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Materials science and chemistry with quantum algorithms: from the textbook to the processor

TERATEC TQCI - Quantum algorithms in the NISQ era

Thursday, November 14th 2024

Thomas Ayrat
Eviden Quantum Lab, France

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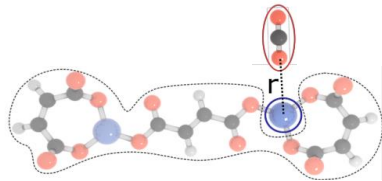
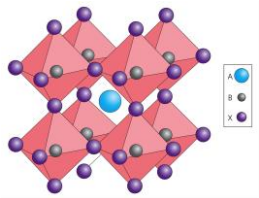
an atos business

The textbook:

On the one hand:

A complex quantum system

$$i\hbar \frac{d|\Psi\rangle}{dt} = H(t)|\Psi\rangle$$

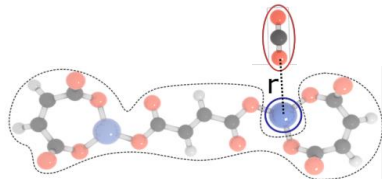
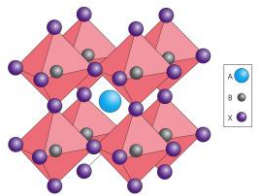


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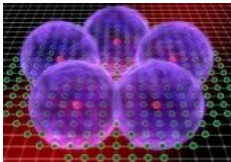
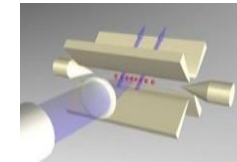
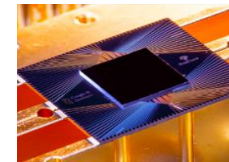
$$i\hbar \frac{d|\Psi\rangle}{dt} = H(t)|\Psi\rangle$$



On the other hand:

A complex... artificial... quantum system

$$i\hbar \frac{d|\tilde{\Psi}\rangle}{dt} = \tilde{H}(t)|\tilde{\Psi}\rangle$$

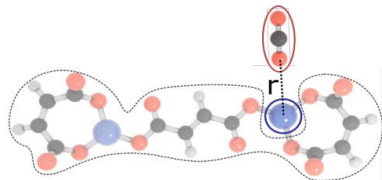
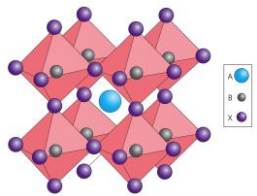


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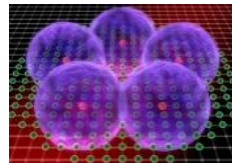
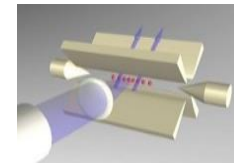
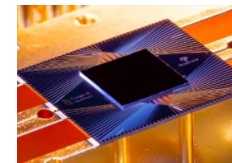
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On the other hand:

A complex... artificial... quantum system

$$i\hbar \frac{d|\tilde{\Psi}\rangle}{dt} = \tilde{H}(t)|\tilde{\Psi}\rangle$$



If $\tilde{H} \approx H$, we learn something about $|\Psi\rangle$ by measuring $|\tilde{\Psi}\rangle$!

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Exponential advantage for quantum dynamics (Lloyd '96)

Materials science and chemistry: low-energy states

Ground state search:

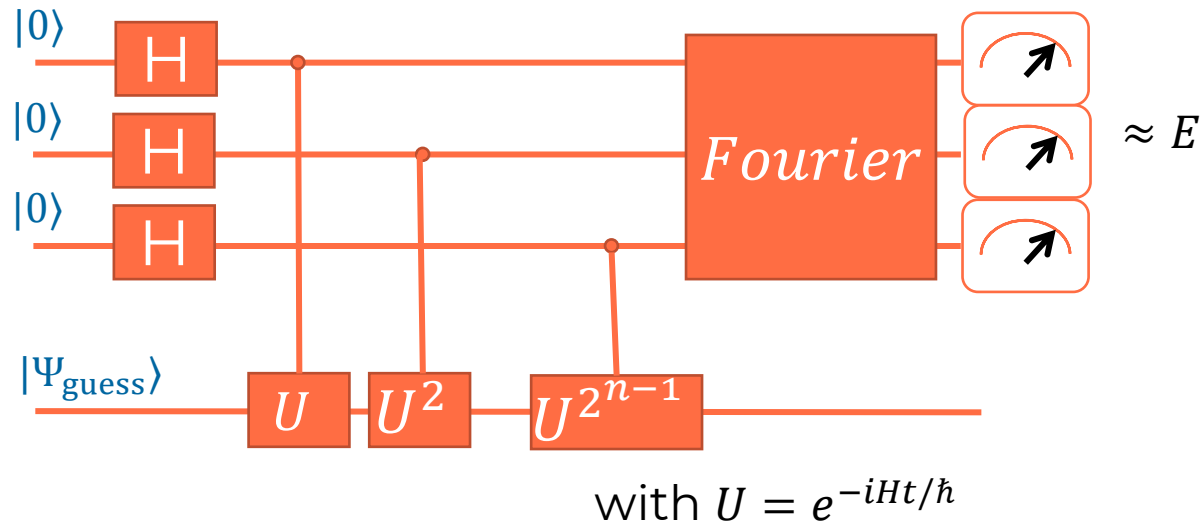
$$H|\Psi\rangle = E|\Psi\rangle$$

Materials science and chemistry: low-energy states

Ground state search:

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Quantum phase estimation (QPE) algorithm
(Kitaev 95)



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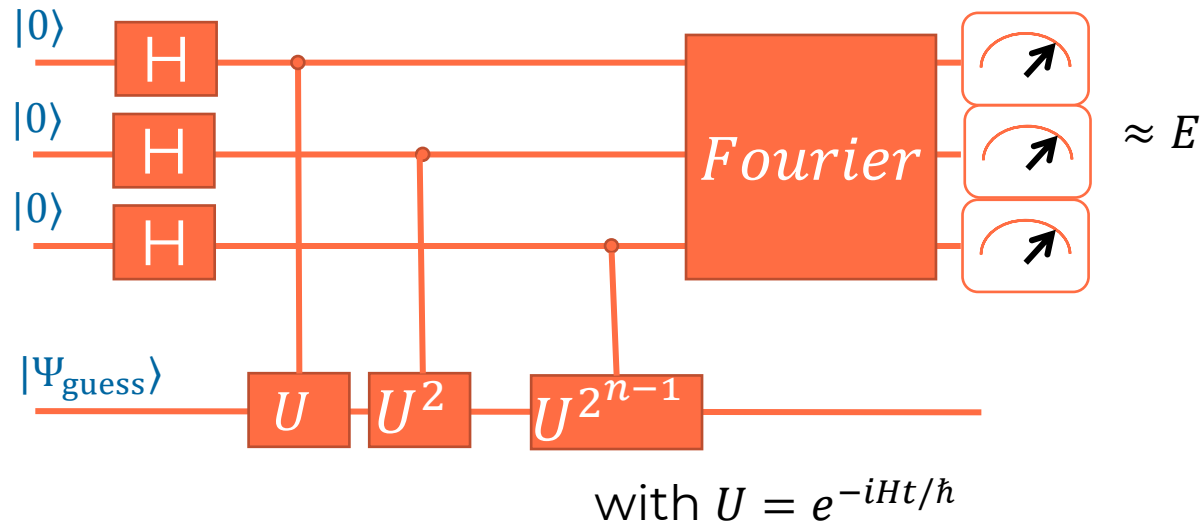
Too long!

Materials science and chemistry: low-energy states

Ground state search:

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**Quantum phase estimation (QPE) algorithm
(Kitaev 95)**



Large Scale Quantum: Tomorrow



Quantum error corrected computers

A lot (millions) of high-quality qubits

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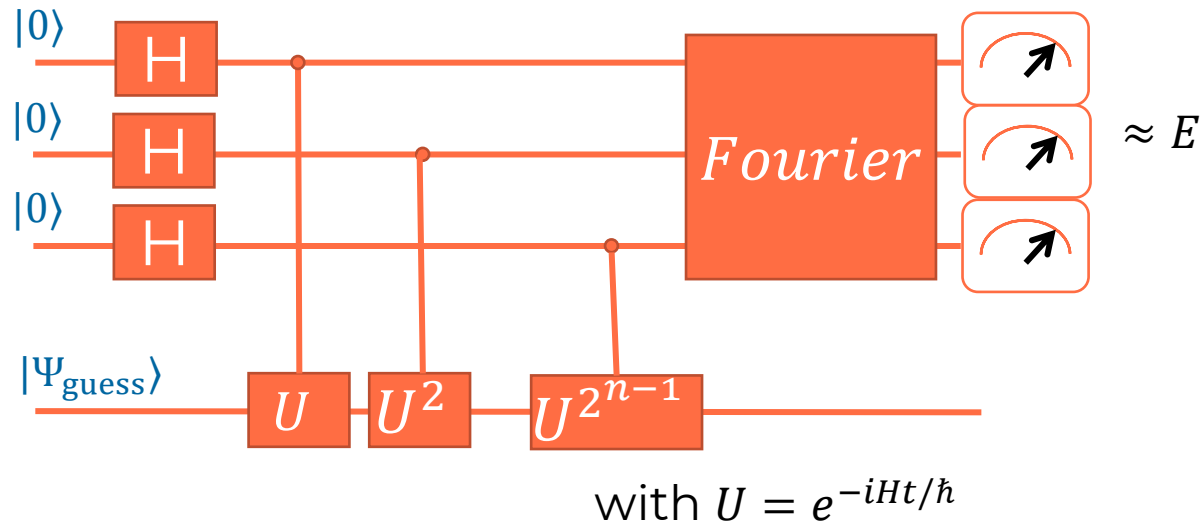
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Most advanced experiments (Rydberg, ions, superconducting qubits):

Only 10-100 physical qubits,
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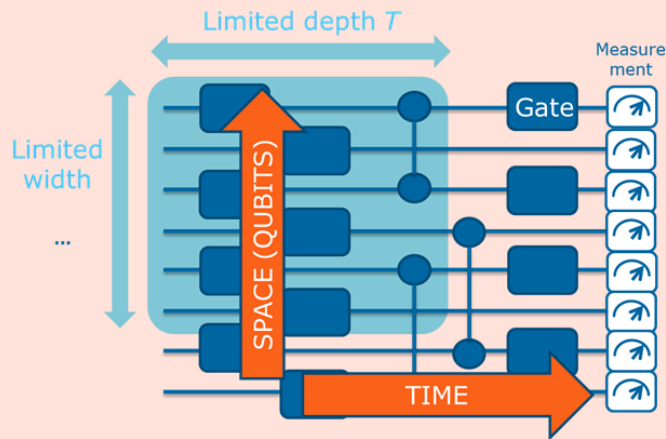
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Materials science and chemistry: low-energy states

Noisy Intermediate Scale Quantum: Today



- Small number of qubits (10-1000 today)
- High error rates (100-1000 gates)



Exponential decay of fidelity:

$$F = e^{-pN_g}$$

Error per gate

Number of gates

Large Scale Quantum: Tomorrow



Quantum error corrected computers

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Most advanced experiments (Rydberg, ions, superconducting qubits):

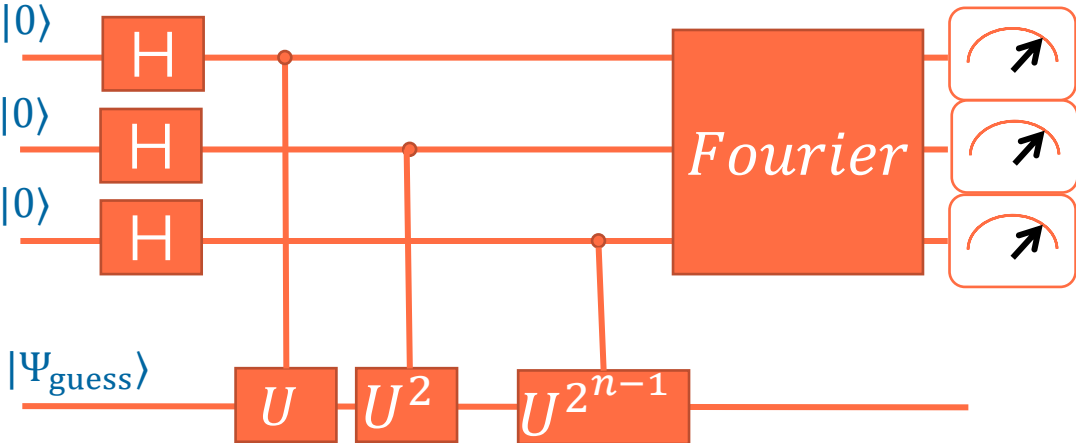
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Too long... also without noise?

Ground state search:

$$H|\Psi\rangle = E|\Psi\rangle$$

Quantum phase estimation (QPE) algorithm (Kitaev 95)



Key point: role of overlap

$$\Omega = |\langle \Psi_{\text{guess}} | \Psi_0 \rangle|^2$$

Need $O(\frac{1}{\Omega})$ repetitions of QPE!

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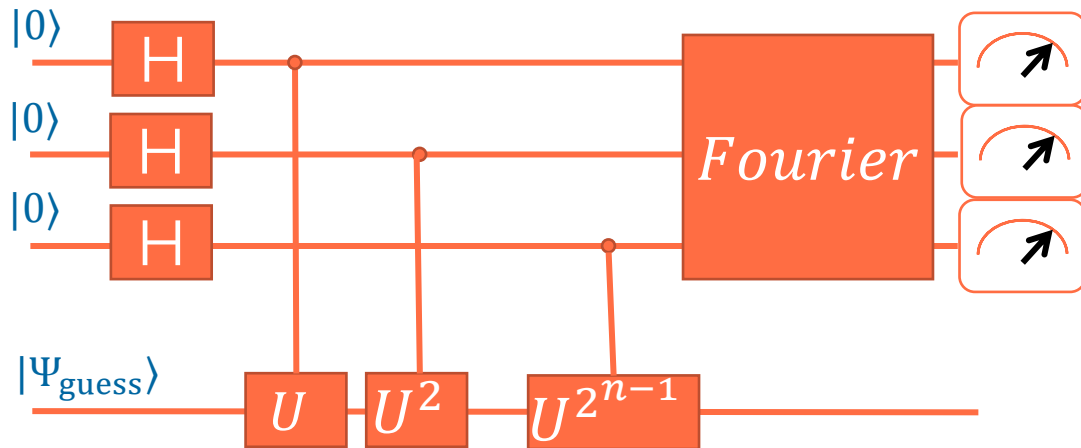
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Key point: role of overlap

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Need $O(\frac{1}{\Omega})$ repetitions of QPE!

We found a formula to assess Ω given the energy + variance of Ψ_{guess} (+ estimate of E_0).

Applied it to advanced classical methods.

Outcome:

Ω decreases exponentially with molecule size!

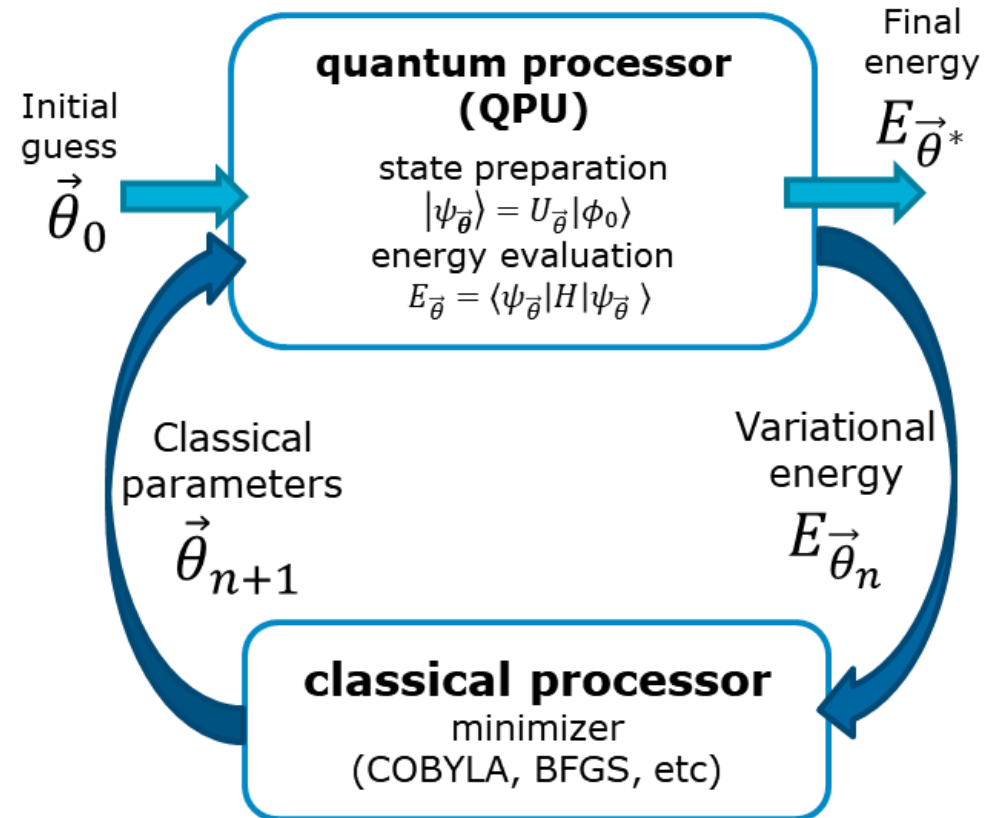
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What can one do with today's processors?

The bread-and-butter NISQ algorithm: the variational quantum eigensolver

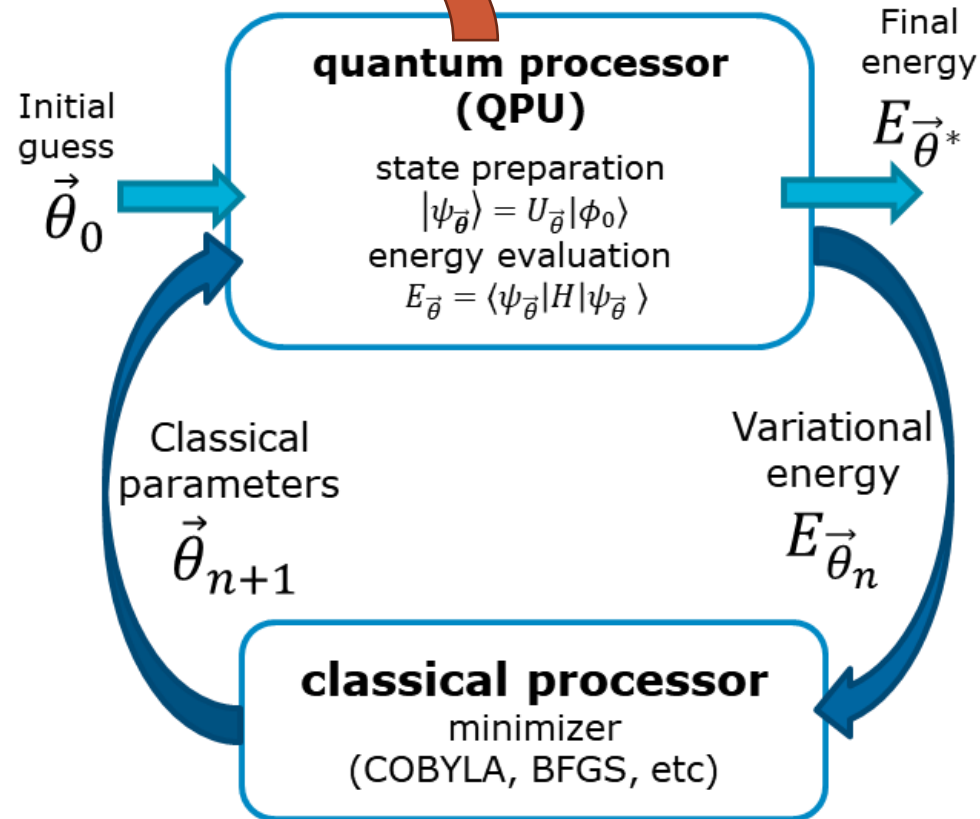
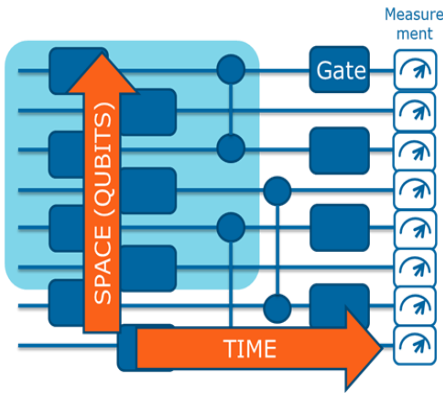
(Peruzzo et al 2014)



