiment:

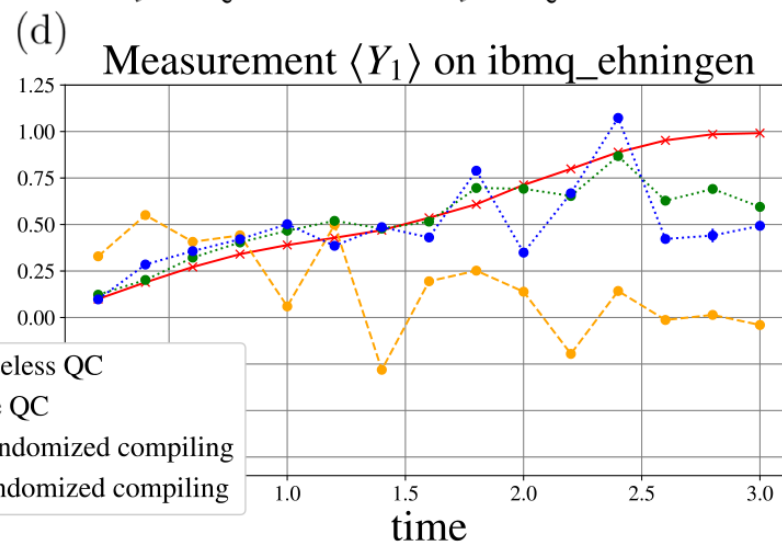
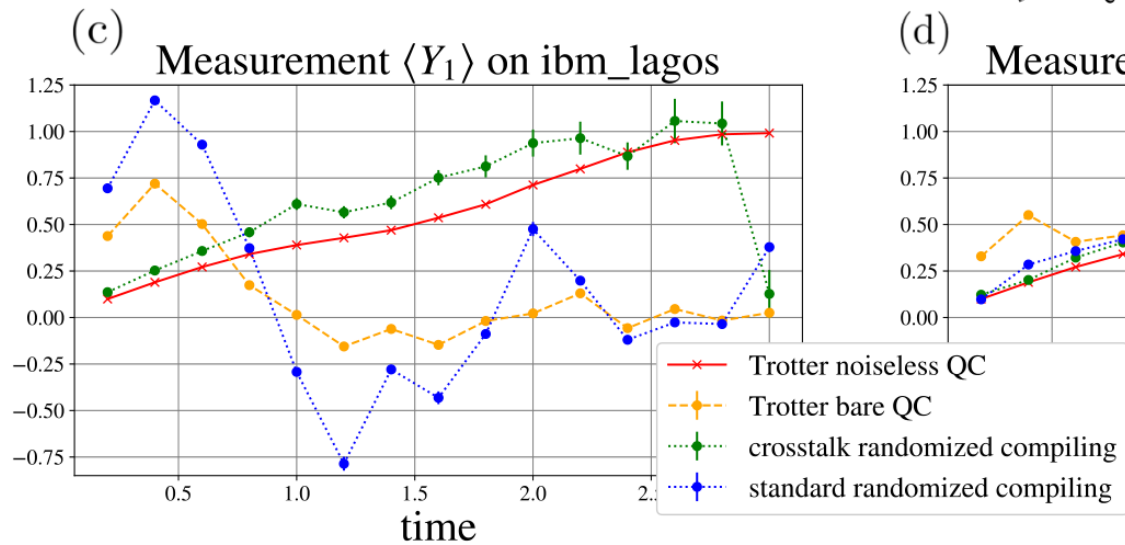


RC + NEC = improved results + error characterization



NEC requires global depolarizing noise

$$\mathcal{E}_n^{\text{glob.}}(\rho) = (1 - \lambda_{\text{glob.}})\rho + \lambda_{\text{glob.}} \frac{\mathbb{I}}{2^N}$$