The bread-and-butter NISQ algorithm: the variational quantum eigensolver

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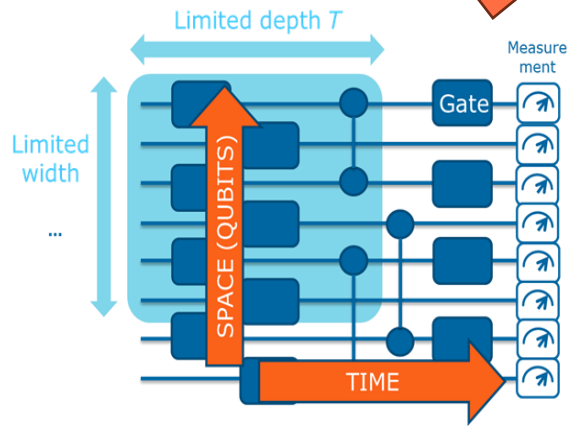
Parametric circuit $U_{\vec{\theta}}$:



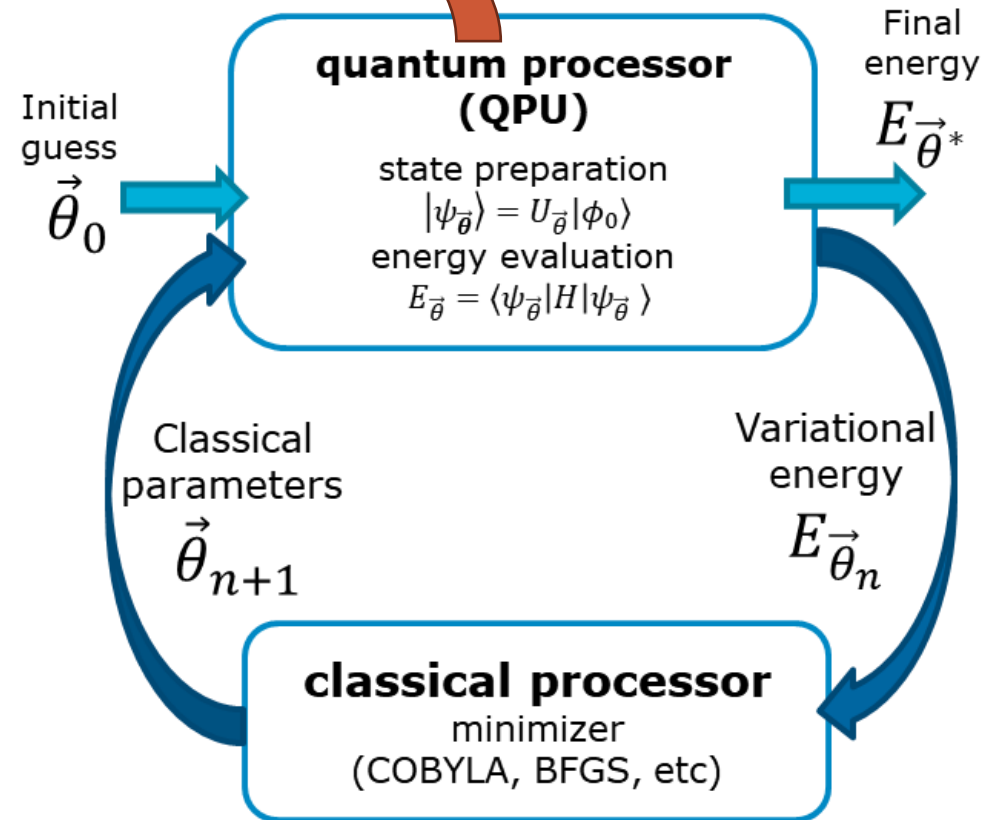
Idea: try to minimize use of quantum resources

Known issues with the variational quantum eigensolver

Parametric circuit $U_{\vec{\theta}}$:

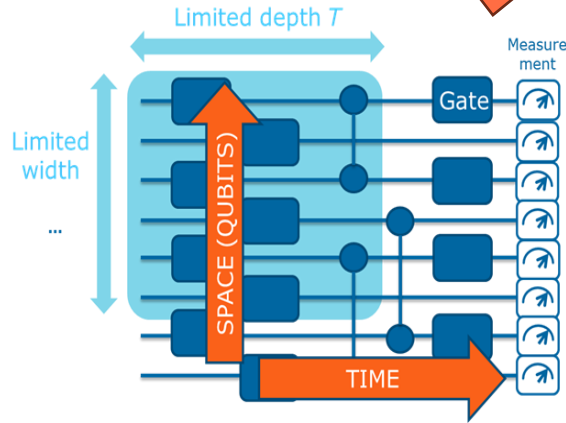


Interesting variational circuits **are still too long!**



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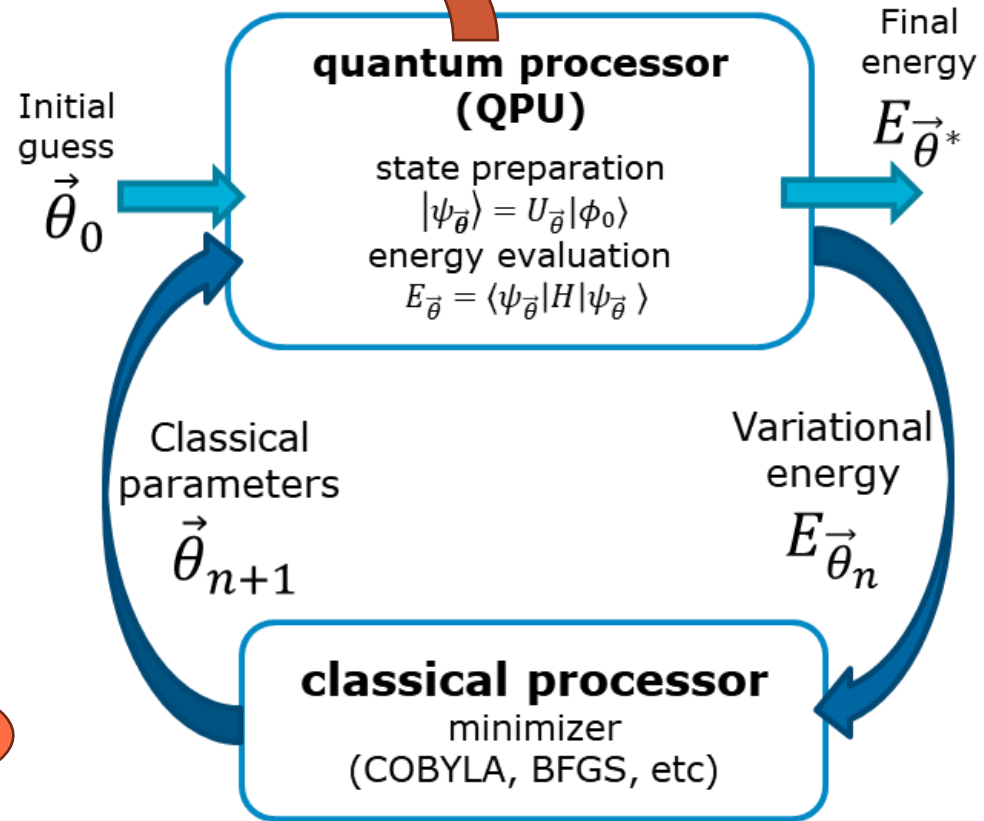


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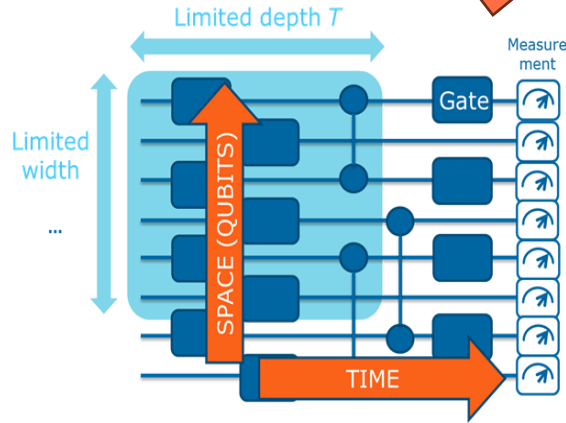
Error per gate

Number of gates



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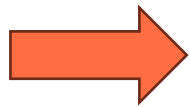


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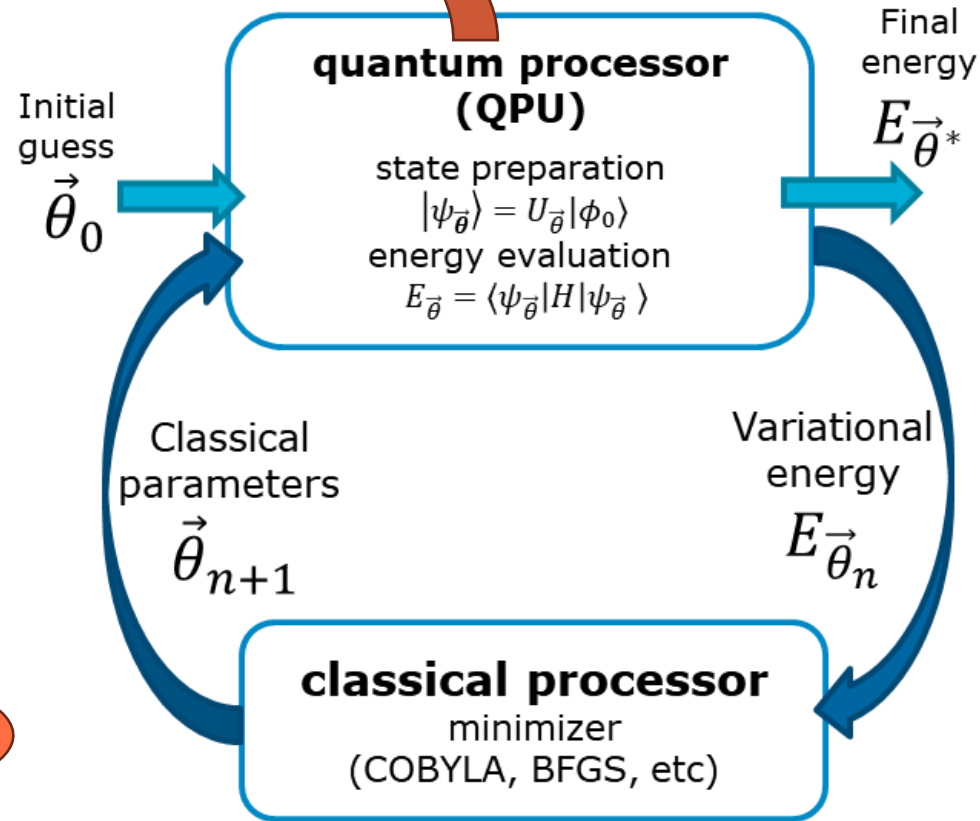
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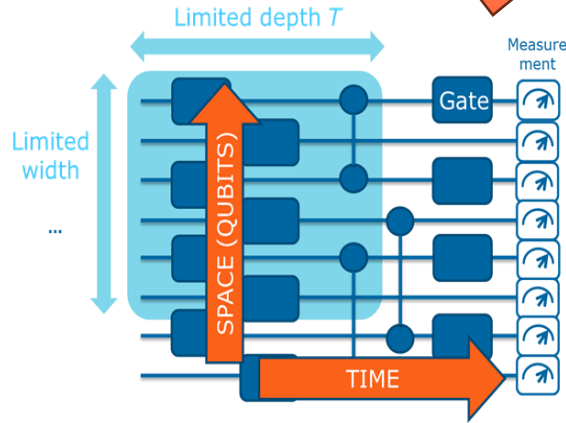
Can we shorten circuits?

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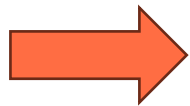


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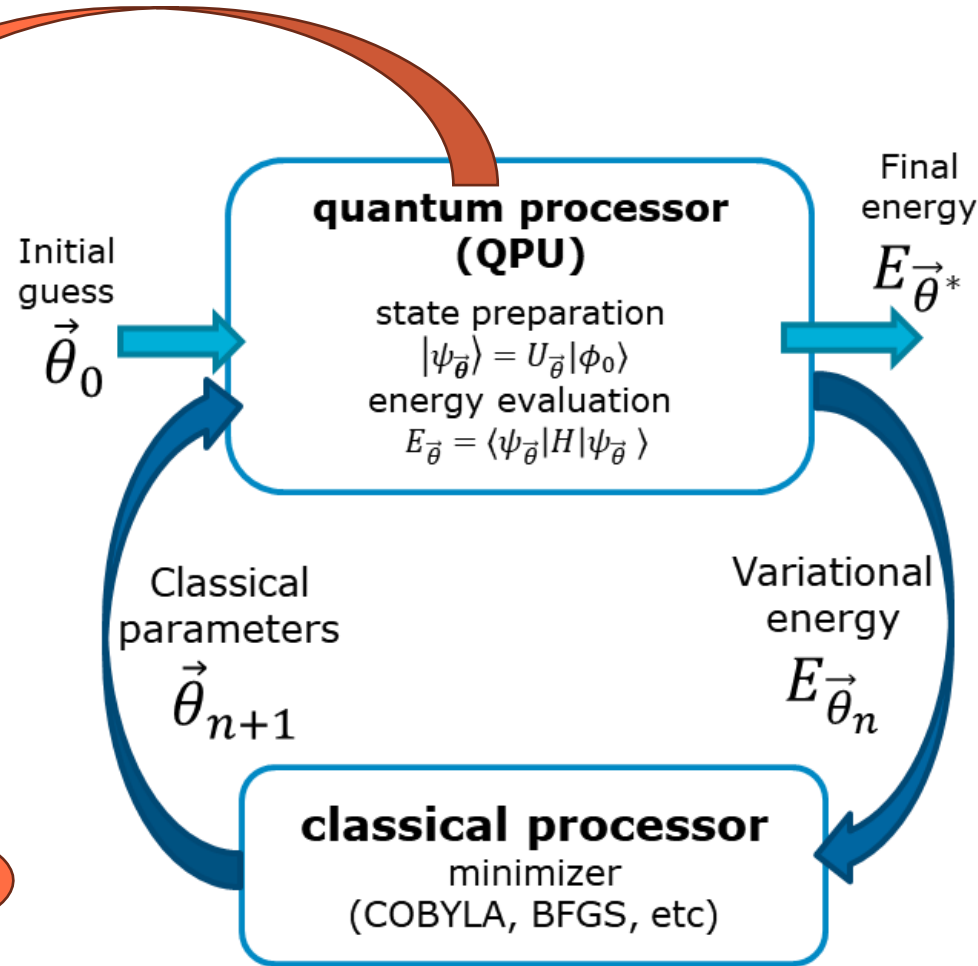
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Electronic structure Hamiltonian:

$$H = \sum_{pq} h_{pq} c_p^\dagger c_q + \frac{1}{2} \sum_{pqrs} h_{pqrs} c_p^\dagger c_q^\dagger c_r c_s$$

Fermion antisymmetry:

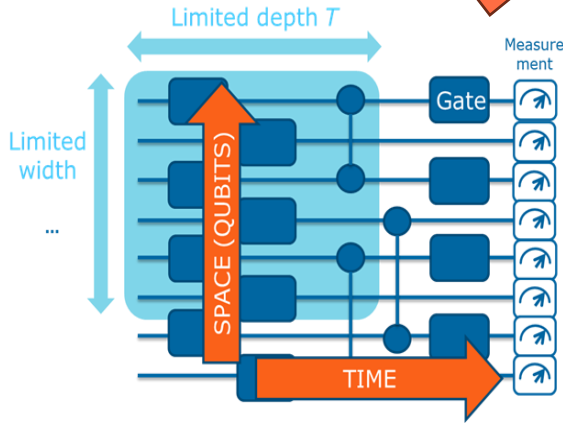
$$c_4^+ |0010\rangle = -|0011\rangle$$

vs. qubits:

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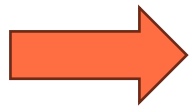


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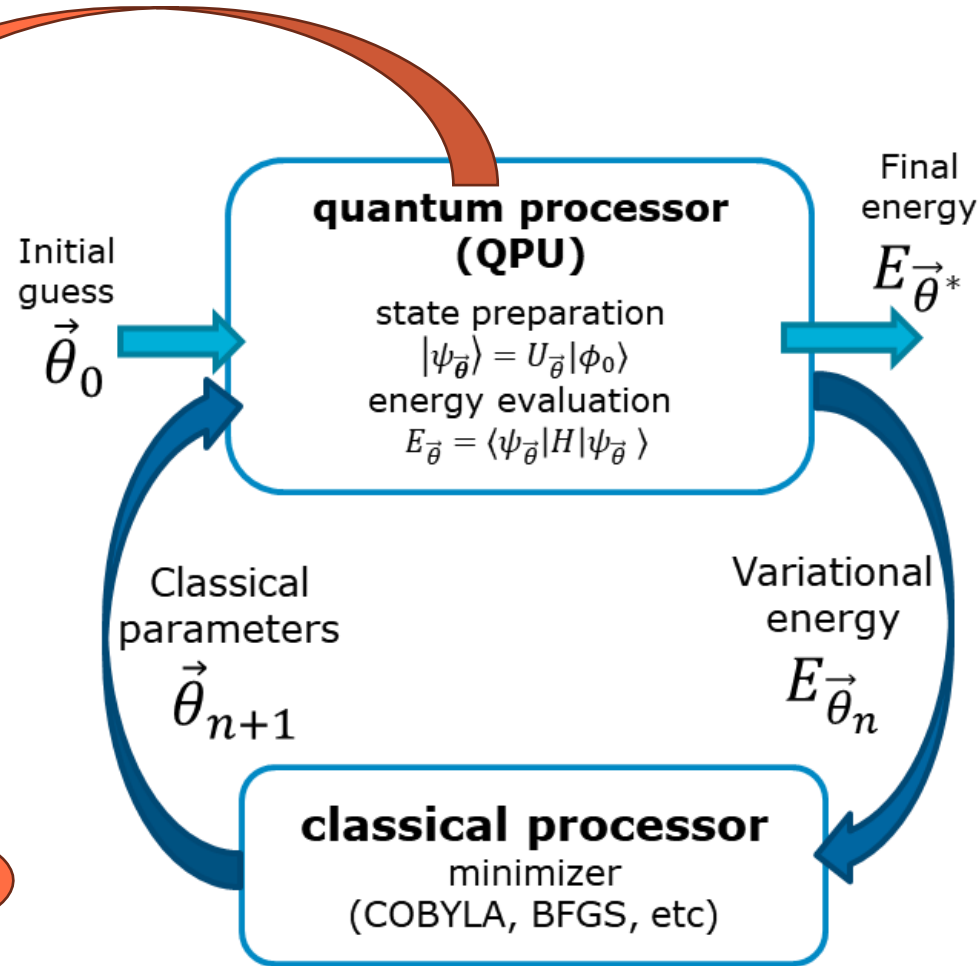
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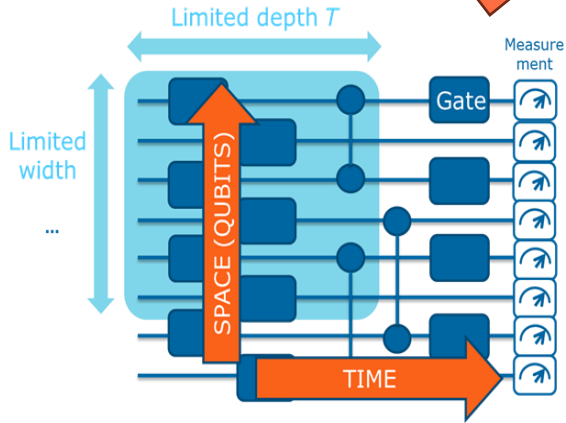
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$c_p^\dagger c_q$ leads to $X_p Z_{p+1} \dots Z_{q-1} X_q$
Hence longer circuits!

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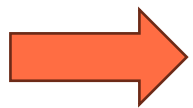


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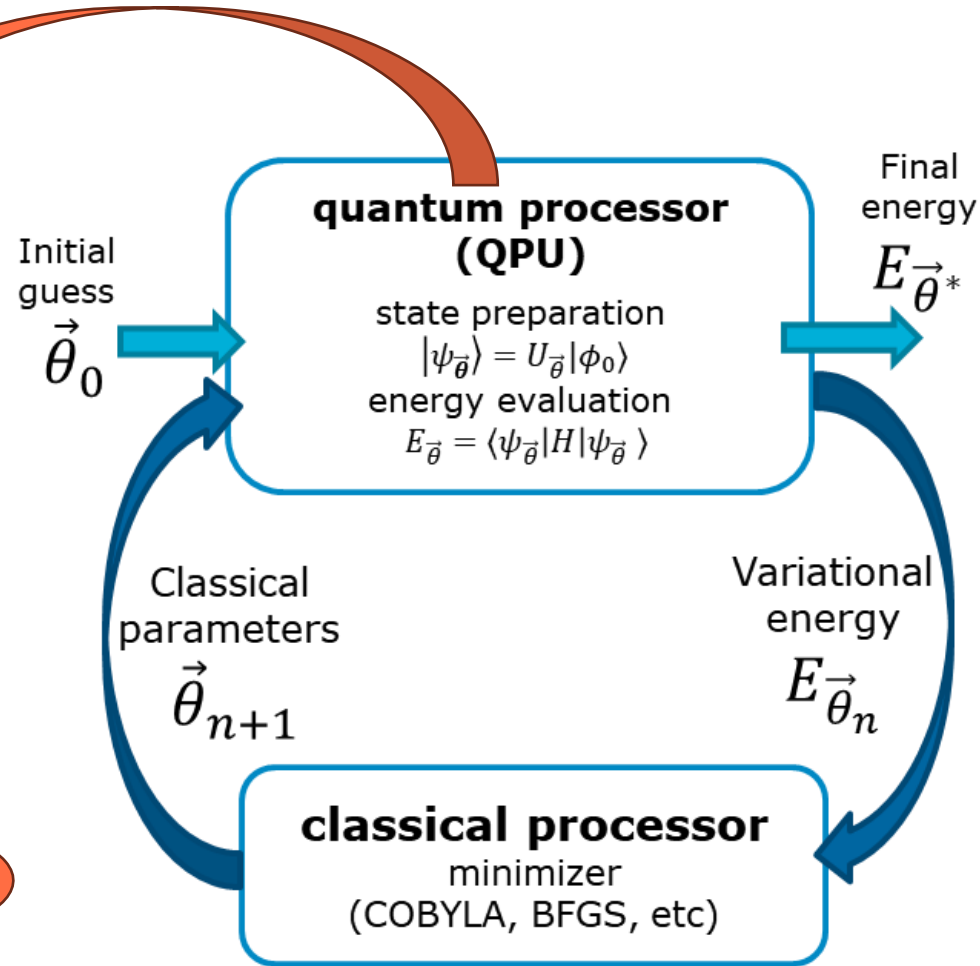
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Can we even avoid fermionic rules?

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Outline



Can we shorten circuits?



Can we even avoid fermionic rules?



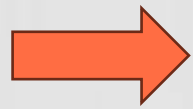
Hybridizing tensor networks and quantum algorithms



Could we use quantum noise to our advantage?

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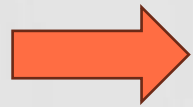
Outline



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Hybridizing tensor networks and quantum algorithms



Could we use quantum noise to our advantage?

The importance of the orbital basis

Consider

$$H = \sum_{pq} h_{pq} c_p^\dagger c_q + \frac{1}{2} \sum_{pqrs} h_{pqrs} c_p^\dagger c_q^\dagger c_r c_s$$

Hartree-Fock method: define

$$\tilde{c}_i^\dagger = \sum_p V_{ip} c_p^\dagger$$

Find orbital transformation V s.t HF wavefunction

$$|\Psi(V)\rangle = \tilde{c}_{i_1}^\dagger \cdots \tilde{c}_{i_{N_e}}^\dagger |00 \dots 0\rangle$$

minimizes $\langle \Psi(V) | H | \Psi(V) \rangle$

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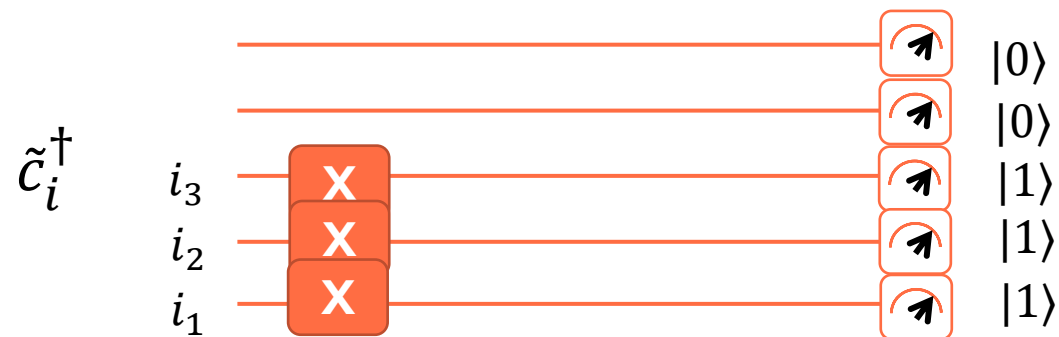
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Quantum computer representation?

In \tilde{c}_i^\dagger (molecular orbital) basis: $|\Psi(V)\rangle = \tilde{c}_{i_1}^\dagger \dots \tilde{c}_{i_{N_e}}^\dagger |00 \dots 0\rangle$



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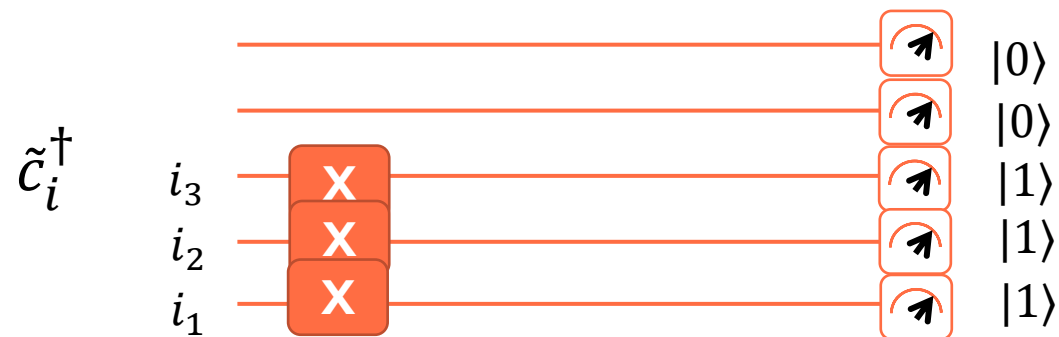
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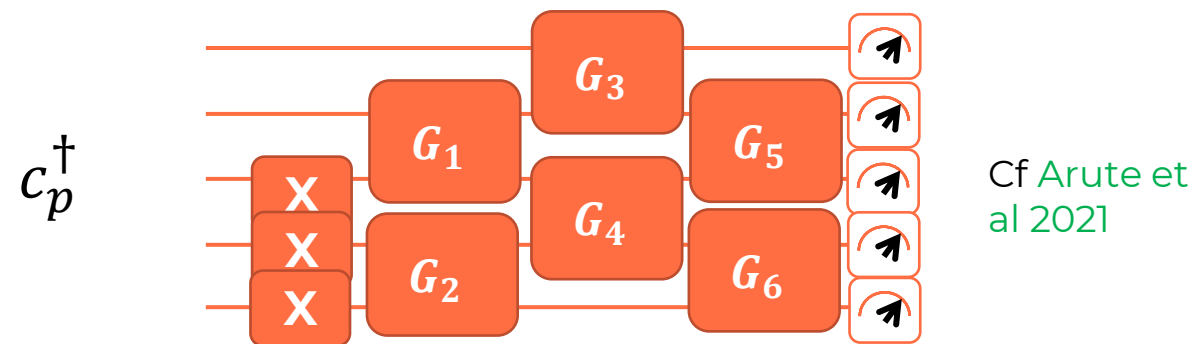
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In e.g original basis... $|\Psi(V)\rangle$ much more complicated!

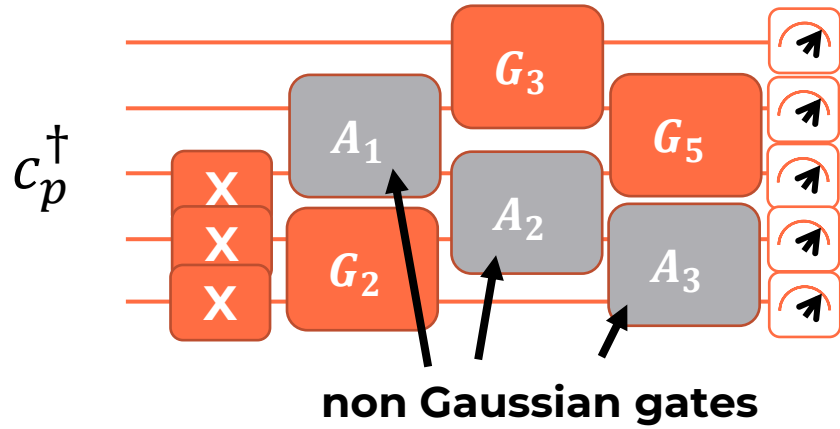


Cf Arute et al 2021

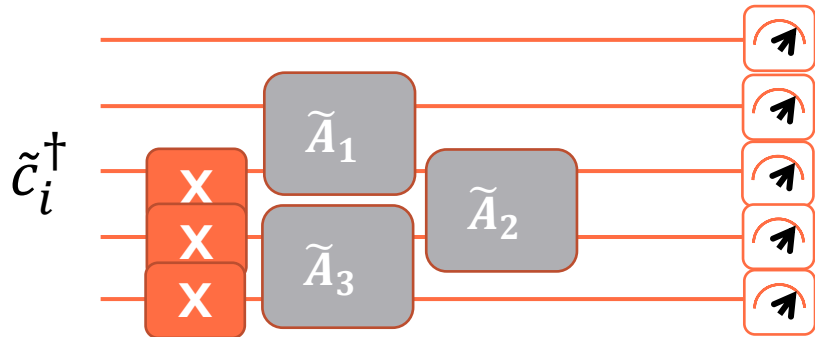
Givens rotations $\sim e^{hc^\dagger c}$... aka **Gaussian gates**

Beyond Hartree-Fock?

In original basis:

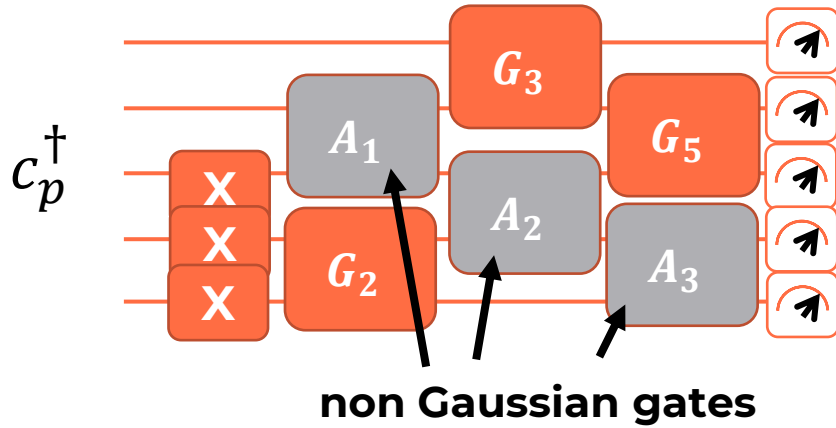


Can we find a (the?) basis that most simplifies the circuit?

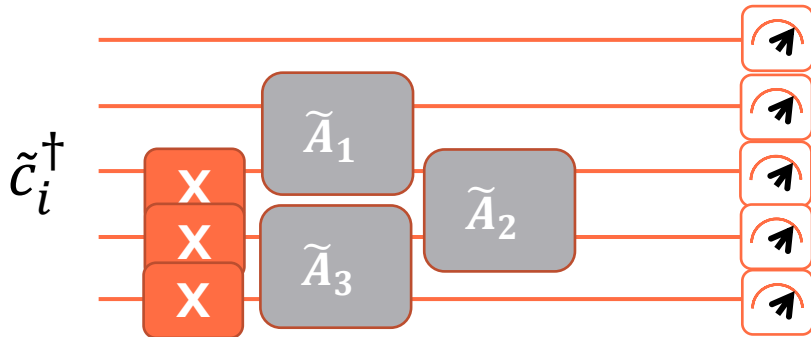


Beyond Hartree-Fock?

In original basis:



Can we find a (the?) basis that most simplifies the circuit?



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The natural orbital basis

**The basis with fewest Slater determinants,
hence shortest circuit!**

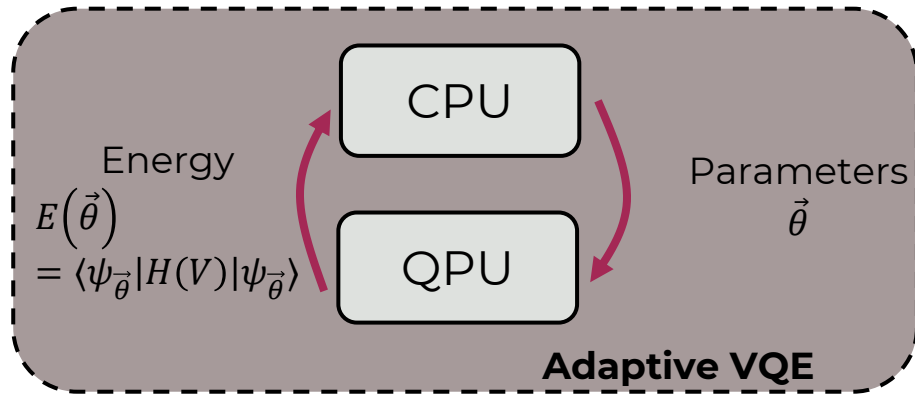
How to compute it ?

Diagonalize

$$D_{pq} = \langle \Psi | c_p^\dagger c_q | \Psi \rangle = V_{pi} n_i V_{iq}^\dagger$$

Iterative rotation to the natural orbital basis

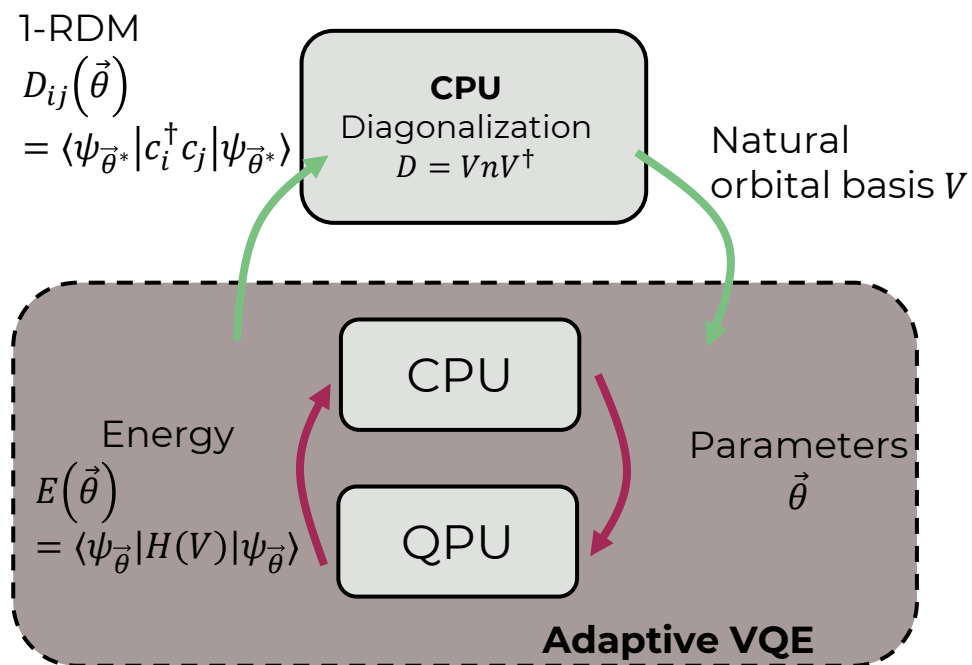
$|\Psi\rangle$ is unknown! Determine RDM iteratively



(Grimsley 2019)

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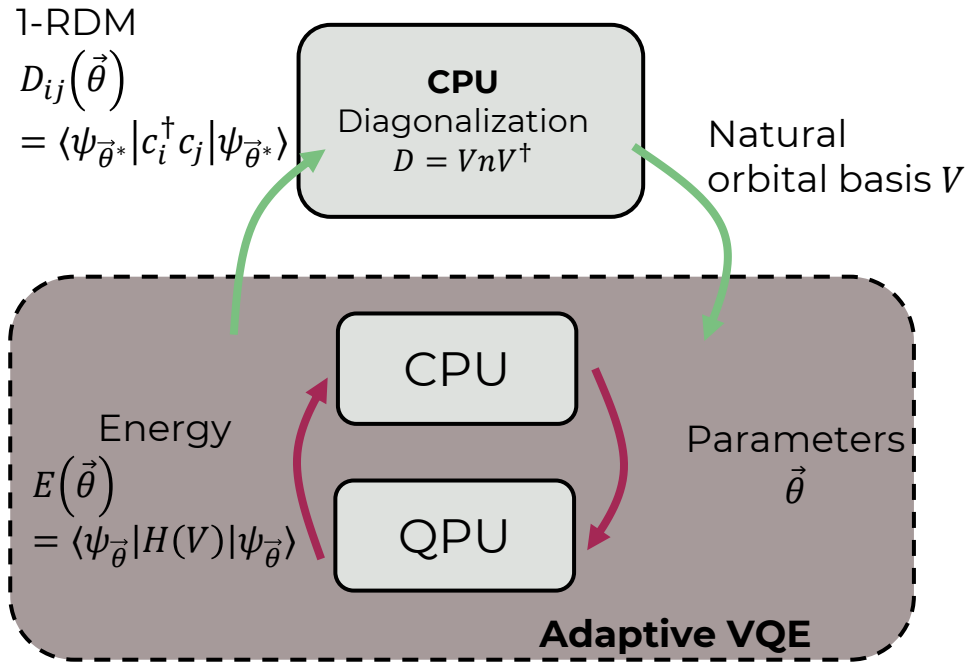
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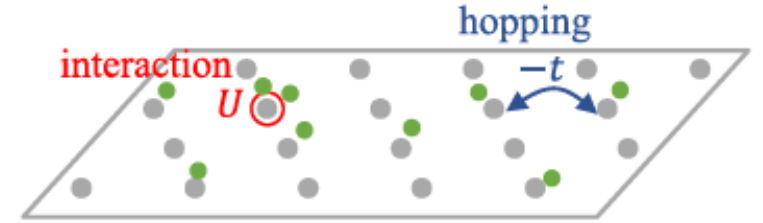
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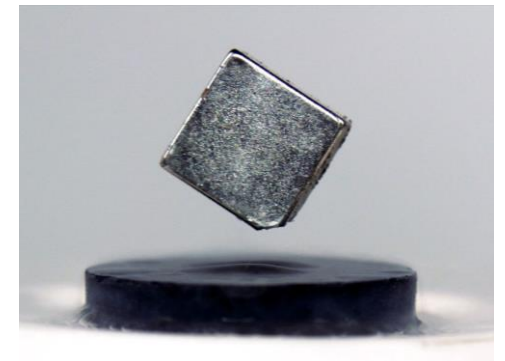
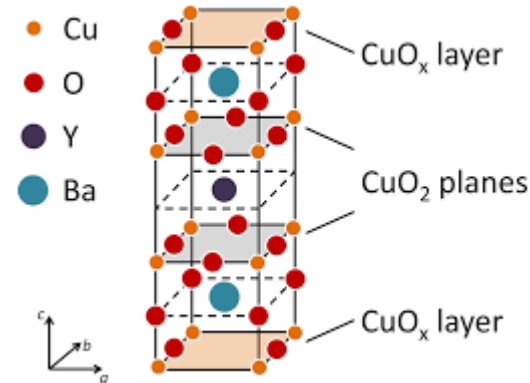


(Grimsley 2019)

Application:
Hubbard model
 (here $N=2$ sites):



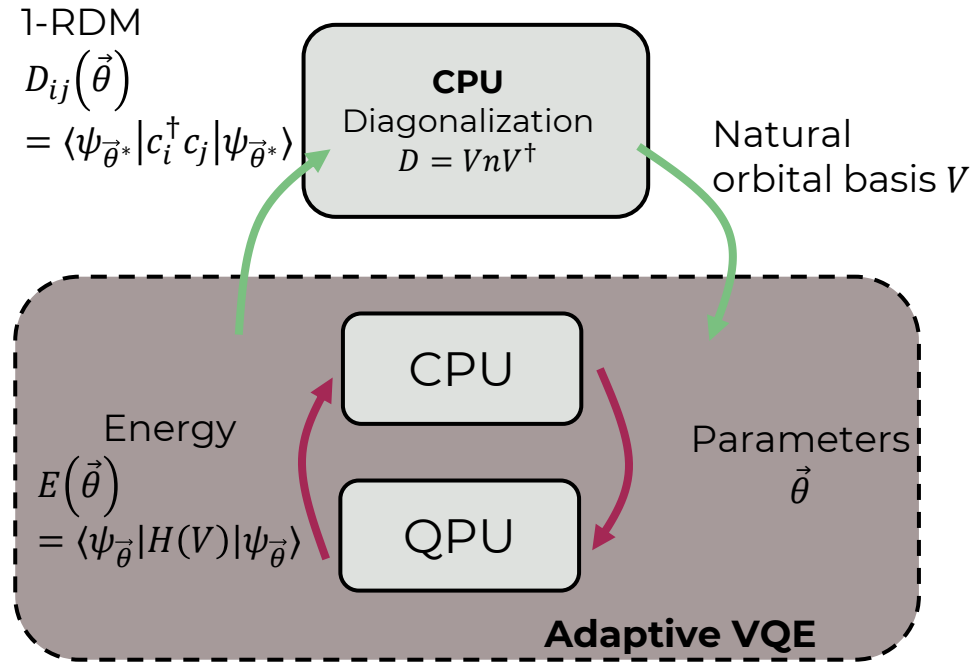
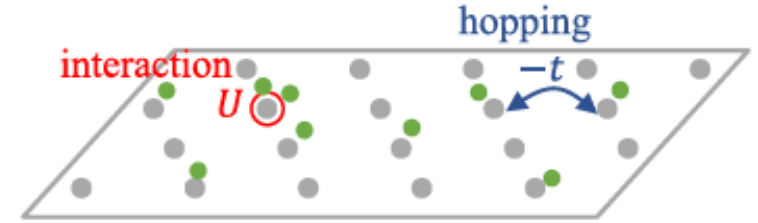
Simplest model for high-temperature superconductors