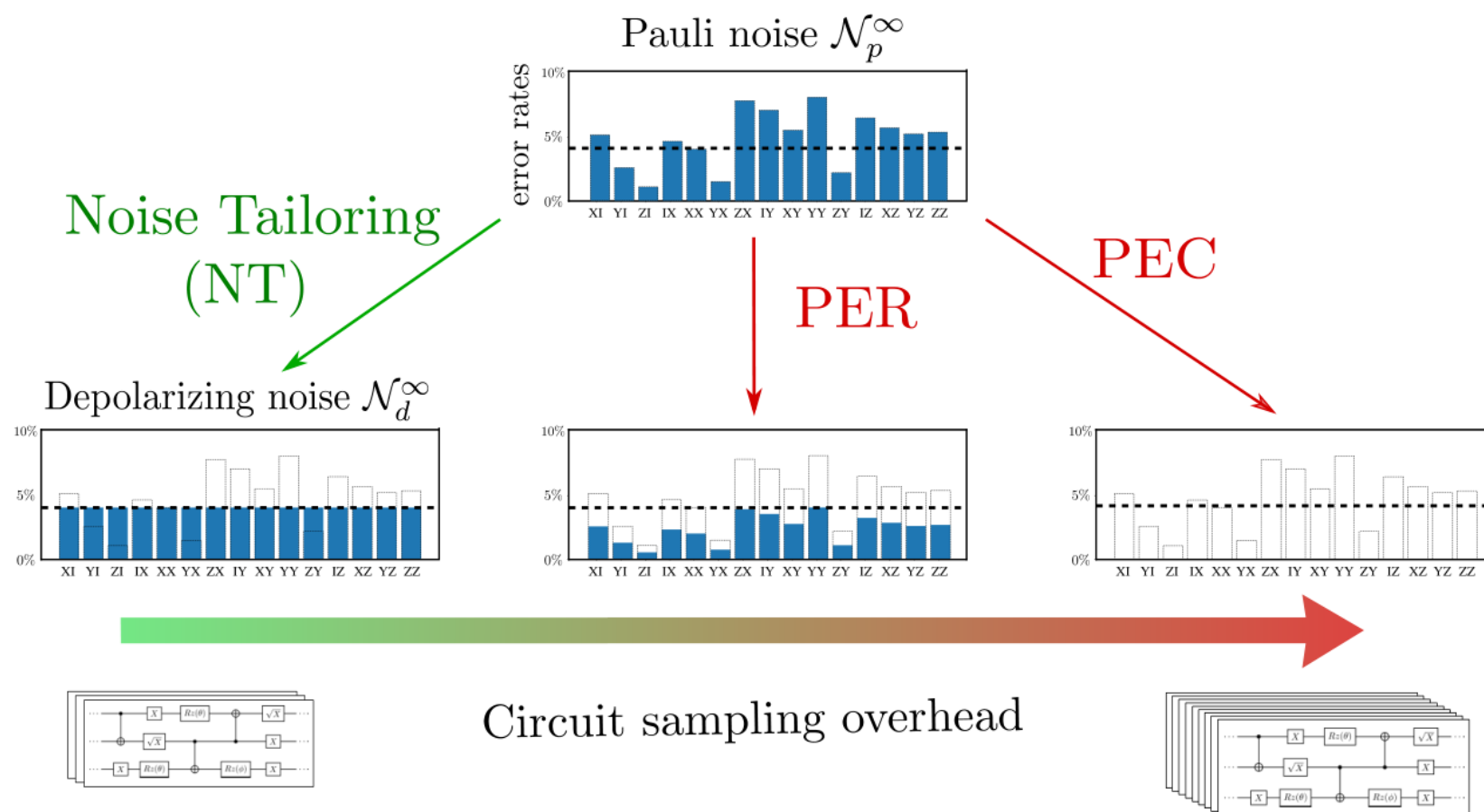


⇐ NEC used for all curves

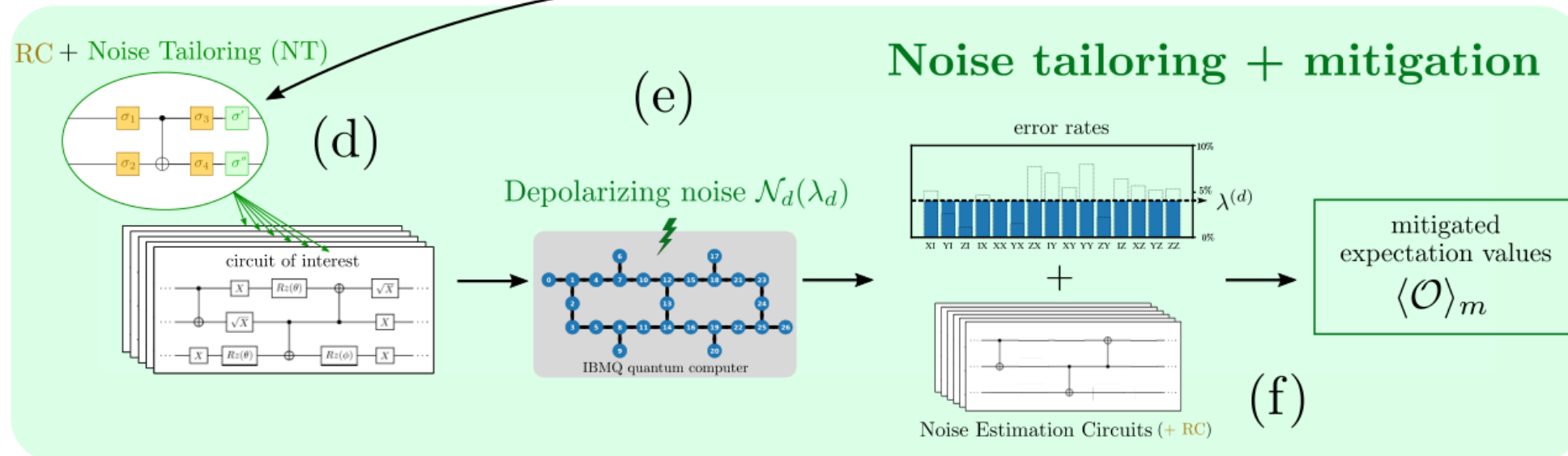
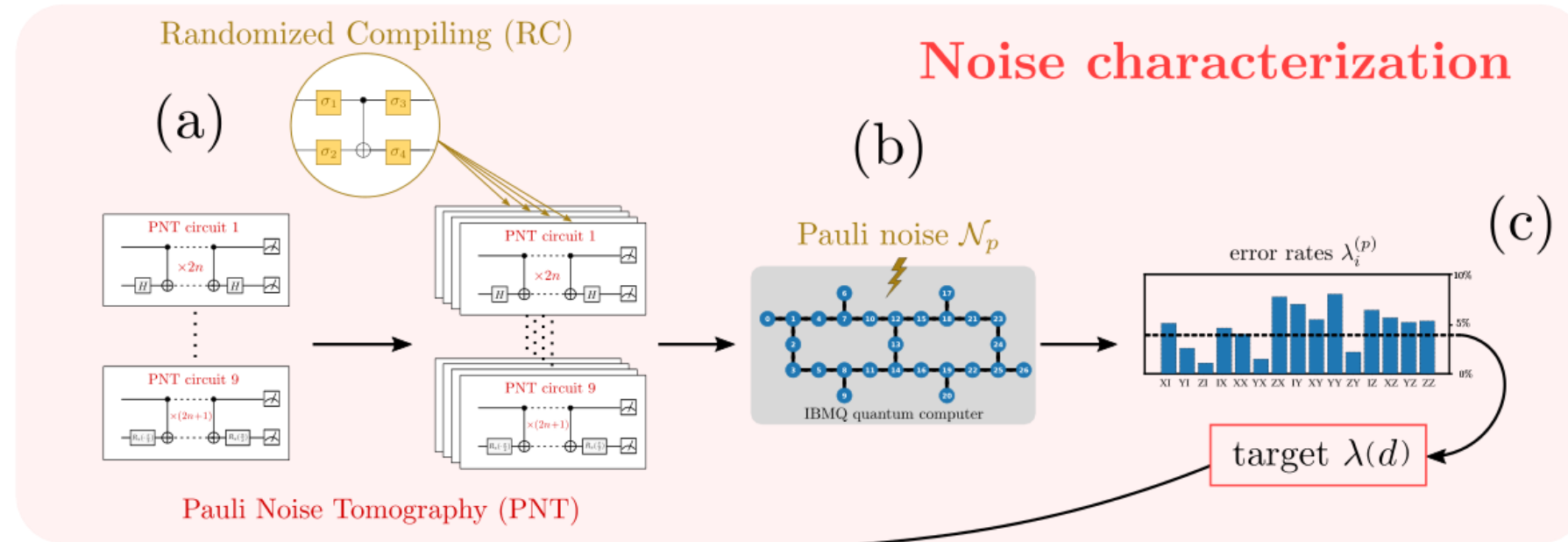
Why not change the noise shape?

NEC requires global
depolarizing noise

$$\mathcal{E}_n^{\text{glob.}}(\rho) = (1 - \lambda_{\text{glob.}})\rho + \lambda_{\text{glob.}} \frac{\mathbb{I}}{2^N}$$



Noise tailoring (NT) protocol



Choosing the target noise

Our target: depolarizing noise.

$$\mathcal{N}_d^\infty(\rho) = (1 - 15\lambda_d)\rho + \lambda_d \sum_{i=1}^{15} \sigma_i^{2\text{-qubit}} \rho \sigma_i^{2\text{-qubit}}$$

Reason: NEC mitigation

$$\langle \hat{O} \rangle_{\text{mitigated}} = \frac{\langle \hat{O} \rangle_{\text{measured}}}{\mathcal{F}_{\text{NEC}}} \sim \frac{\langle \hat{O} \rangle_{\text{measured}}}{\langle 1 \rangle_{\text{measured}}}$$

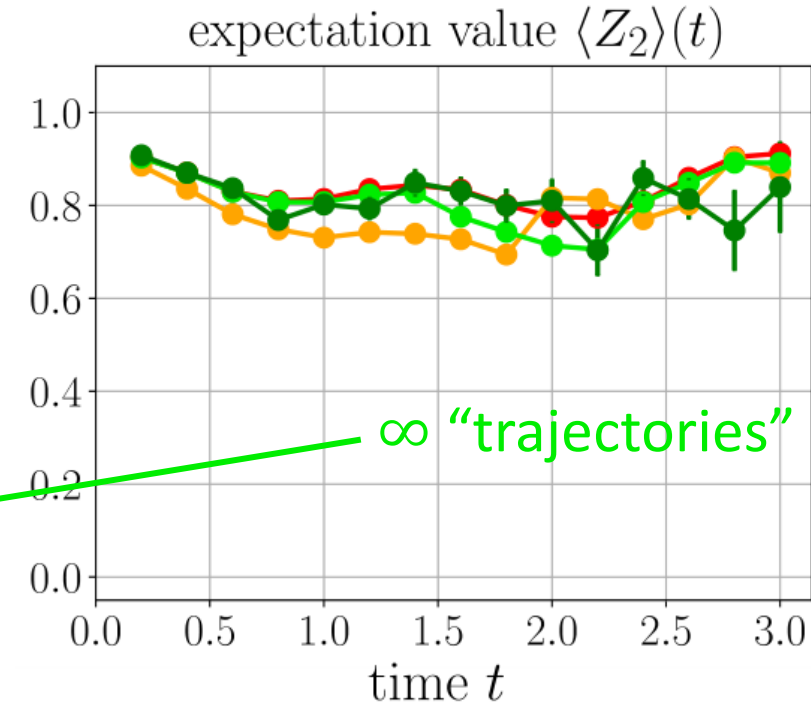
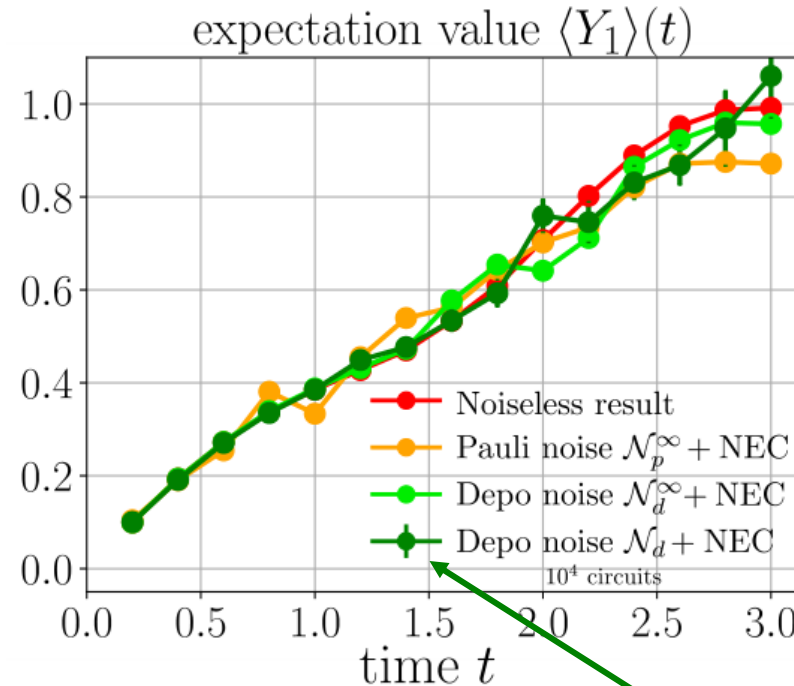
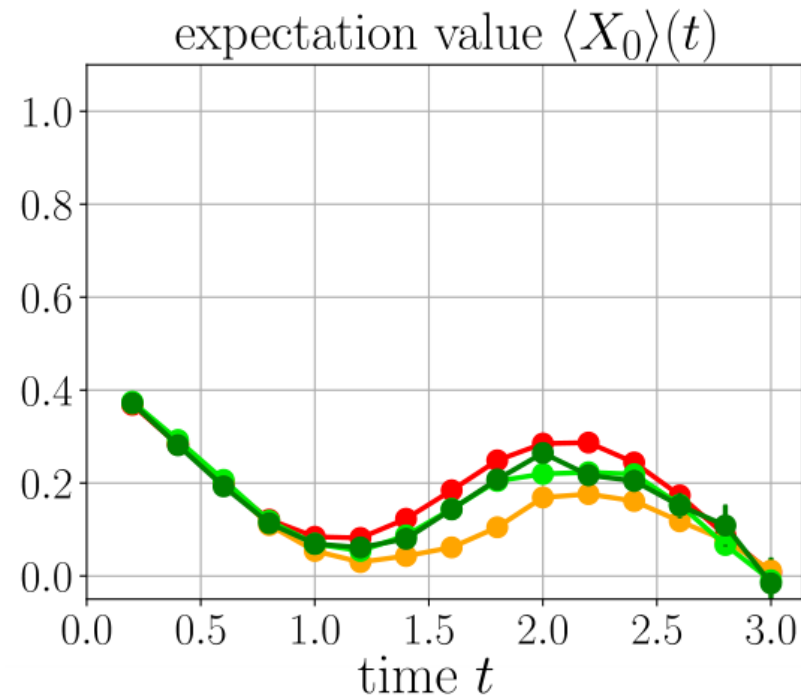
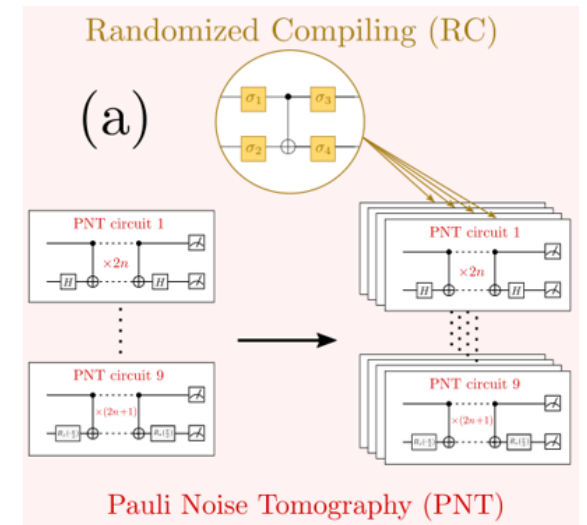
The effect of finite circuit («trajectory») sampling:

$$\langle \hat{O} \rangle_{\text{mitigated}} = \langle \hat{O} \rangle_{\text{mitigated}}^\infty + \frac{\gamma^{n_{\text{CNOT}}}}{\mathcal{F}_{\text{NEC}}} [\text{Sampling errors}]$$

Choose λ_d to minimize $\frac{\gamma^{n_{\text{CNOT}}}}{\mathcal{F}_{\text{NEC}}}$