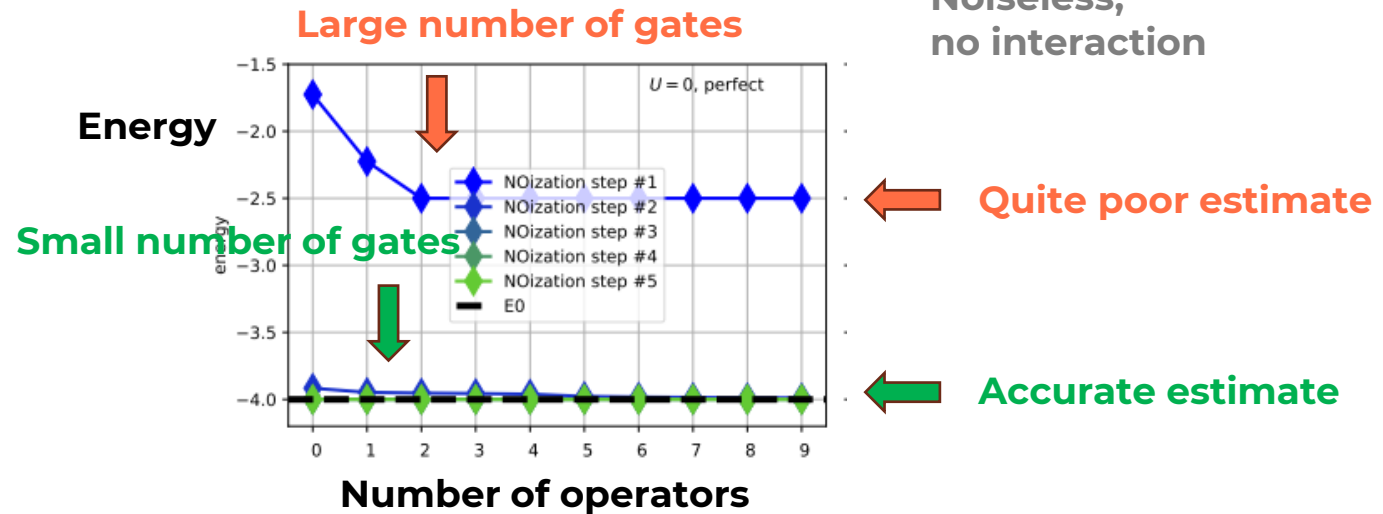
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Conclusions of Part 1

One method to reduce sensitivity to decoherence.

Still many issues with VQE (even without noise!)

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- Measurement problem: $\langle \psi_\theta | H | \psi_\theta \rangle$ known only up to statistical error

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=> Lots of samples (days/months)

(Wecker 2017)

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(Wecker 2017)

- Barren plateau problem (McClean 2018)



Ways out?

- Clever initialization
- Change way of optimizing
- (etc)

Find zeroes instead of minimizing: the projective quantum eigensolver (PQE)

Chemistry: Unitary Coupled Cluster ansatz $U(\vec{\theta})|HF\rangle$

VQE: minimize $\langle HF|U^\dagger(\vec{\theta})HU(\vec{\theta})|HF\rangle$

PQE: find zeros of 'residues': Stair et al '22

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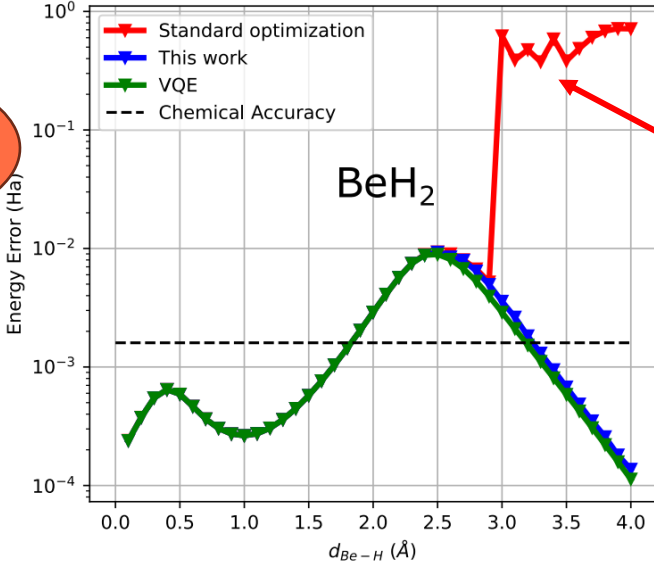
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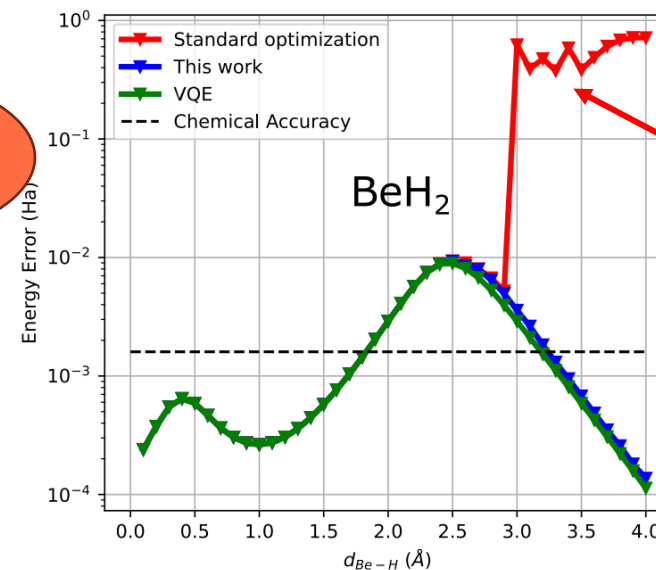
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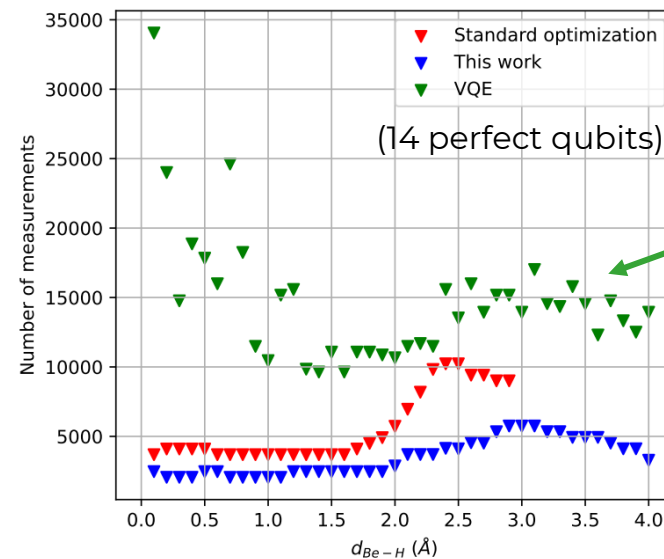
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→ Much fewer measurements than **VQE**.

→ Can it help mitigate barren plateau issue?

EVIDEN

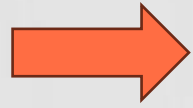
Outline



Can we shorten circuits?



**Can we even avoid fermionic rules?
Hubbard physics with Rydberg processors**



Hybridizing tensor networks and quantum algorithms



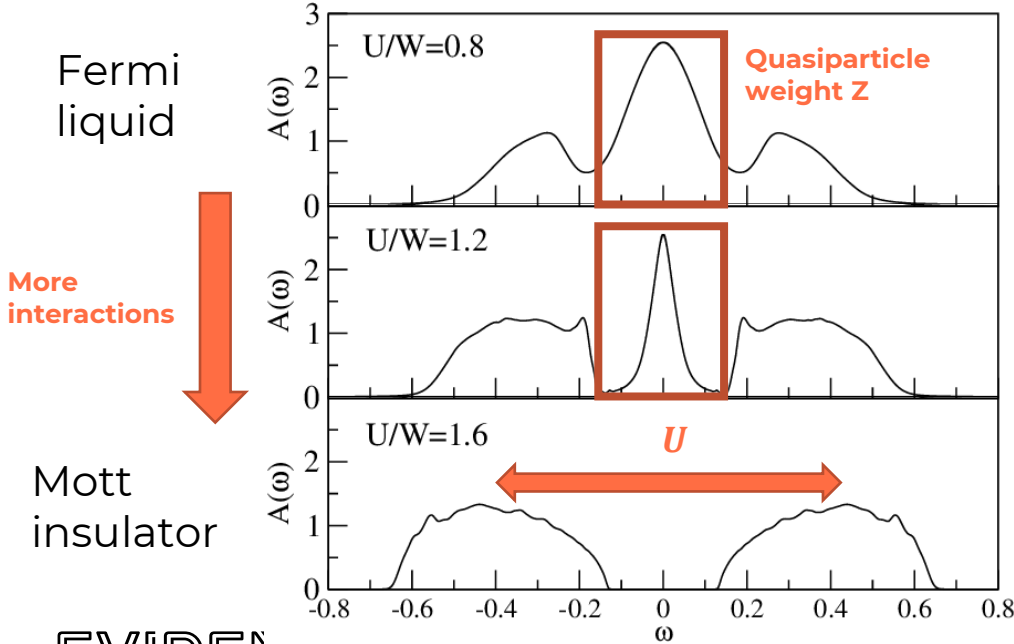
Could we use quantum noise to our advantage?

Mott physics in the Hubbard model

2D Hubbard model



Typical evolution of the spectral function:



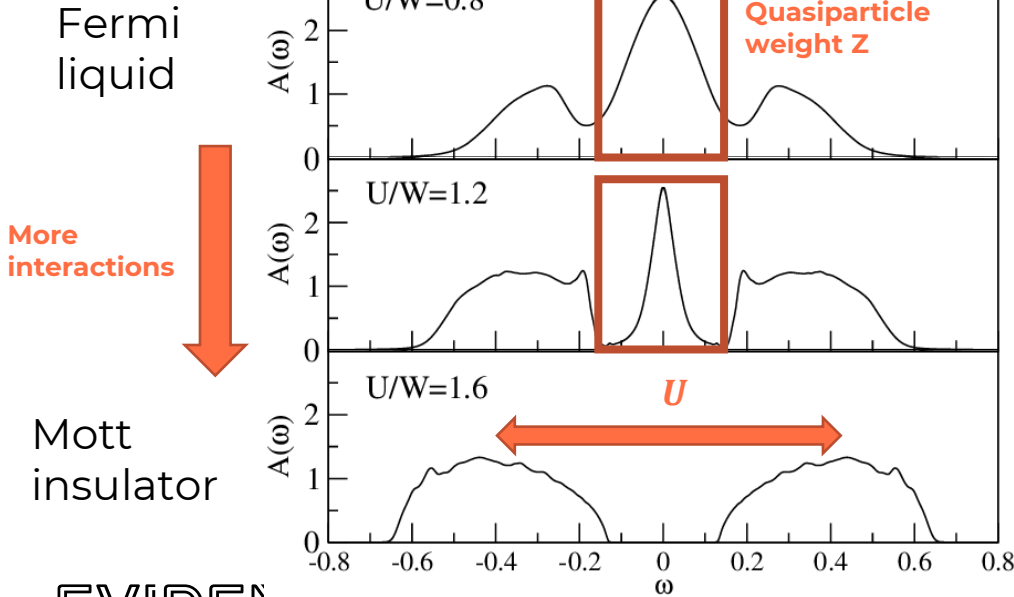
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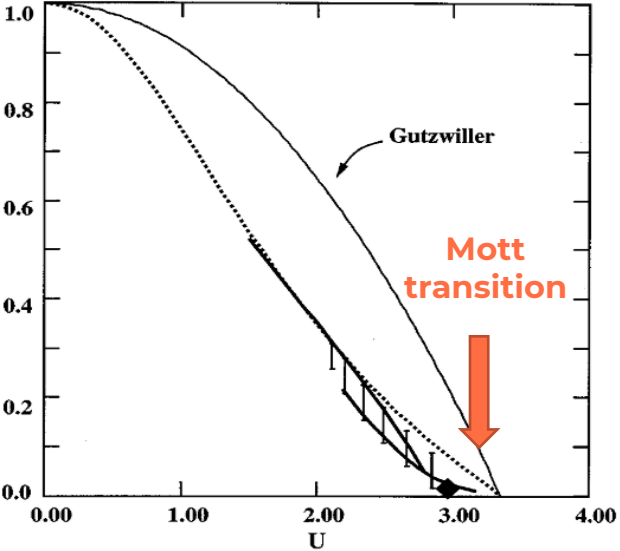


EVIDEN

Equilibrium properties:
Mott transition

Quasiparticle weight Z

DMFT
Georges et al '96



Mott physics on spin-based quantum processors

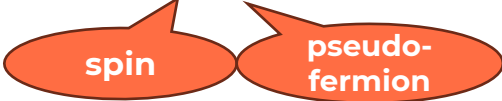
Michel, Henri, Domain, Browaeys, TA, PRB 24

Goal: avoid overhead of fermion-to-qubit translation

$$H = -t \sum_{\langle ij \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

“Slave-spin theory”: decompose

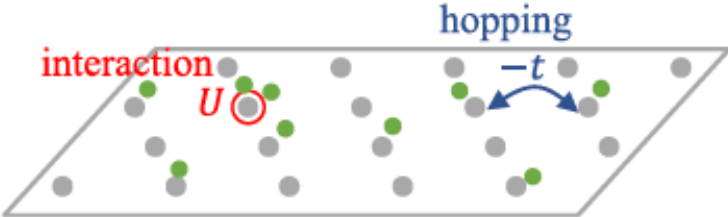
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de' Medici 2005
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Interacting electrons (Hubbard model)



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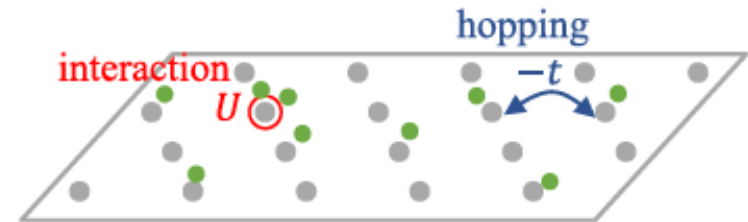
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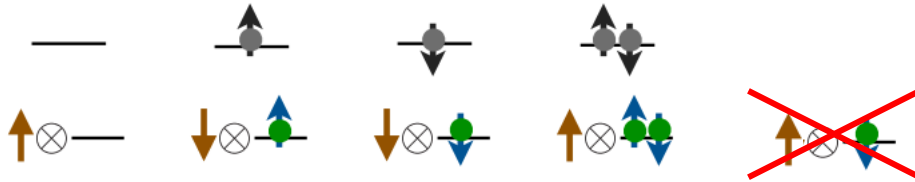
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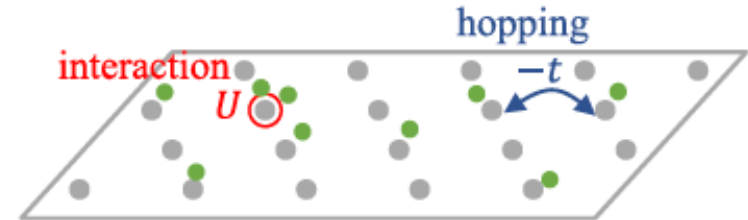


Approximation: Mean-field decoupling:

$$Z_i Z_j f_{i\sigma}^\dagger f_{j\sigma} \approx \langle Z_i Z_j \rangle f_{i\sigma}^\dagger f_{j\sigma} + Z_i Z_j \langle f_{i\sigma}^\dagger f_{j\sigma} \rangle + \text{const.}$$



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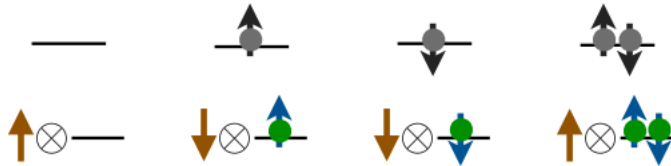
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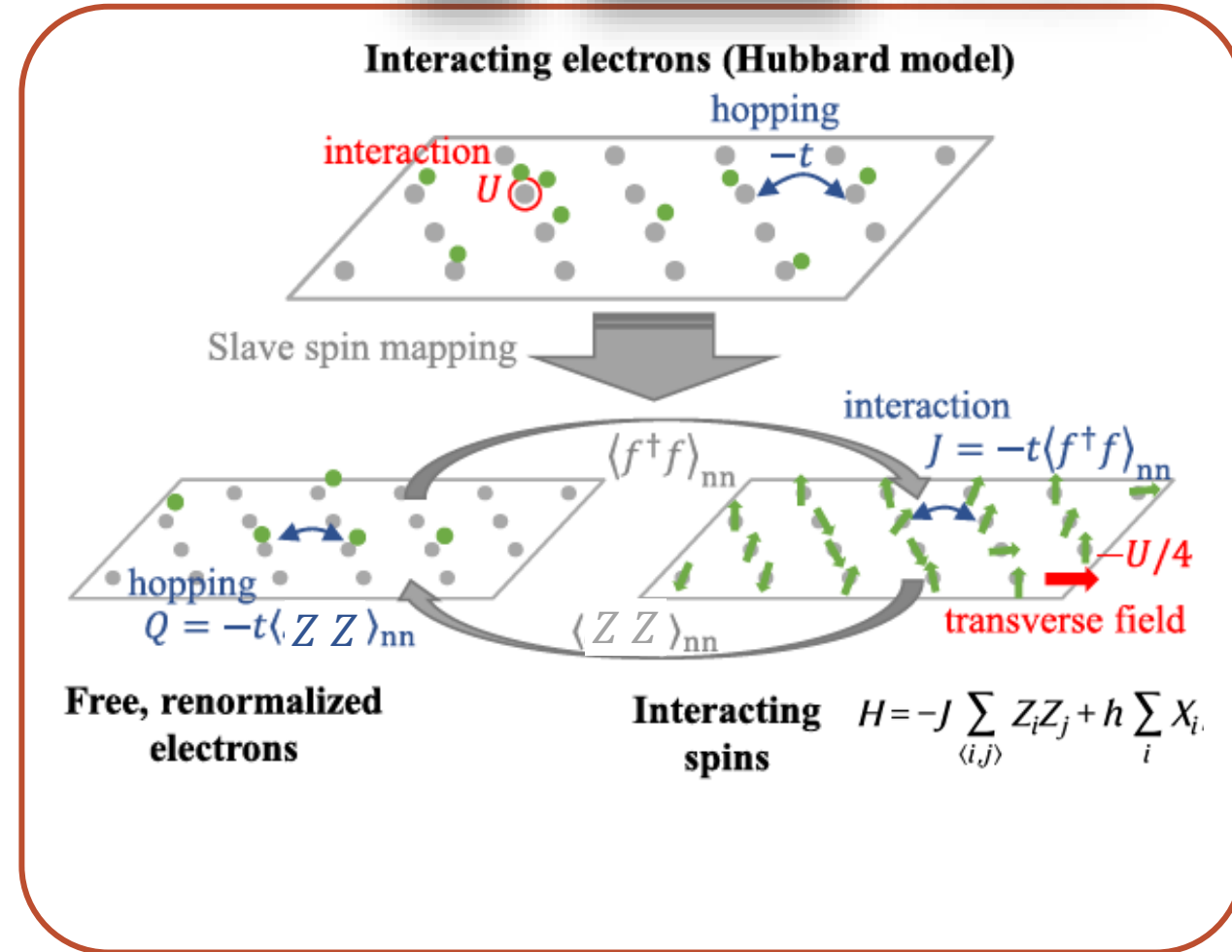
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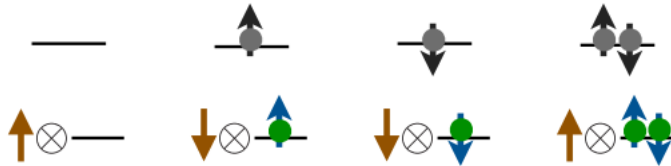
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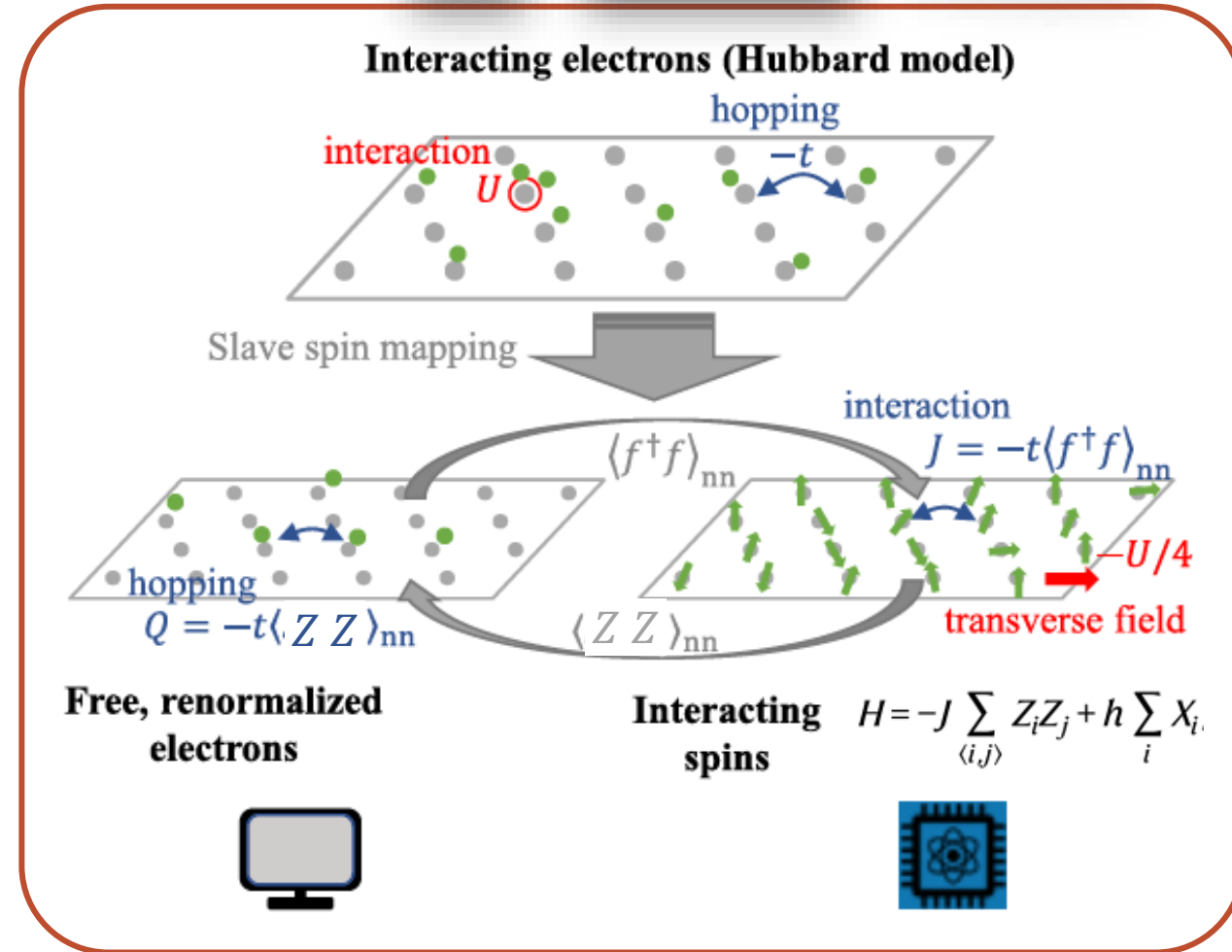
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Using Rydberg atoms to deal with the spin model