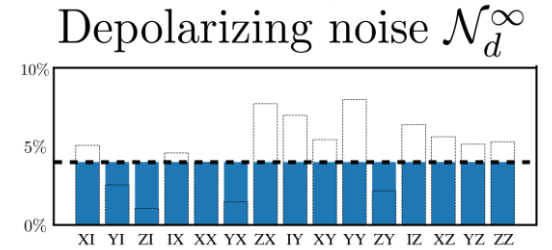
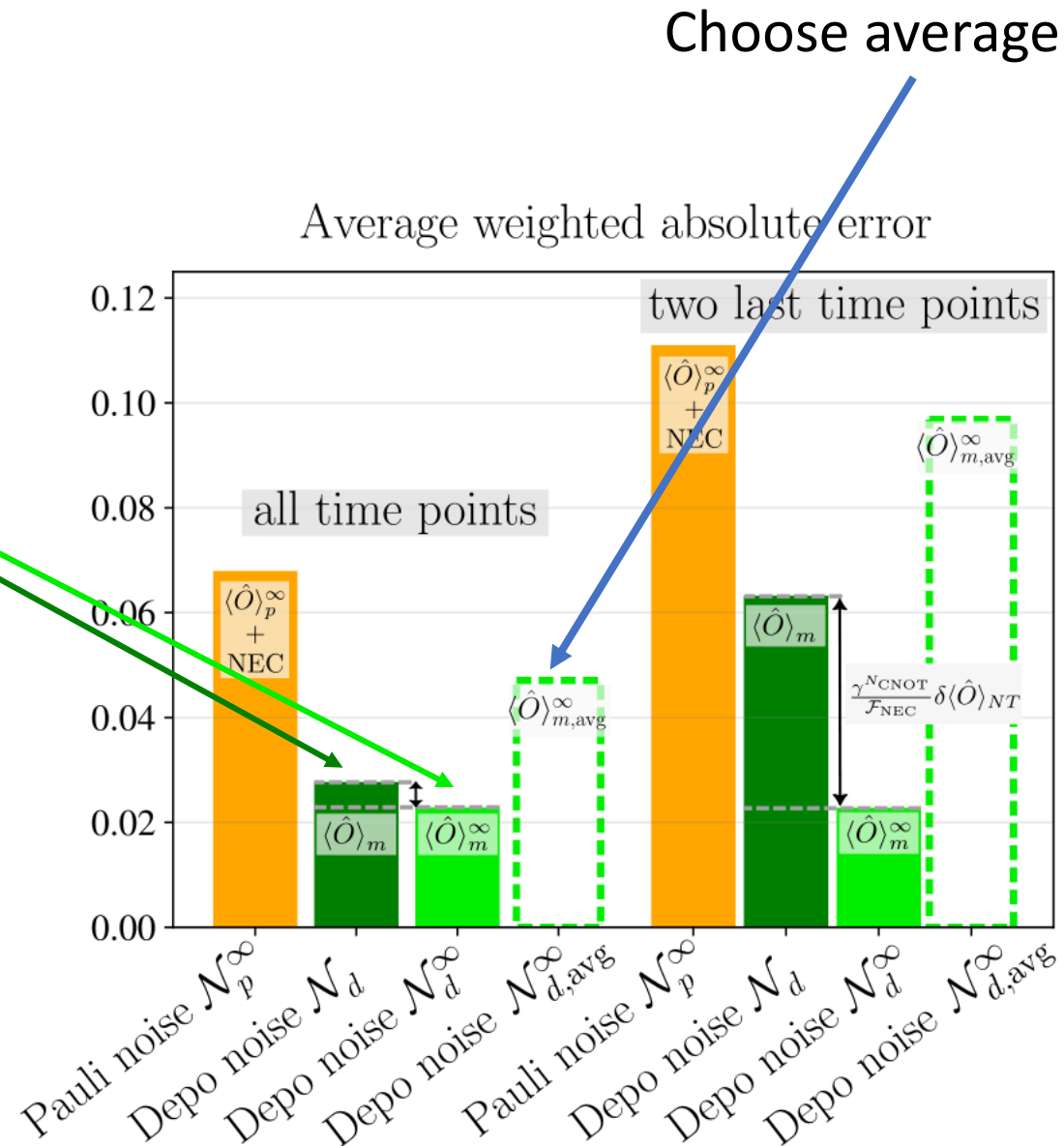
Classical simulations of NT

Noise extracted from actual
IBM quantum computer (**ibm_hanoi**, 27 qubits)

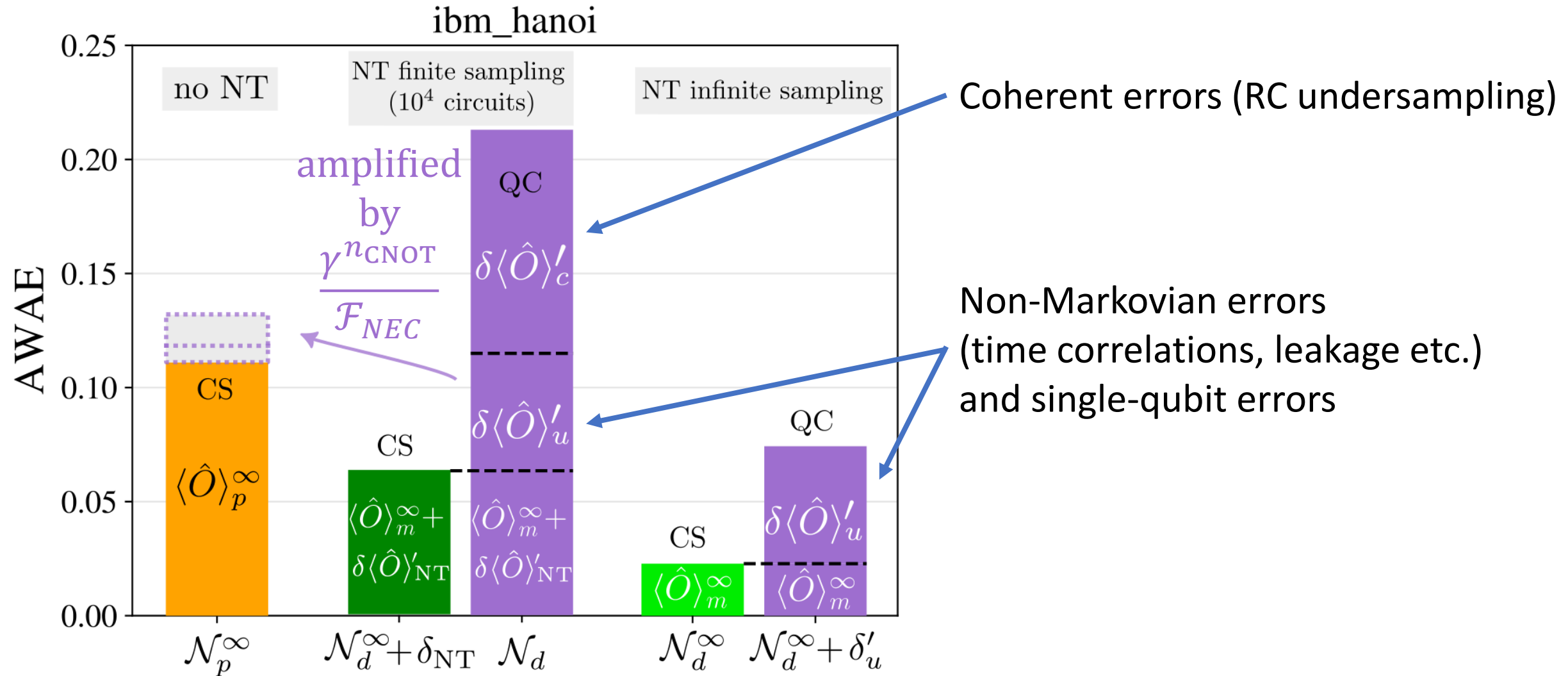


Classical simulations of NT

Choose λ_d to
minimize $\frac{\gamma^{n_{\text{CNOT}}}}{\mathcal{F}_{\text{NEC}}}$

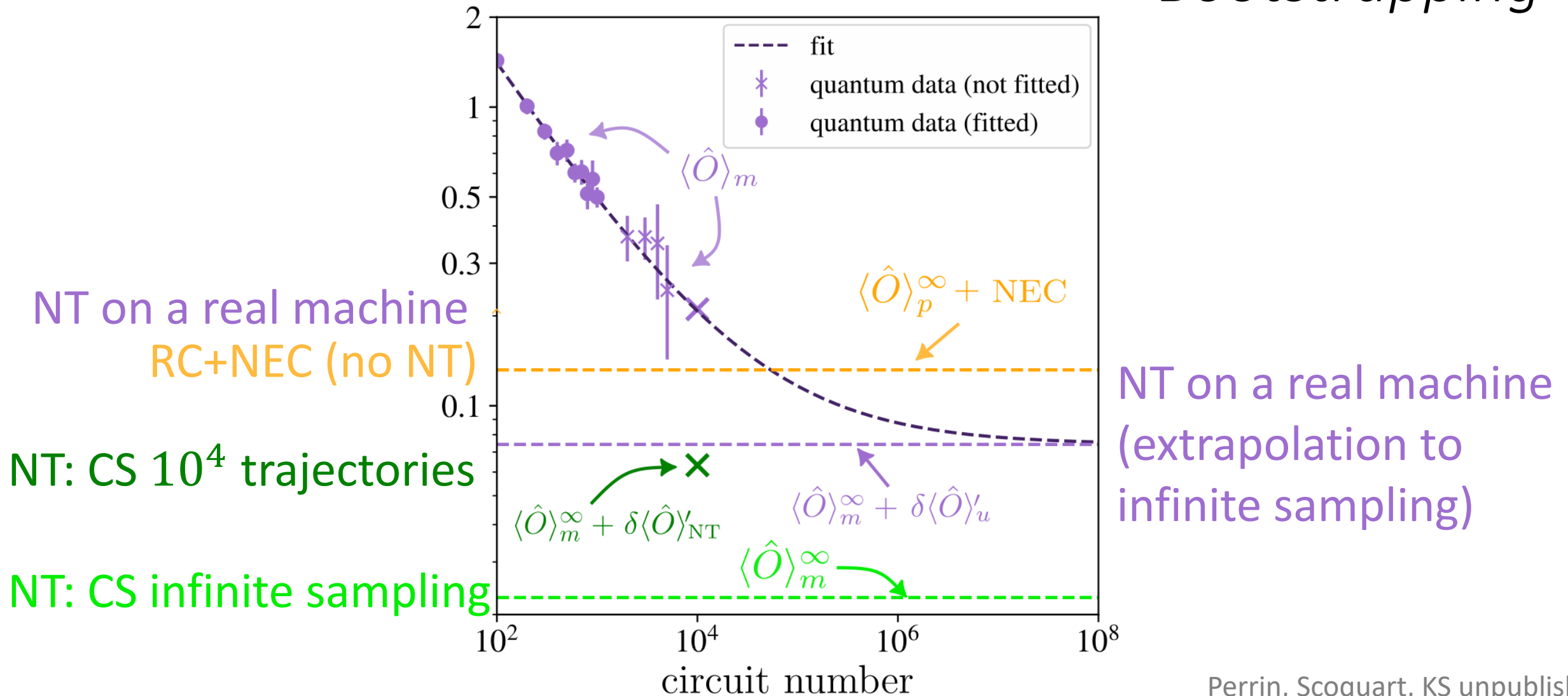


NT on an actual quantum computer



How to estimate accuracy at infinite sampling on a quantum computer?

Bootstrapping

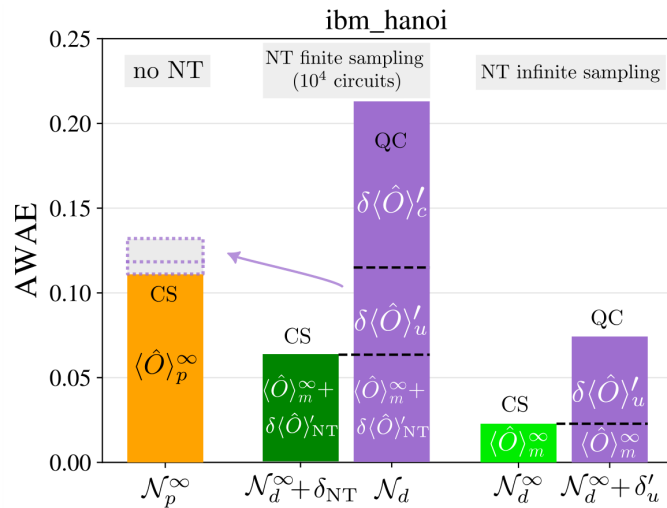
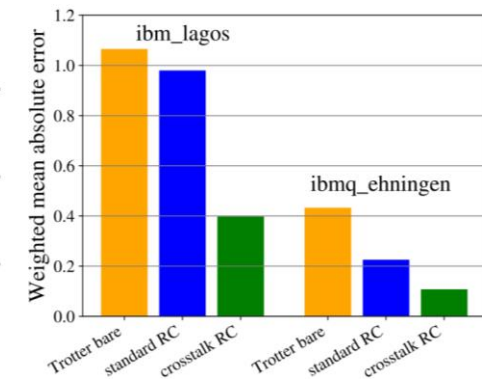
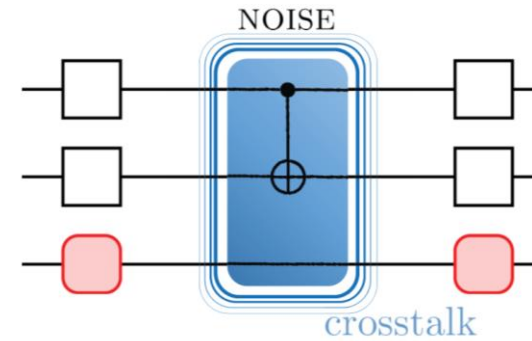


Conclusions



Application-based benchmarking
gives insight about error sources

RC vs cRC to
characterise crosstalk

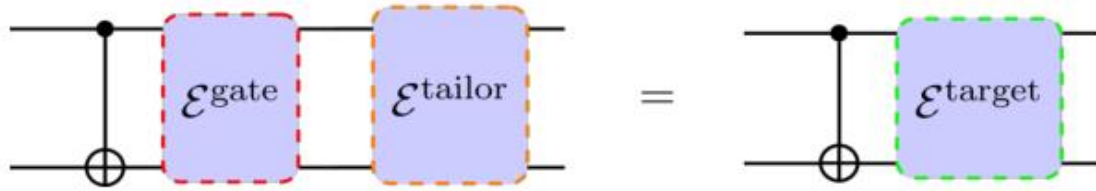


Noise tailoring to
characterize (small) but important sources of noise
(residual coherent; single-qubit & non-Markovian)

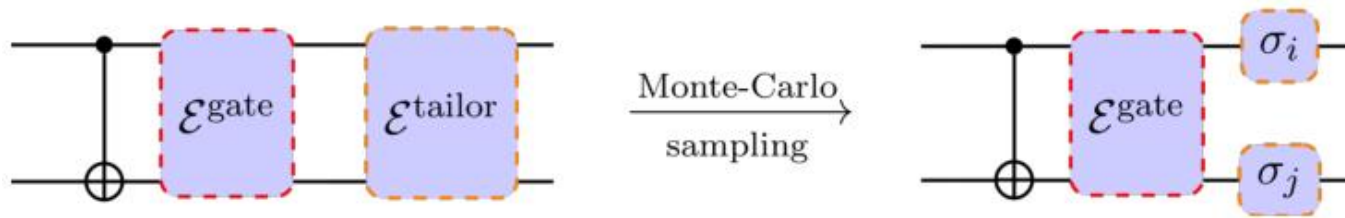
Thank you for attention!

How do PEC and PER work?