Michel, Henriët, Domain, Browaeys, TA,
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Effective model: Transverse Field Ising model (TFIM):

$$H_s^C = \sum_{i,j \in \mathcal{C}} J_{ij} S_i^z S_j^z + \frac{U}{4} \sum_{i \in \mathcal{C}} S_i^x + \sum_{i \in \mathcal{C}} h_i S_i^z,$$

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$$\hat{H}_{\text{Rydberg}} = \sum_{i \neq j} \frac{C_6}{|\mathbf{r}_i - \mathbf{r}_j|^6} \hat{n}_i \hat{n}_j + \frac{\hbar \Omega(\tau)}{2} \sum_i \hat{S}_i^x - \hbar \delta(\tau) \sum_i \hat{n}_i,$$

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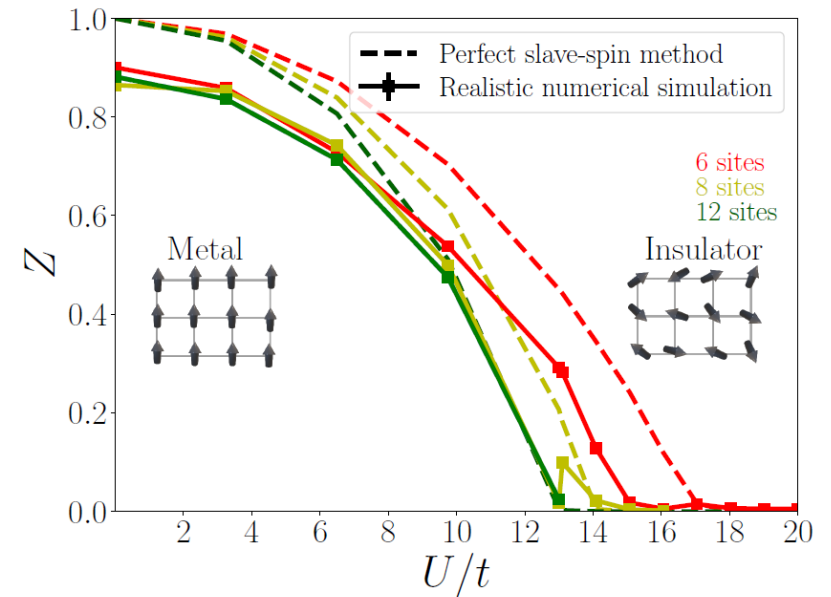
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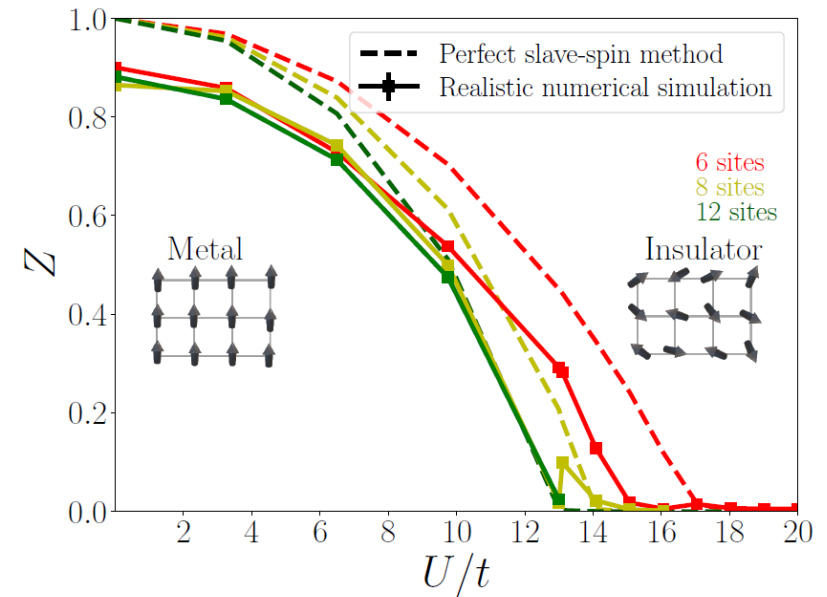
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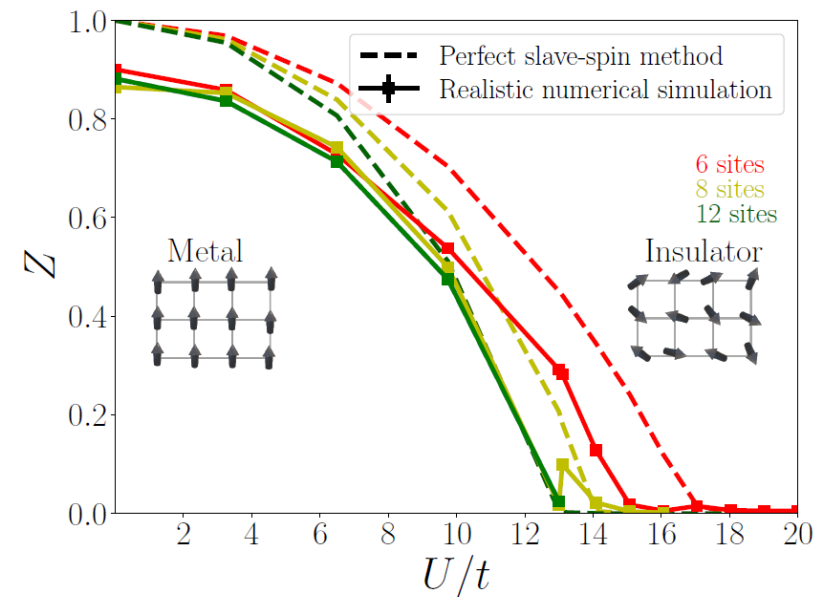
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Ongoing experimental realization @Pasqal!

EVIDEN

Outline



Can we shorten circuits?



Can we even avoid fermionic rules?
Hubbard physics with Rydberg processors



Hybridizing tensor networks and quantum algorithms
Jump-starting quantum computations



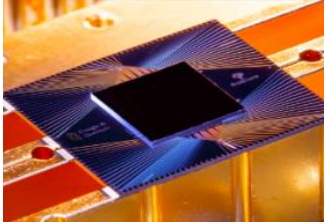
Could we use quantum noise to our advantage?

Google's and IBM's quantum advantage claims

Google supremacy?

(Arute et al '19)

Sycamore, 53 qubits



Sampling from random circuits

200 seconds! (and $F = 0.2\%$!)

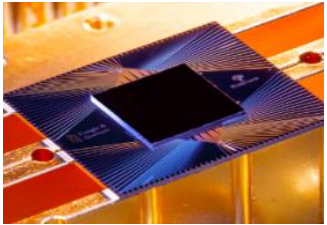
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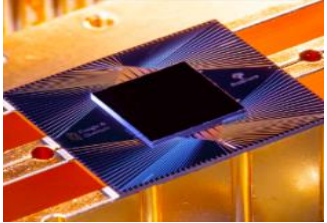
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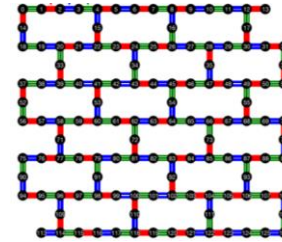
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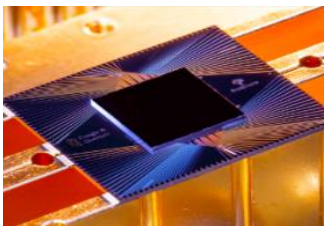
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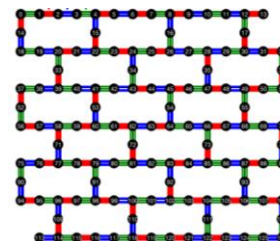
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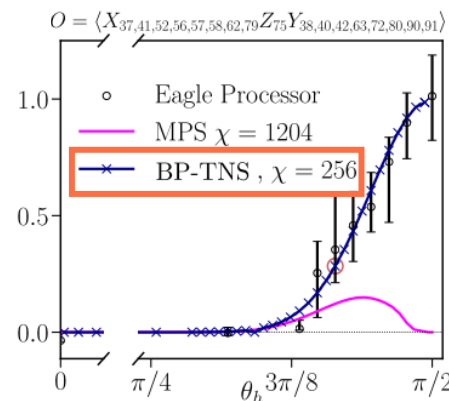
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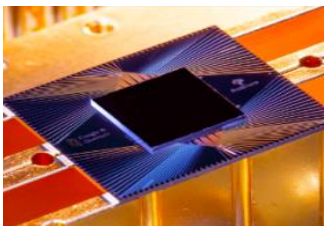
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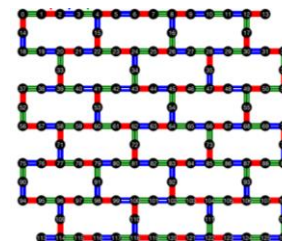
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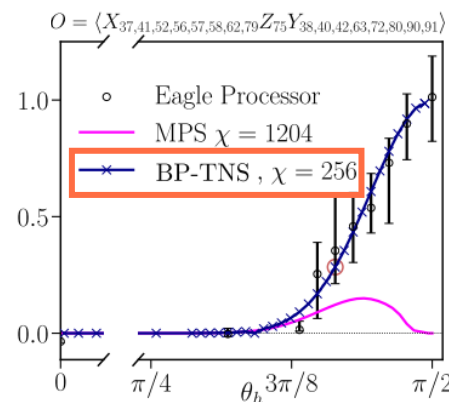
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Method to beat the exponential wall?

Basics of tensor networks (matrix product states)

Generic wavefunction:

$$|\Psi\rangle = \sum_{b_1 b_2 \dots b_n} \psi_{b_1 b_2 \dots b_n} |b_1, \dots, b_n\rangle$$

Representation:

$$\psi_{b_1 b_2 b_3} = \text{[Diagram: An orange horizontal bar with three vertical blue lines extending upwards from its top edge, representing a tensor with three indices.]}$$

Storage cost

$$2^n$$

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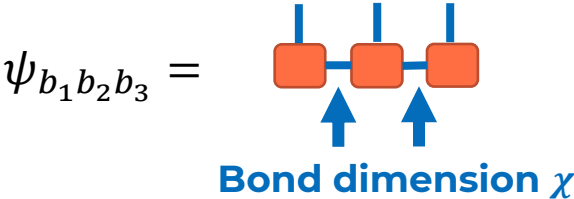
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$2n$

If some entanglement: $\psi_{b_1 b_2 b_3} = \text{Tr}(A_{b_1} B_{b_2} C_{b_3})$



$2n\chi^2$

Basics of tensor networks (matrix product states)

Generic wavefunction:

$$|\Psi\rangle = \sum_{b_1 b_2 \dots b_n} \psi_{b_1 b_2 \dots b_n} |b_1, \dots, b_n\rangle$$

Storage cost

Representation:

$$\psi_{b_1 b_2 b_3} = \text{[Diagram: A single orange horizontal bar with three vertical blue lines extending upwards from its top edge, representing a full tensor with three indices.]}$$

$$2^n$$

If no entanglement, $\psi_{b_1 b_2 \dots b_n} = \psi_{b_1} \phi_{b_2} \varphi_{b_3}$

$$\psi_{b_1 b_2 b_3} = \text{[Diagram: Three separate orange squares, each with a vertical blue line extending upwards from its top edge, representing three independent tensors.]}$$

$$2n$$

If some entanglement: $\psi_{b_1 b_2 b_3} = \text{Tr}(A_{b_1} B_{b_2} C_{b_3})$

$$\psi_{b_1 b_2 b_3} = \text{[Diagram: Three orange squares connected by horizontal blue lines between their right and left sides. Two blue arrows point upwards from the bottom of the first and second squares. Below the diagram is the text 'Bond dimension \chi'.]}$$

$$2n\chi^2$$

No free lunch: if entanglement S , **need**

$$\chi \gtrsim 2^S$$

1 exponential wall + 1 exponential wall < 2 exponential walls?

Tensor network (TN) showstopper:

$$\text{Need } \chi \gtrsim 2^S$$

with S : entanglement entropy

1 exponential wall + 1 exponential wall < 2 exponential walls?

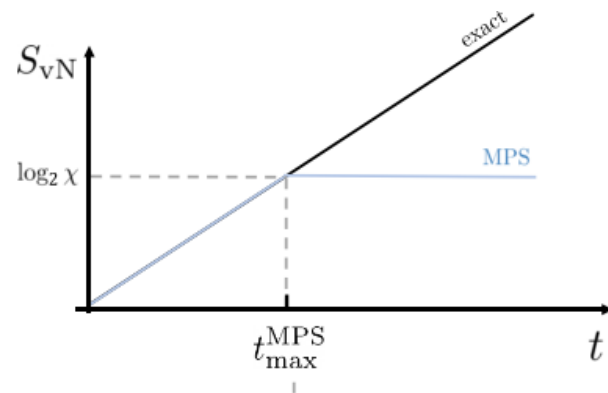
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$$H = -J \sum_{\langle ij \rangle} Z_i Z_j + h \sum_i X_i$$



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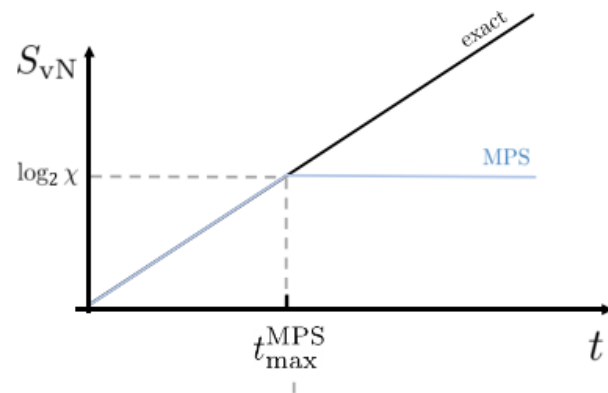
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Classical cost $\propto e^{at}$!

Quantum computation (QC) showstopper:

$$\text{Fidelity reduction } F \propto e^{-pN_g}$$

Large N_g for accurate Suzuki-Trotter time evolution:

$$e^{-iHt} = \prod_k^{N_t} \prod_{\langle ij \rangle} R_{ZZ}(ij) \prod_i R_X(i) + O\left(\frac{t}{N_t}\right)^2$$

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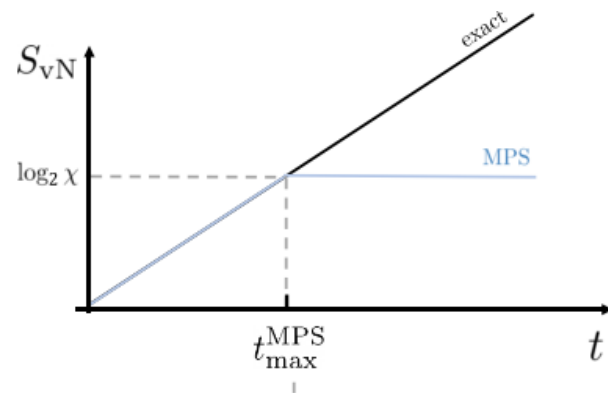
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Two key ideas:

⇒ Push TN computation to its limit and take over with QC

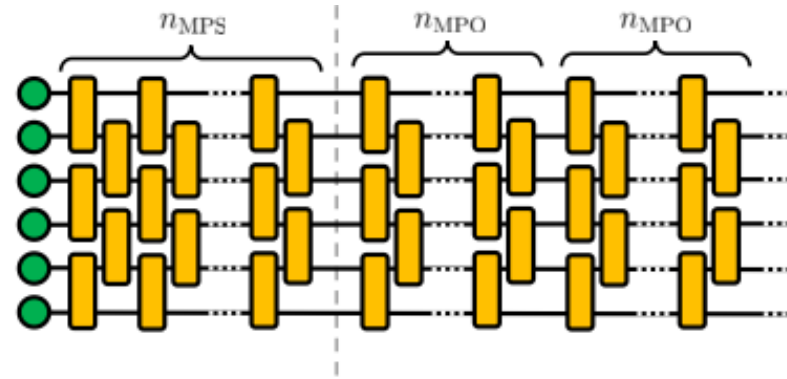
⇒ Use TN techniques to compress quantum circuits

Hybridizing tensor networks and quantum computation

Anselme-Martin, TA et al, PRA 24

See also Causer et al '23

**Formal target: fine-grained
Suzuki-Trotter time evolution:**



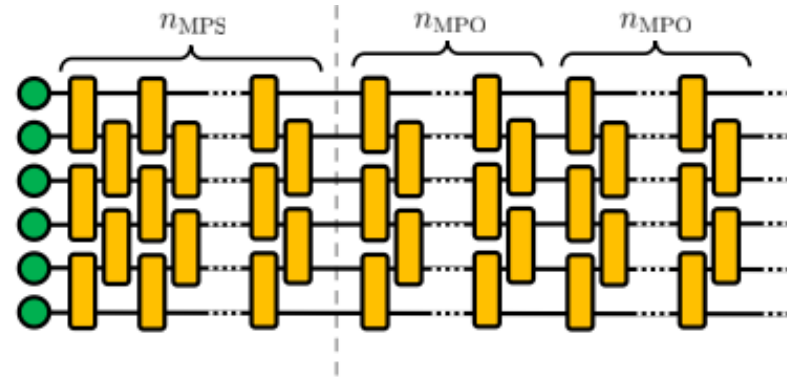
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Too many steps for QC (limited coherence)