(a)



(b)

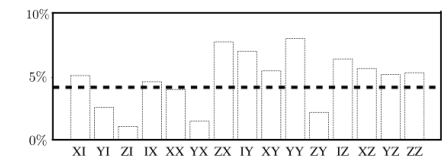
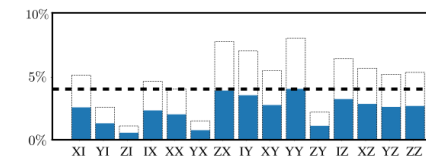


Sample σ_i, σ_j

Get target noise channel

PER

PEC



Temme, Bravyi, Gambetta, PRL **119**, 180509 (2017)

Berg, Mineev, Kandala, Temme, Nature Physics **19**, 1116 (2023)

Noise channel representations

χ -matrix representation:

$$\rho \rightarrow \mathcal{E}(\rho) = \sum_{a,b} \chi_{ab} P_a \rho P_b \quad \text{with n-qubit Pauli matrices } P_a \in \{I, X, Y, Z\}^{\otimes n_{\text{qubits}}}$$

Pauli noise: $\chi_{ab} = p_a \delta_{ab}$, $\sum_a p_a = 1$

Pauli transfer-matrix (PTM) representation:

$$\rho = \rho_a P_a \quad \left(\text{or } \rho_a = \frac{1}{2^{n_{\text{qubits}}}} \text{Tr}(P_a \rho) \right)$$

$$\{\rho_a\} \rightarrow \left\{ \sum_b E_{ab} \rho_b \right\}$$

$$\text{PTM: } E_{ab} = \frac{1}{2^{n_{\text{qubits}}}} \text{Tr}(P_a \mathcal{E}(P_b))$$

Pauli noise: $E_{ab} = f_a \delta_{ab}$

Connection

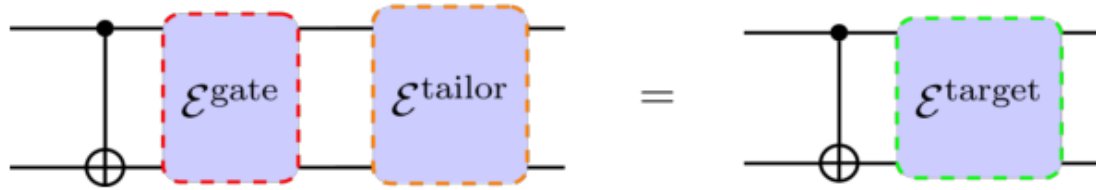
(Walsh-Hadamard transform):

$$p_a = \frac{1}{4^{n_{\text{qubits}}}} \sum_b (-1)^{\langle P_a, P_b \rangle_{\text{sp}}} f_b$$

Symplectic inner product:

$$\langle P_a, P_b \rangle_{\text{sp}} = \begin{cases} 0, & \text{if } P_a P_b = +P_b P_a \\ 1, & \text{if } P_a P_b = -P_b P_a \end{cases}$$

How do PEC and PER work?

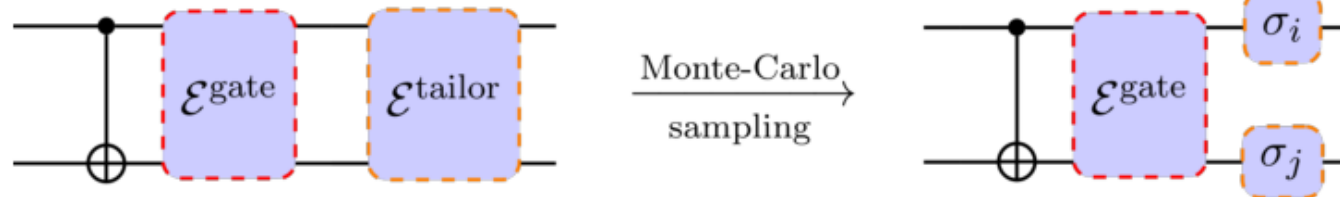


$$E^{\text{target}} = E^{\text{tailor}} \times E^{\text{gate}}$$

$$\Rightarrow E^{\text{tailor}} = E^{\text{target}} \times (E^{\text{gate}})^{-1} = f_a^{\text{tailor}} \delta_{ab}$$

$$p_a^{\text{tailor}} = \frac{1}{4^{n_{\text{qubits}}}} \sum_b (-1)^{\langle P_a, P_b \rangle_{\text{sp}}} f_b^{\text{tailor}}$$

$$\mathcal{E}(\rho) = \sum_a p_a^{\text{tailor}} P_a \rho P_a$$



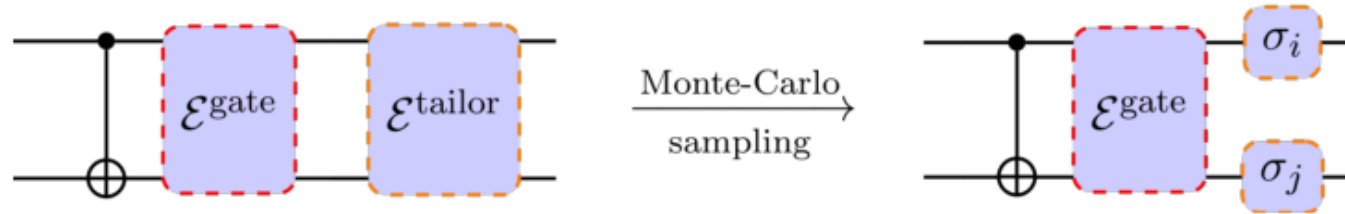
Temme, Bravyi, Gambetta, PRL **119**, 180509 (2017)

Berg, Mineev, Kandala, Temme, Nature Physics **19**, 1116 (2023)

How do PEC and PER work?

$$p_a^{\text{tailor}} = \frac{1}{4^{n_{\text{qubits}}}} \sum_b (-1)^{\langle P_a, P_b \rangle_{\text{sp}}} f_b^{\text{tailor}}$$

$$\mathcal{E}(\rho) = \sum_a p_a^{\text{tailor}} P_a \rho P_a$$



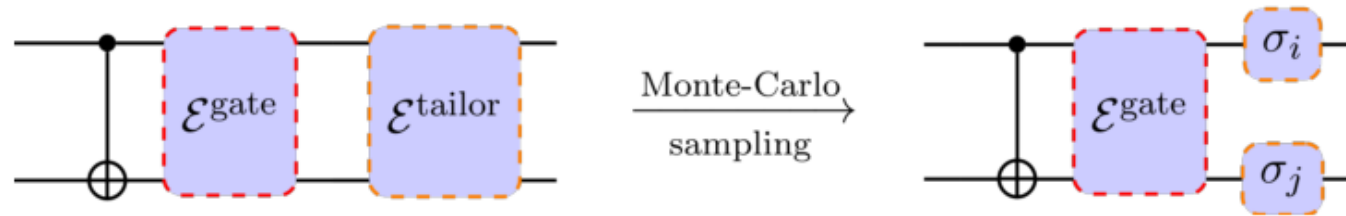
Problem: p_a^{tailor} can be negative

How do PEC and PER work?

$$q_a^{\text{tailor}} = \frac{1}{4^{n_{\text{qubits}}}} \sum_b (-1)^{\langle P_a, P_b \rangle_{\text{sp}}} f_b^{\text{tailor}}$$

$$\mathcal{E}(\rho) = \sum_a q_a^{\text{tailor}} P_a \rho P_a$$

$$\text{Sample: } \tilde{p}_a^{\text{tailor}} = \frac{|q_a^{\text{tailor}}|}{\gamma}, \quad \gamma = \sum_a |q_a^{\text{tailor}}| > 1$$



Take the sign q_a^{tailor} into account when calculating the Monte-Carlo average

Multiply the average by $\gamma^{n_{\text{CNOT}}}$

$\Rightarrow$ exponentially costly to keep a fixed error bar (sign problem)

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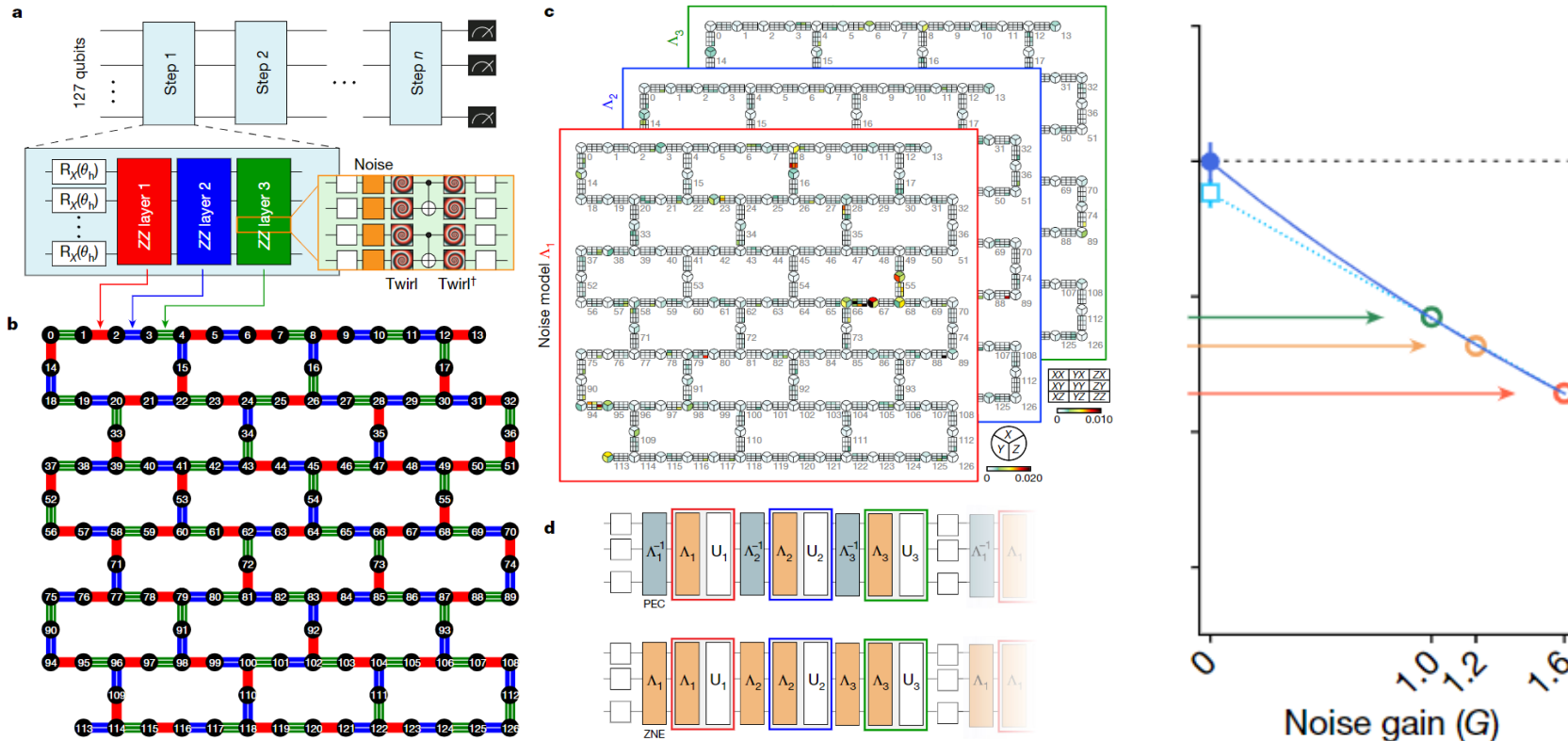
How do PEC and PER work?

Multiply the average by $\gamma^{n_{\text{CNOT}}}$

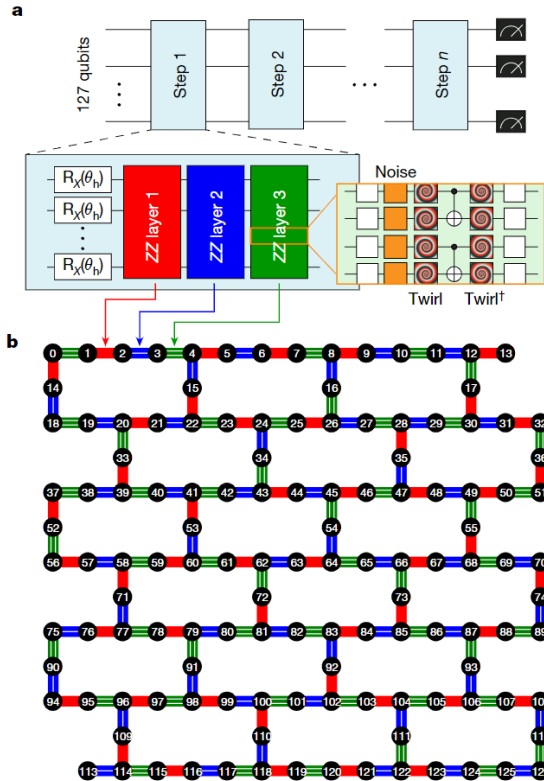
⇒ exponentially costly when reducing noise

Possible solution: increase noise (avoid quasiprobability distributions!)

E.g., IBM “quantum utility” experiment:



Quantum utility?



Kim et al., Nature **618**, 500 (2023)