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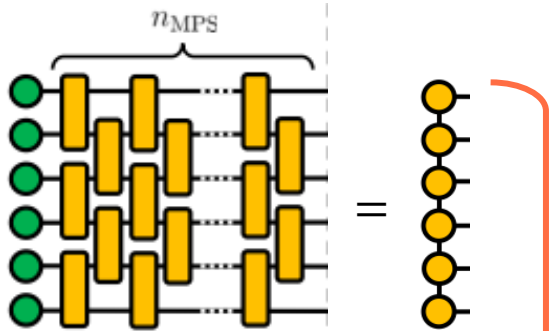
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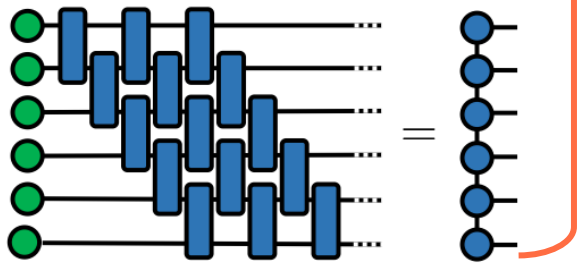


Too many steps for TEBD (limited RAM)
Too many steps for QC (limited coherence)

(classical) TEBD computation:



QMPS circuit ansatz:



Depth N_L^{MPS}

$$\chi_{MPS} = 2^{N_L^{MPS}}$$

maximize
overlap
to find

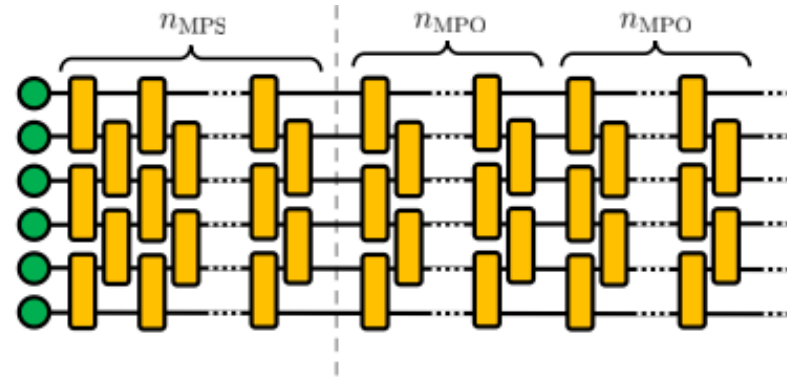


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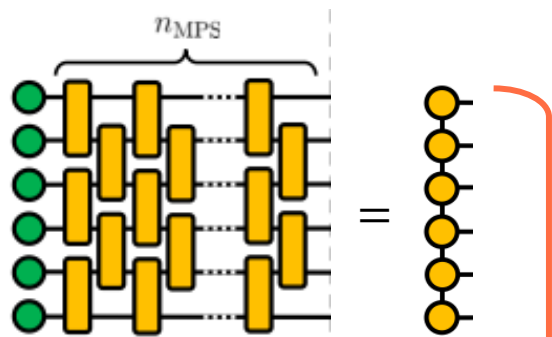
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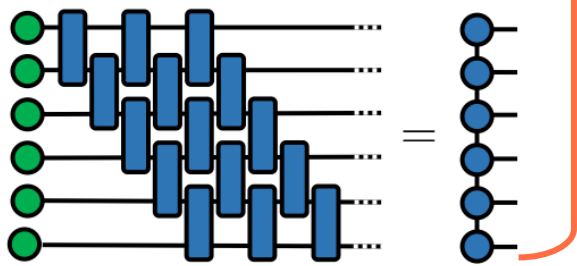


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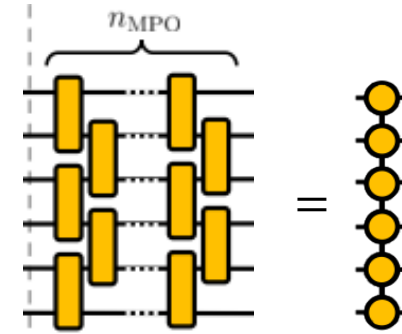
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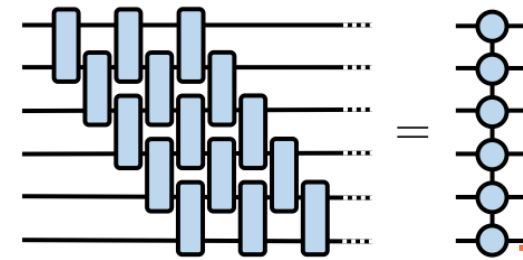
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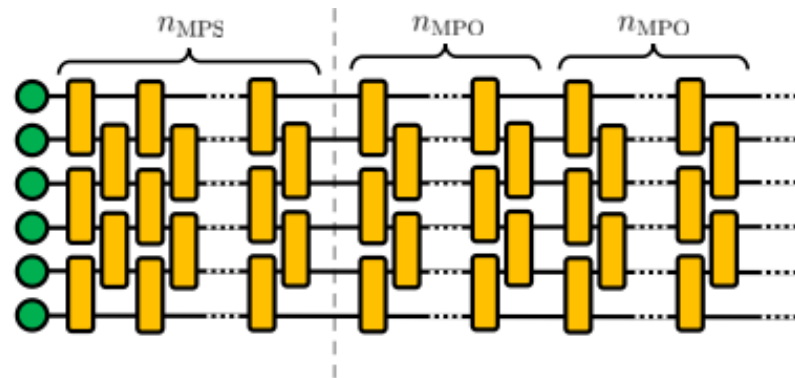


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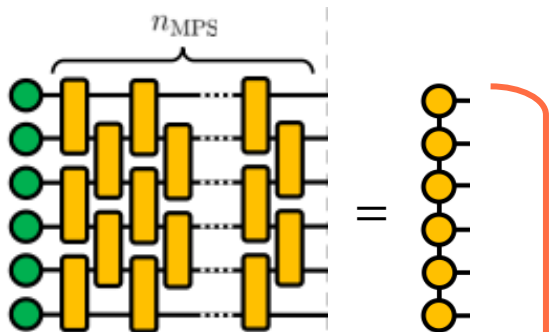
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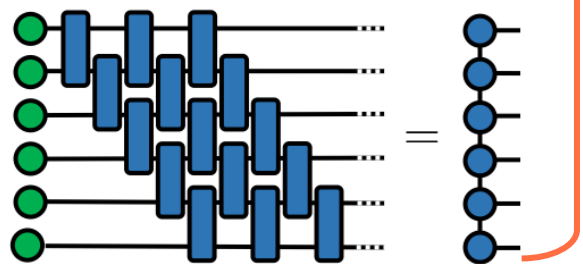


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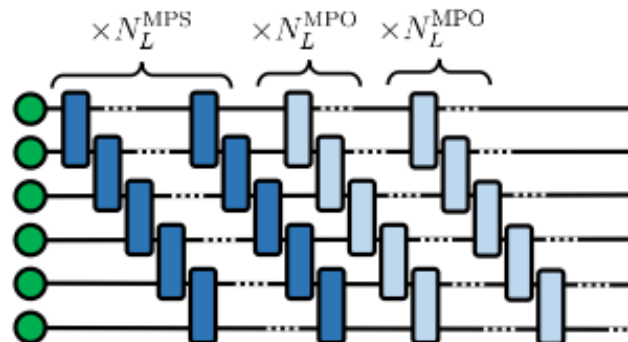
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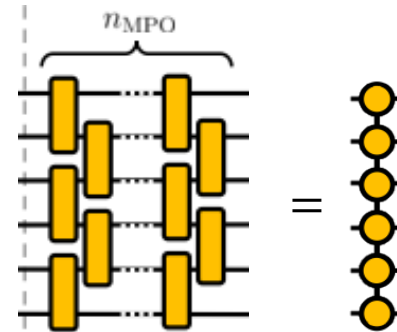
maximize overlap to find



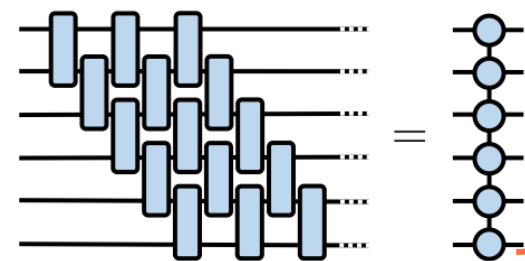
Run circuit:



(classical) TEBD computation:



QMPO circuit ansatz:



maximize overlap to find

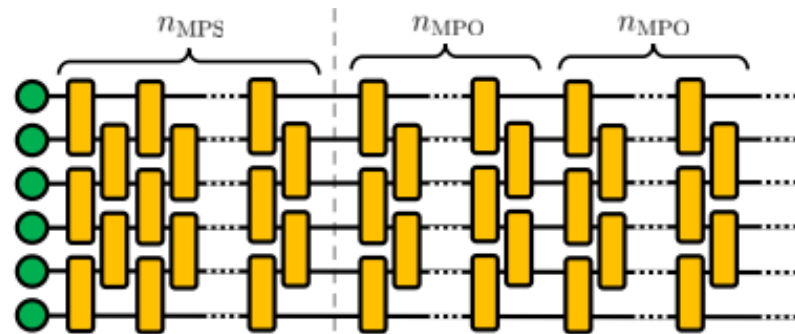


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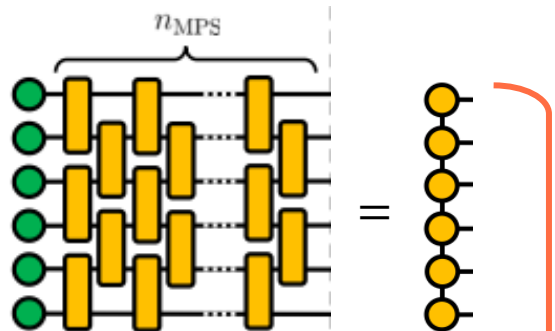
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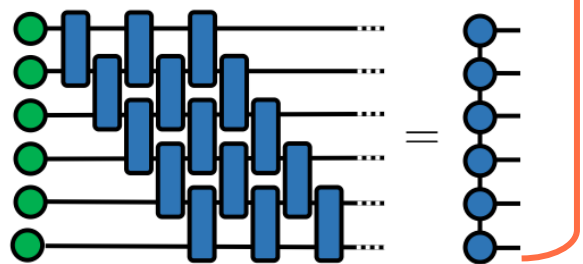


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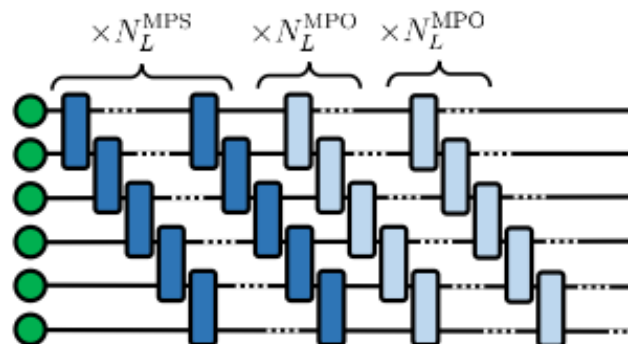
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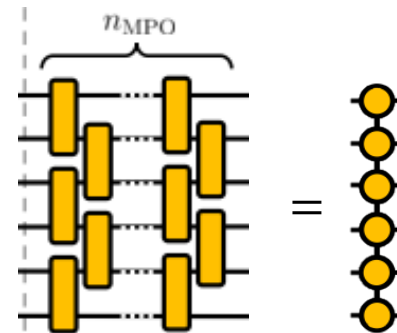
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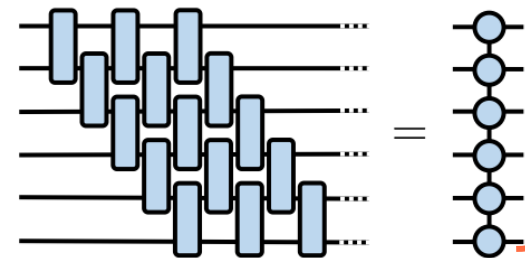
Run circuit:



(classical) TEBD computation:



QMPO circuit ansatz:



maximize overlap to find



What did we gain?

$$N_L^{MPS} \ll n_{MPS}$$

$$N_L^{MPO} \ll n_{MPO}$$

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Experimental proof of concept on IBM quantum computers

Look at magnetization for quenched Ising

$$H = -J \sum_{\langle i,j \rangle} Z_i Z_j + h \sum_i X_i,$$

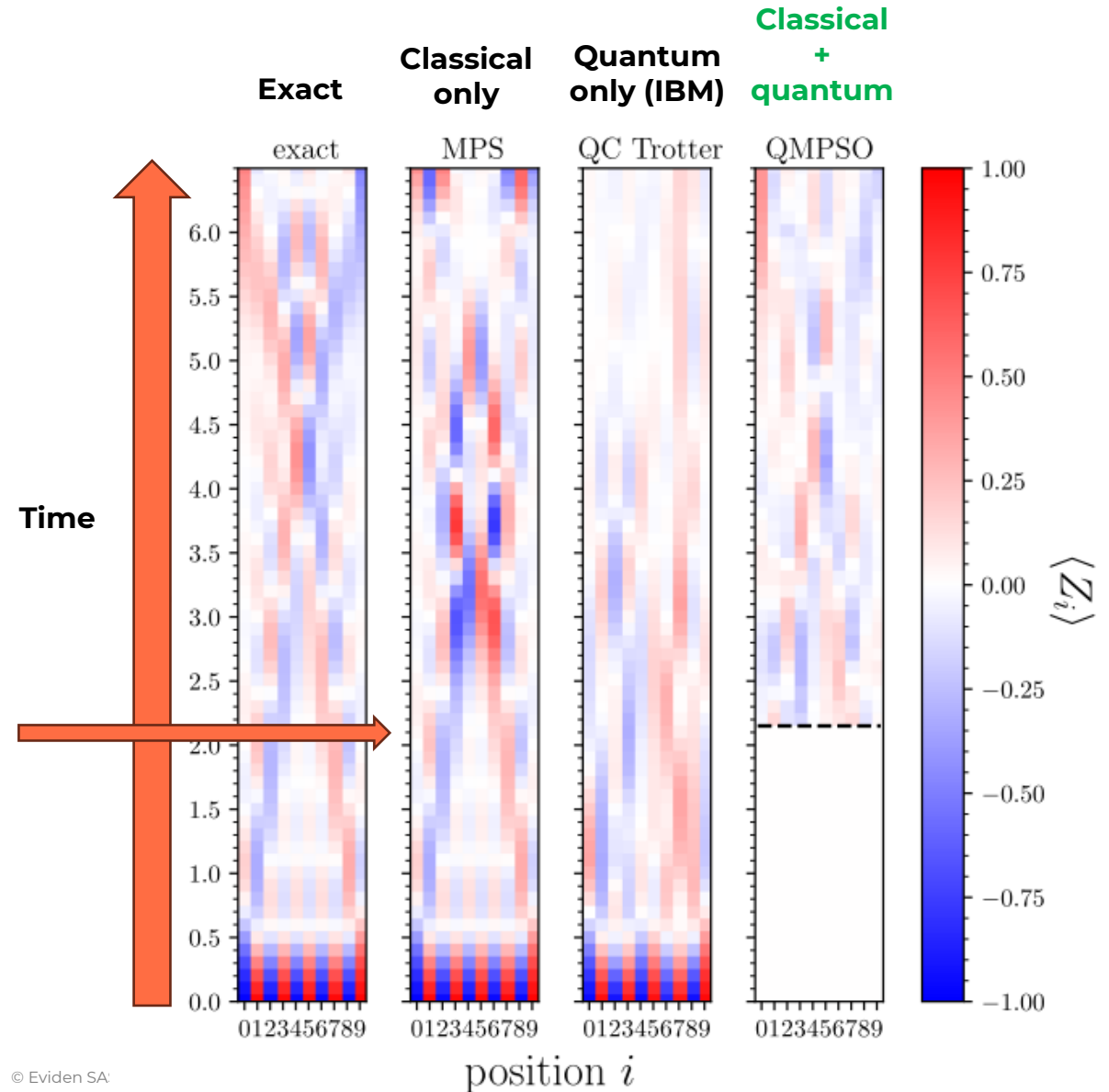
- 10 spins/qubits (toy model)
- Assume fixed RAM, hence max bond dim
⇒ max time to keep MPS 'exact'

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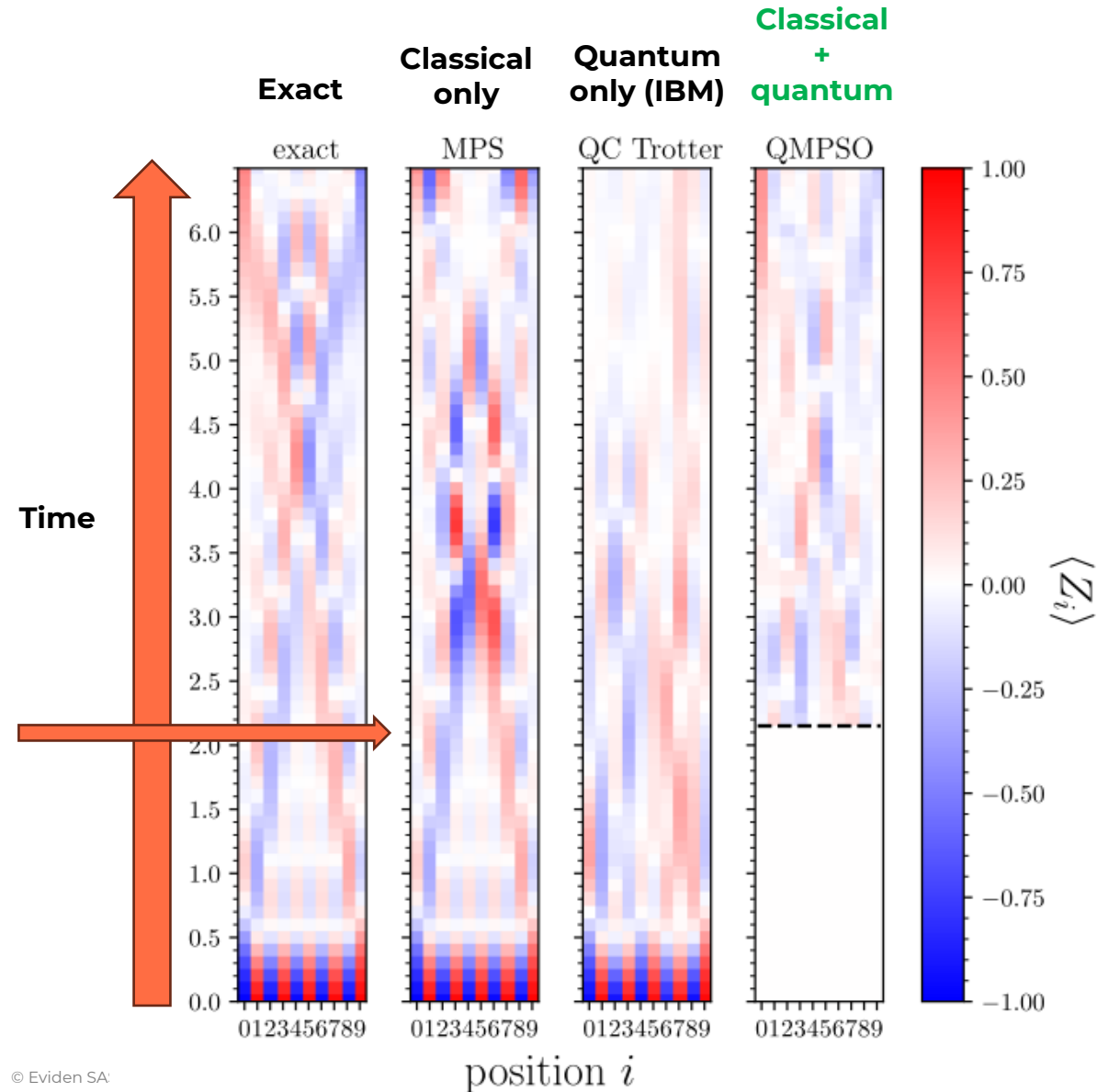
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- 10 spins/qubits (toy model)
- Assume fixed RAM, hence max bond dim \Rightarrow max time to keep MPS 'exact'
- Hybrid approach outperforms both others

Only proof of concept!

- **Artificially small RAM budget:** realistic budget would make it hard for QC to compete
- True challenge for TN: **2D (but same ideas apply)**

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Conclusions of Part 3

Double role of tensor networks:

- Often the most advanced classical algorithm:
a yardstick for quantum advantage
(deflate quantum advantage claims)

- Can jump-start a quantum computation!
(Here, limited to 1D TN... true challenge: 2D)

Conclusions of Part 3

Double role of tensor networks:

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- Can jump-start a quantum computation!
(Here, limited to 1D TN... true challenge: 2D)

Not mentioned here... **a third role:**

- Tensor networks are also powerful tools to **emulate execution of quantum circuits!**
- Help interpret results of QCs with 100-1000 noisy qubits!

Key advantage: decoherence reduces entanglement $S...$ and recall: $\chi \approx 2^S$

⇒ Noisy QCs are easier for TNs!

⇒ **Eviden develops QC emulators with 100s qubits!**

See Müller, TA, Bertrand, 2403.00152

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Outline



Can we shorten circuits?



Can we even avoid fermionic rules?
Hubbard physics with Rydberg processors



Hybridizing tensor networks and quantum algorithms
Jump-starting quantum computations

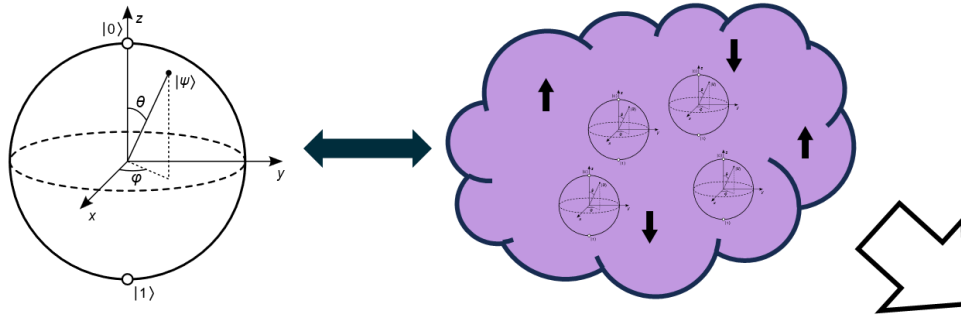


Could we use quantum noise to our advantage?

Can we use qubit noise to simulate a thermodynamical bath?

Bertrand, Besserve, Ferrero, TA, in preparation

Noisy quantum computer

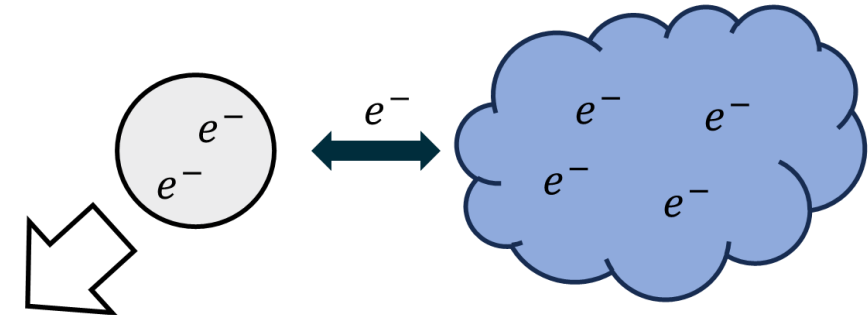


Dissipative processes:

- Amplitude damping $\rightarrow S^- = |0\rangle\langle 1|$
- Dephasing $\rightarrow Z$

formally the same

Many-body system + thermodynamic bath



Dissipative processes:

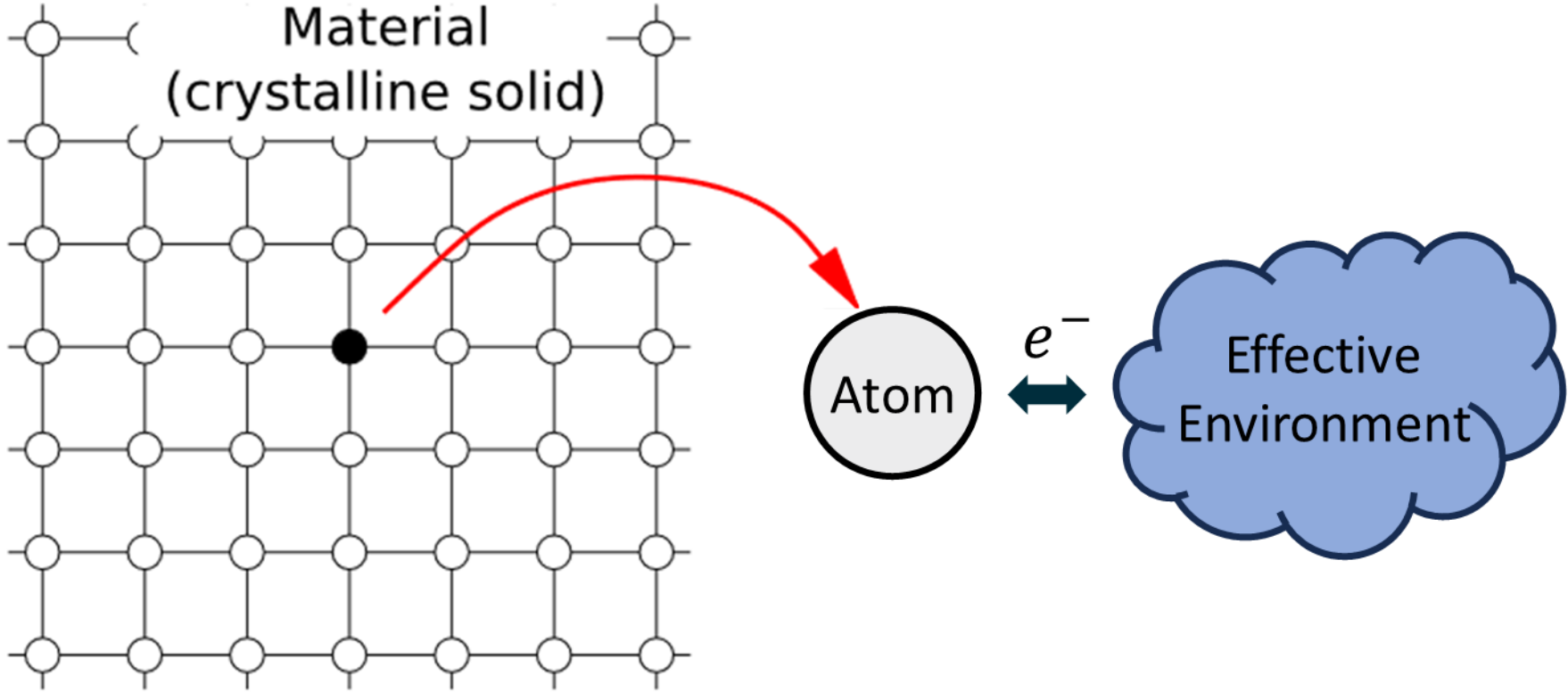
- Creation of particle $\rightarrow c^\dagger$
- Annihilation of particle $\rightarrow c$

Dynamical mean field theory, an ideal playground

From a lattice problem to an atomic problem coupled to a bath

Bertrand, Besserve, Ferrero, TA, in preparation

e.g Hubbard model



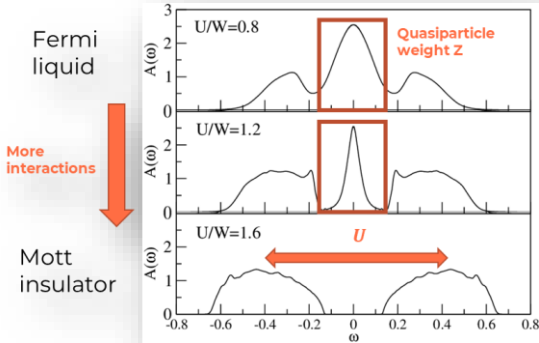
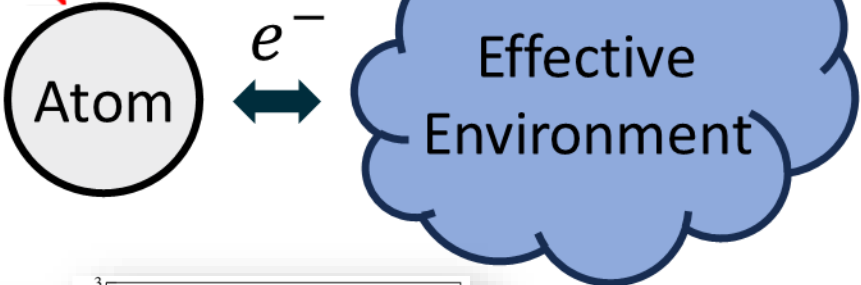
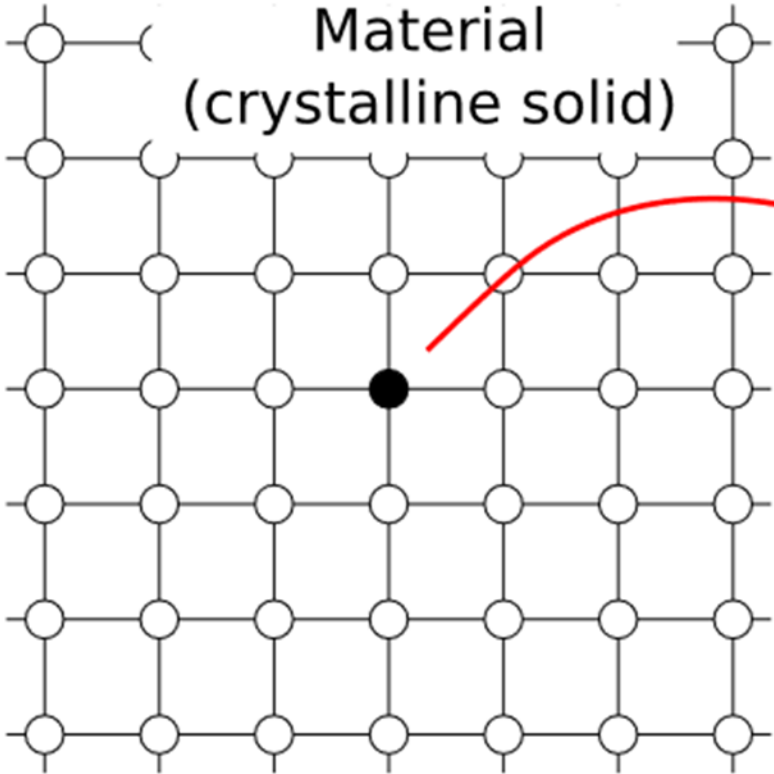
Georges et al '96

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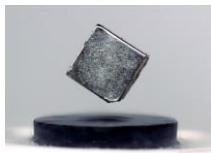
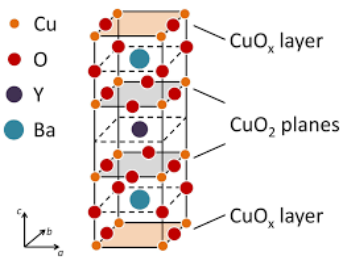


© Eviden SAS

Slide courtesy of Corentin Bertrand

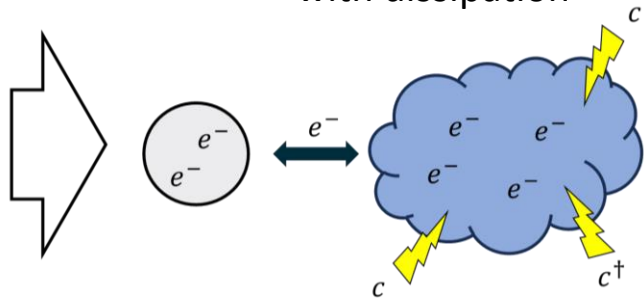
A workflow to leverage noisy qubits

Strongly correlated material



Arrigoni '13
Dorda '14 '15 '17
Schwarz '17

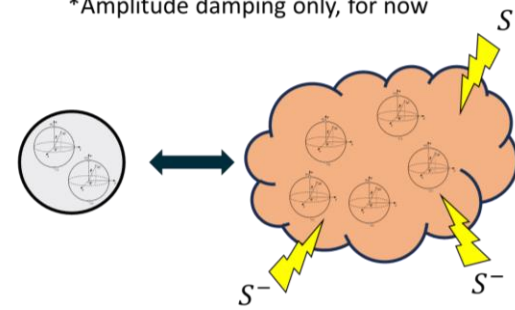
Fermionic impurity model
with dissipation



This work

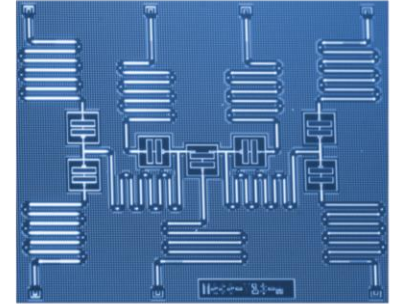
Qubit model with noise*

*Amplitude damping only, for now



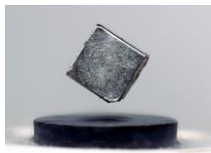
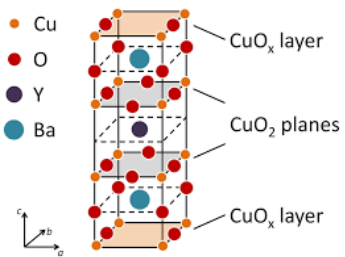
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Simulate on noisy QC



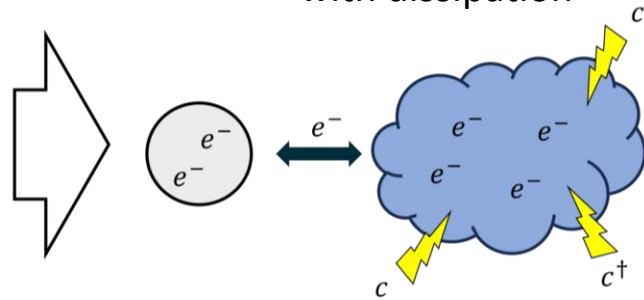
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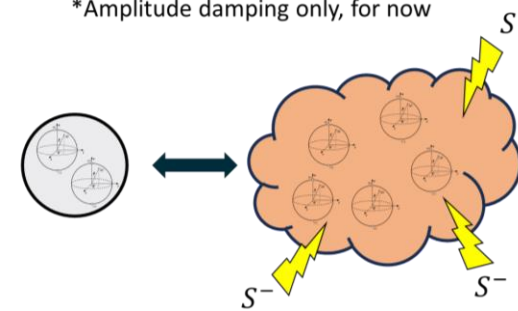
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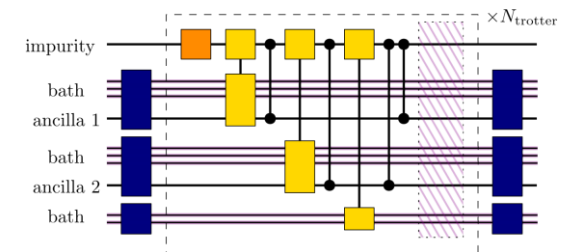
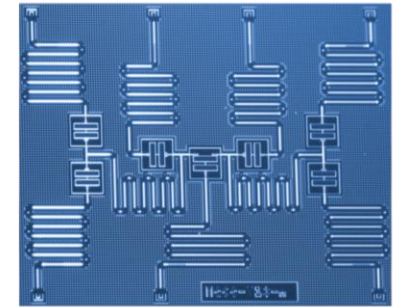
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What is the advantage of noise?

Coupling to a dissipative bath

- Alleviates **finite-size effects** (dissipation stems from large systems):

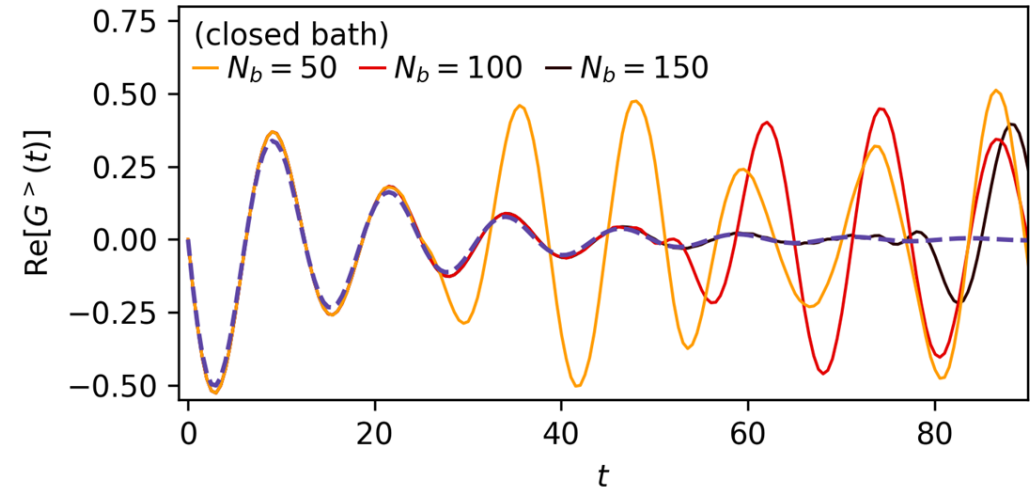
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Green's function computation:

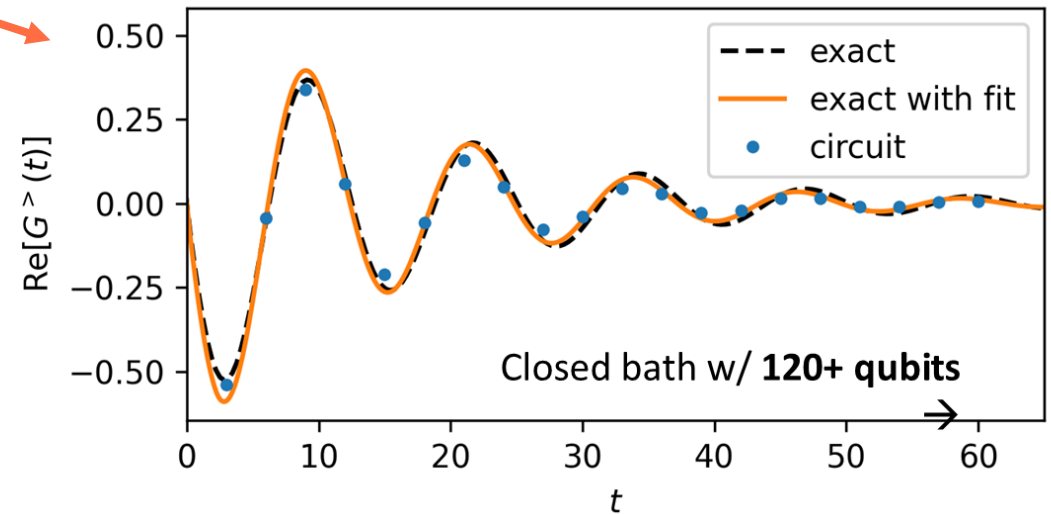
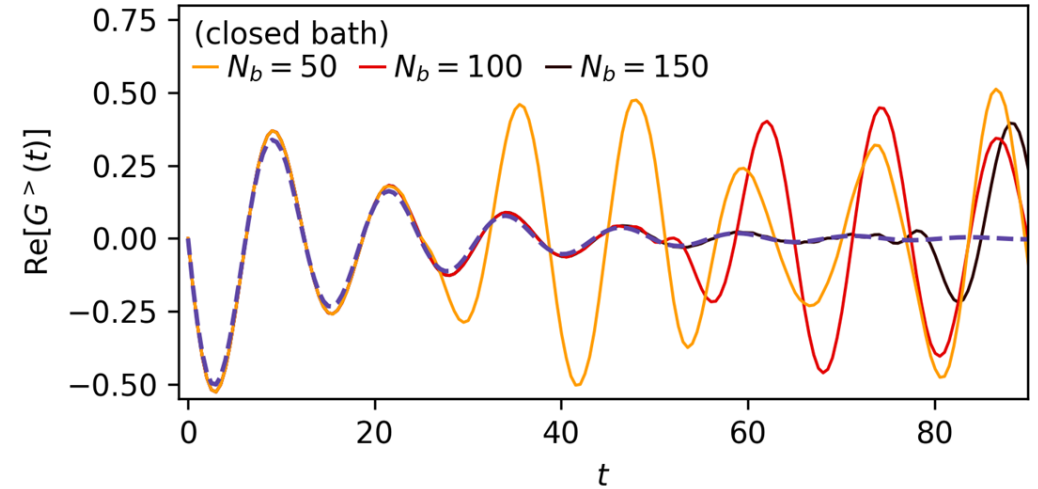