Quantum Disadvantage

Or, simulating IBM's 'quantum utility' experiment with a Commodore 64

Anonymous

quantum.disadvantage@proton.me

<https://quantum-disadvantage.co.uk>

March 29, 2024

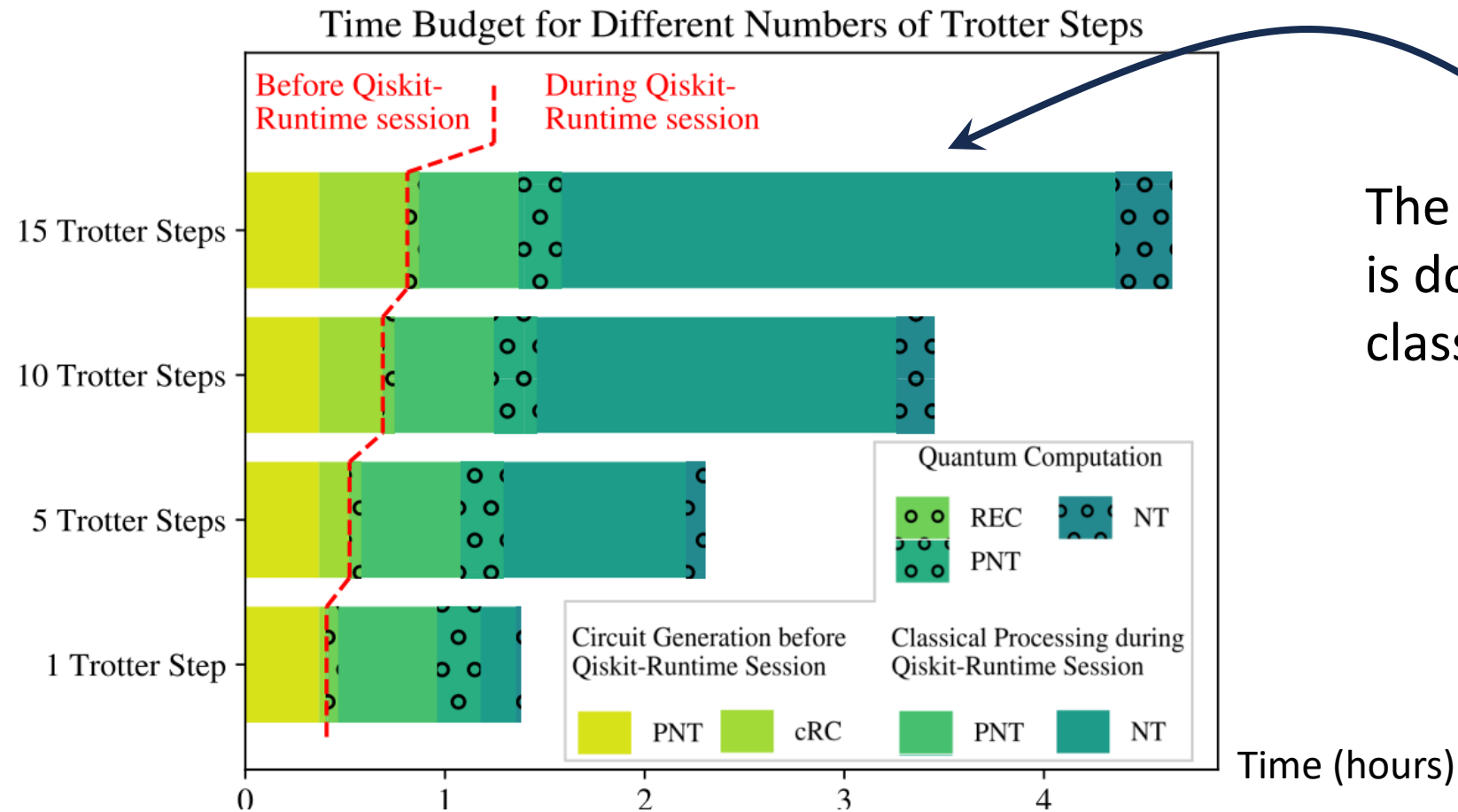
Abstract

measuring expectation values of a Trotterized Ising model on their 127-qubit quantum device, claiming that their results were unlikely to be replicable on a classical computer. In this work, we implement a classical simulation of the same experiment using a Commodore 64. Our simulation requires less than 15kB of memory and less than 100ms of time per data point. To accomplish this we use a variant of the sparse Pauli basis introduced by Begušić and Chan. We show that aggressive truncation combined with error mitigation is sufficient to replicate the results of the quantum device. We show that aggressive truncation combined with error mitigation is sufficient to replicate the results of the quantum device.



Figure 2: The experimental setup – a Commodore 64 is connected to a monitor through a composite video to HDMI converter, with the code cartridge inserted into the expansion port.

Cost of increasing sampling?



The computation time is dominated by classical generation of trajectories

(Can be much improved with adjusting the way of storing circuits?)

Note: noise evolves in time: need to be fast enough

Solution to the portability issue: QLM/Qaptiva



Welcome to Qaptiva Access Portal

QLMaaS-1.9.1

Qaptiva Access is a software solution that extends myQLM to submit Quantum jobs to a Qaptiva Appliance: Qaptiva 800s Plugins and QPUs are available through myQLM.

Install

Get started

Configure

Qaptiva Access client is available on [PyPI](#). This python library can be installed from your terminal using the following command:

```
python3 -m pip install myqlm
```

Useful links



Documentation



Display Notebooks



Download Notebooks

<https://qlm35e.neasqc.eu/>

Solution to the portability issue: QLM/Qaptiva

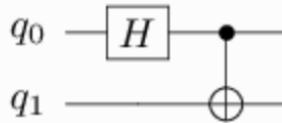


Welcome to Qaptiva Access Portal

QLMaaS-1.9.1

Quantum Hello World

The following code snippet creates and simulates a simple Bell pair circuit:



Functional mode

Sequential mode

```
from qat.lang import qrount, H, CNOT

@qrount
def bell_pair():
    H(0)
    CNOT(0, 1)

result = bell_pair().run()

for sample in result:
    print(f"State {sample.state} amplitude {sample.amplitude}")
```

```
State |00> amplitude (0.7071067811865475+0j)
State |11> amplitude (0.7071067811865475+0j)
```

n jobs to a Qaptiva Appliance: Qaptiva 800s

Configure

led from your terminal using the following



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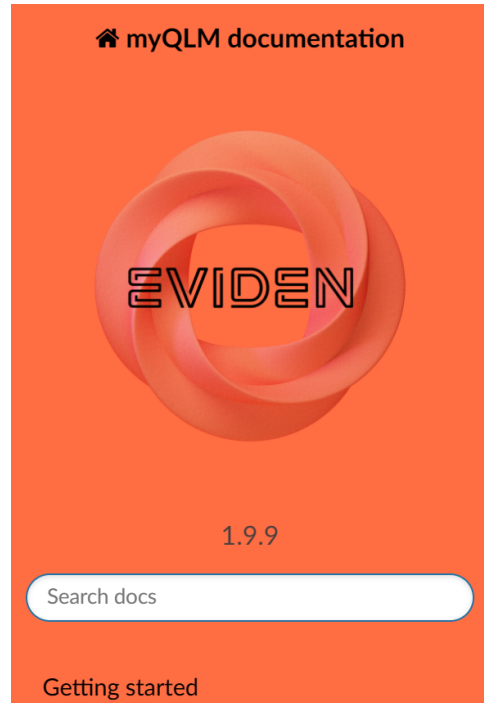


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Qaptiva (paid) — advanced simulation
+ (in the future) access to quantum hardware

Solution to the portability issue: QLM/Qaptiva



» Welcome page

myQLM – Quantum Python Package

myQLM is the quantum software stack developed by [Eviden](#), for writing, simulating, optimizing, and executing quantum programs. Through a Python interface, it provides:

- a **powerful semantic** for [writing quantum algorithms](#) (gate-based programming, analog programming, or quantum annealing programming)
- a **versatile execution stack** for [running quantum jobs](#), including an easy handling of [observables](#), special tools for carrying NISQ-oriented [variational methods](#) (such as VQE, QAOA), an easy API for [designing custom plugins](#) (e.g. compilation), as well as for connecting to any Quantum Processing Unit (QPU)
- a **seamless interface** to [available quantum processors and major quantum programming frameworks](#)

<https://myqlm.github.io/>

Solution to the portability issue: QLM/Qaptiva



Interoperability

Warning

Interoperability packages are deprecated for Python versions 3.6 and 3.7

This package enables access to other quantum programming environments such as Qiskit, ProjectQ, PyQuil, Cirq ... This package will not automatically install dependency packages because someone who want to interface with Qiskit may not want to interface with Cirq... The desired quantum environment can be cherry-picked using the pip command:

Qiskit

ProjectQ

Cirq

PyQuil

All frameworks

```
pip install myqlm-interop[qiskit_binder]
```

myQLM documentation



» Welcome page

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[seamless interface](#) to [available quantum processors](#) and [major quantum programming networks](#)

<https://myqlm.github.io/>

myQLM = my Quantum Learning Machine

myQLM (free) — gate-based programming and noiseless simulation

Lots of examples