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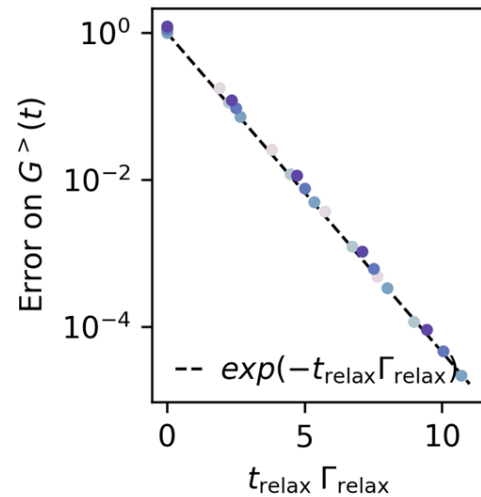
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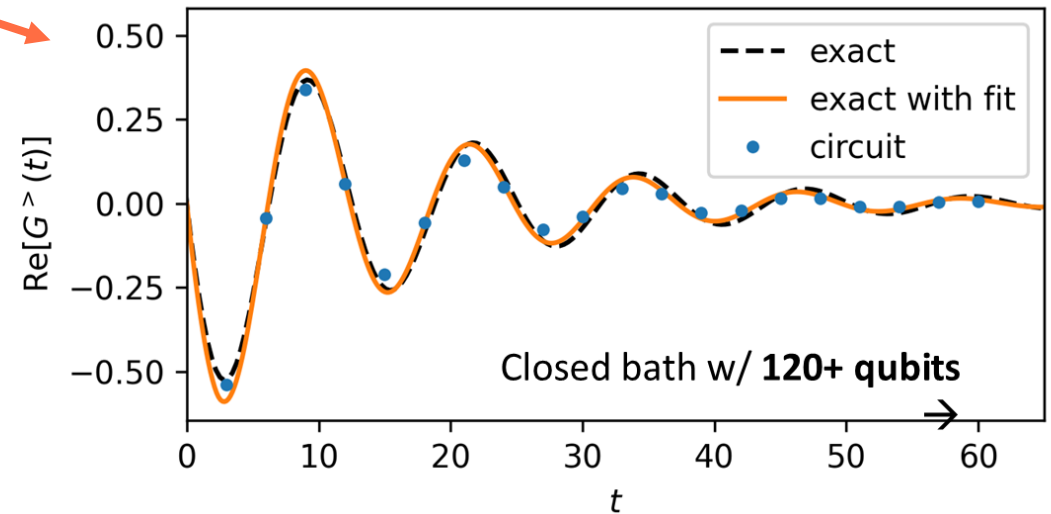
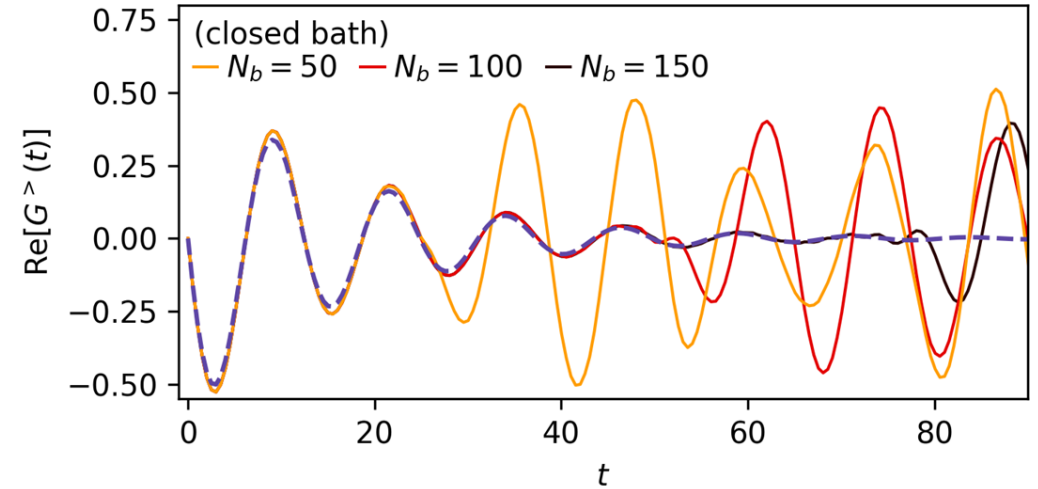
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- **Speeds up state preparation** (dissipation helps reach steady state)



Green's function computation:



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Conclusion



What prospects for today's processors?

Today, many-body platforms with **100-1000 particles/qubits**.

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VQE or beyond?



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Today's examples:

- Shorter circuit with natural orbitals
- Better convergence properties of PQE than VQE?
- Slave-spin to short-circuit fermionic overhead
- MPS to jump start QC
- Use noise to our advantage?

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Thanks

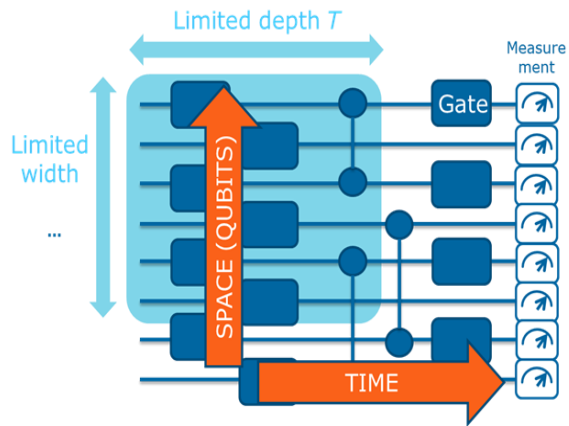
thomas.ayral@eviden.com

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Known issues with the variational quantum eigensolver

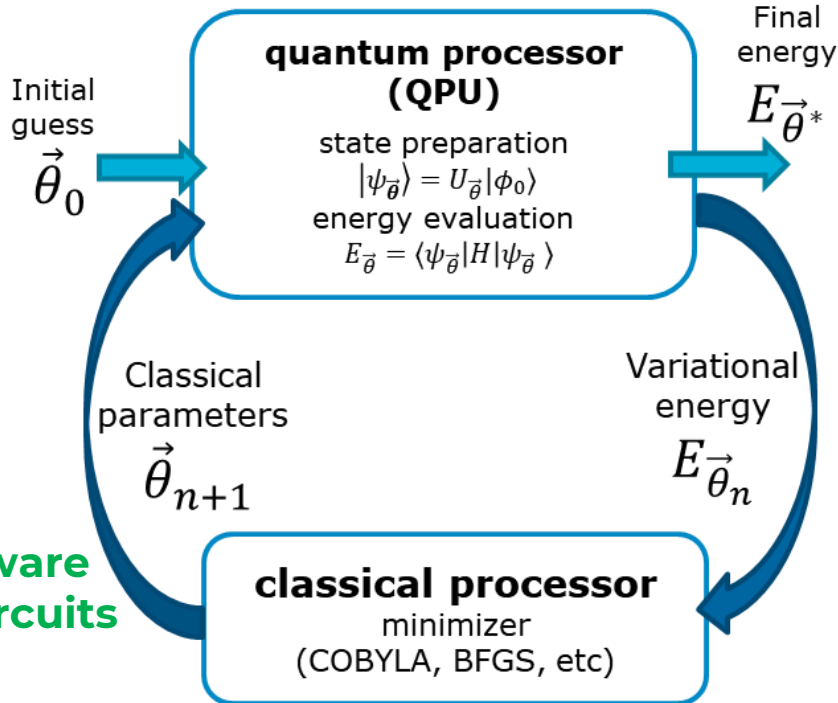
Interesting variational circuits **are still too long!**



Noisy hardware... **Better hardware or shorter circuits**

Fermion antisymmetry:
 $c_i^\dagger c_j$ leads to $X_i Z_{i+1} \dots Z_{j-1} X_j$
 Hence longer circuits!

Better encodings or shortcut antisymmetry?



Is it hopeless?

Use QC for dynamics!

Measurement of $\langle \psi_{\theta} | H | \psi_{\theta} \rangle$:
 statistical error $\Delta E \approx \frac{\|H\|_1}{\sqrt{N_{\text{samples}}}}$
 Typically, $\|H\|_1 = 10 \text{ Ha}$, $\Delta E = 1 \text{ mHa}$...
 => 10^8 samples / 10 kHz = 3 hours
 (x number of optimization steps!)

**Don't measure $\langle \psi_{\theta} | H | \psi_{\theta} \rangle$, just sample!
 Use VQE as input to LSQ algorithms**

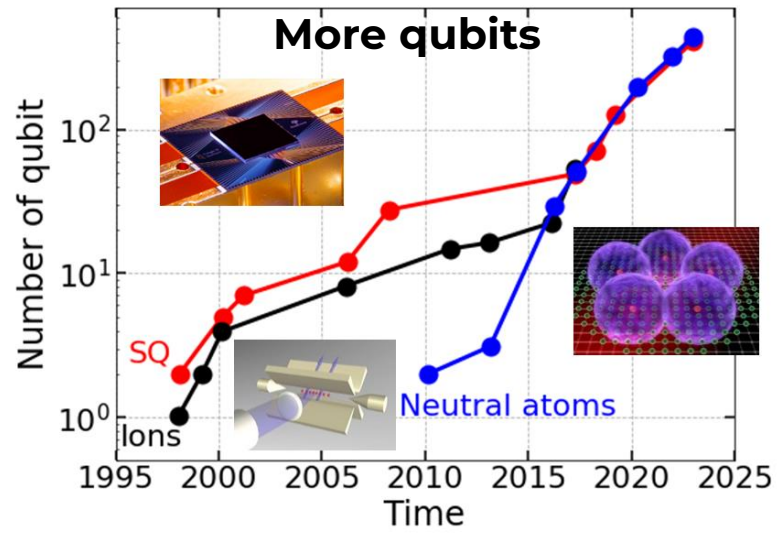
Barren plateau problem



**Adaptive ansatz construction
 Smarter initial starting point
 Don't minimize $E(\theta)$
 (find zero residues (cf coupled cluster), ...)**

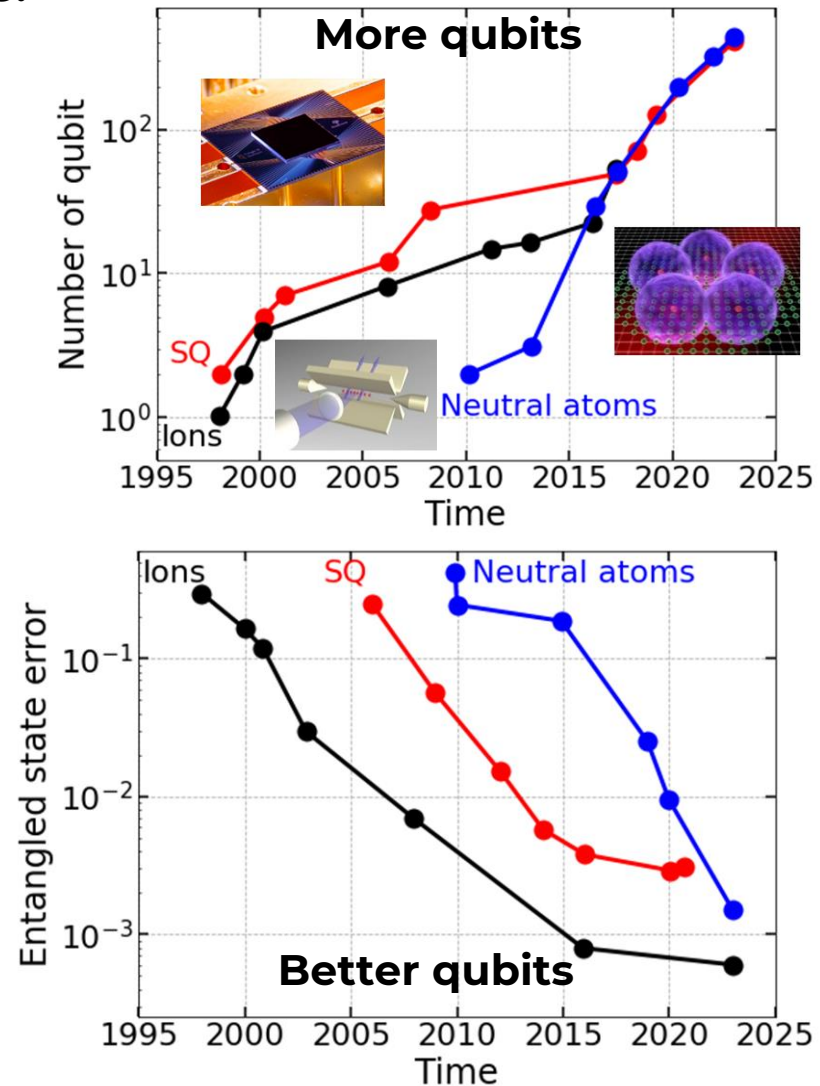
Should we directly turn to error-corrected QCs?

YES!



Should we directly turn to error-corrected QCs?

YES!

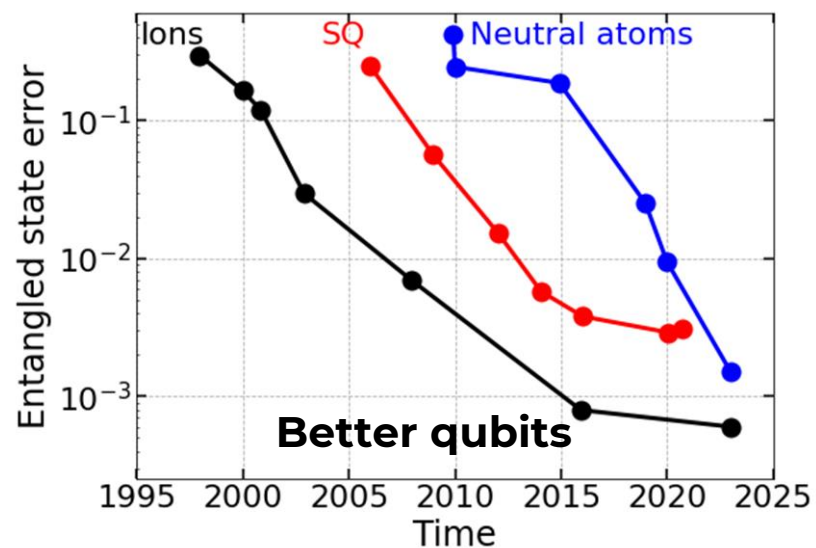
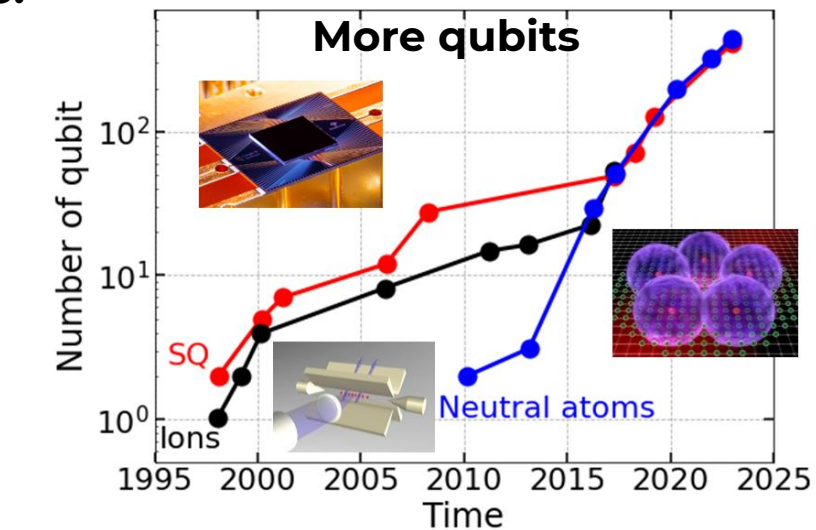


EVIDEN

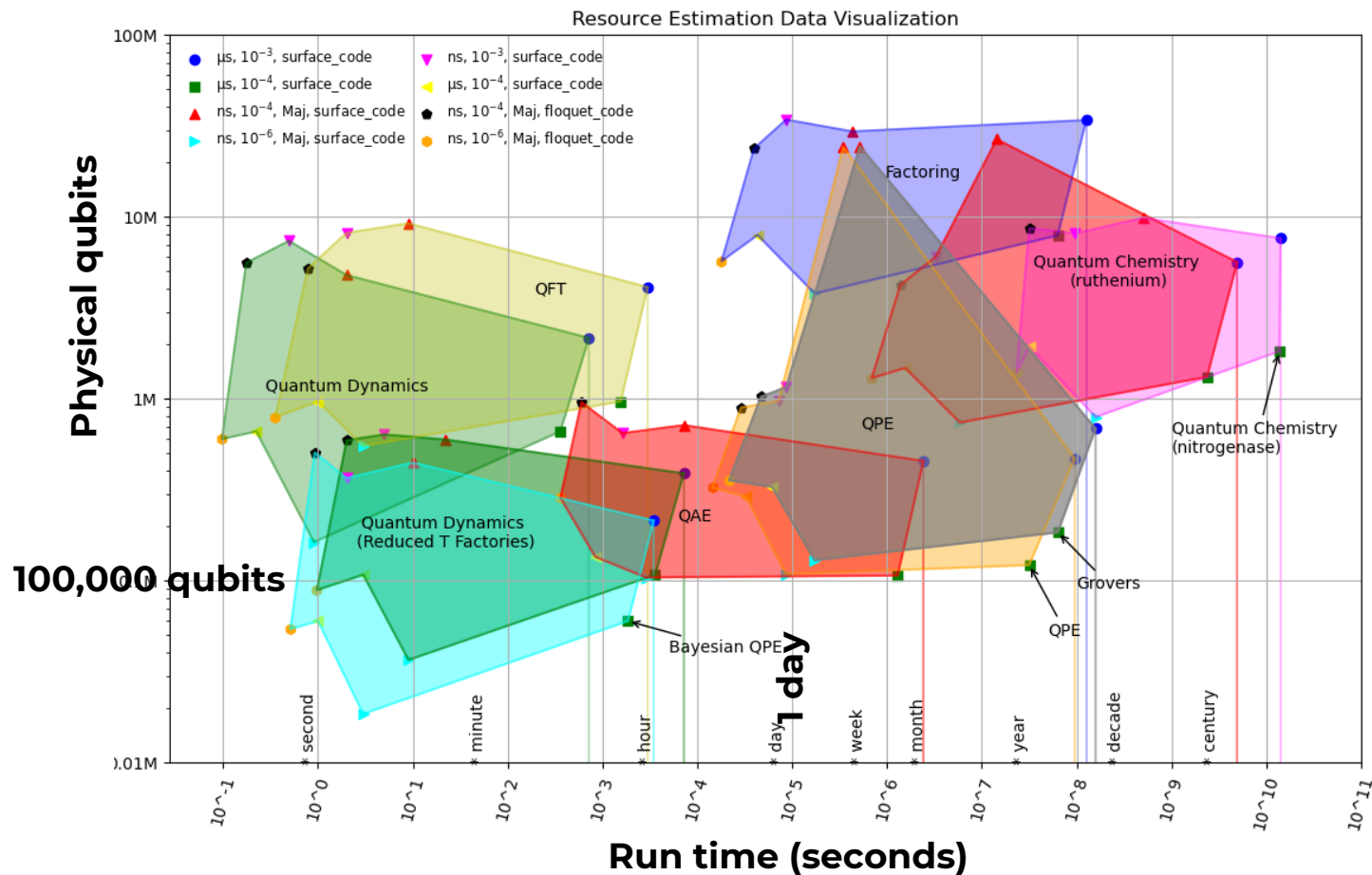
Courtesy of L.P Henry & L. Henriet @Pasqal

Should we directly turn to error-corrected QCs?

YES!

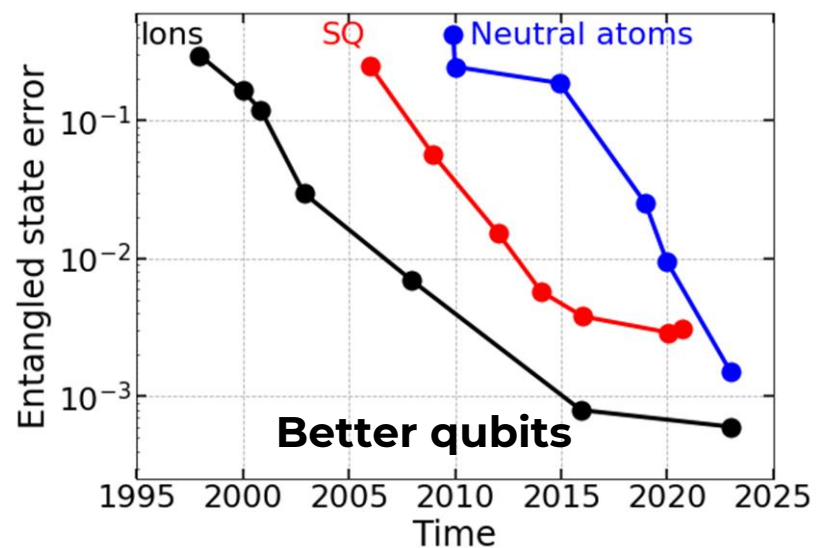
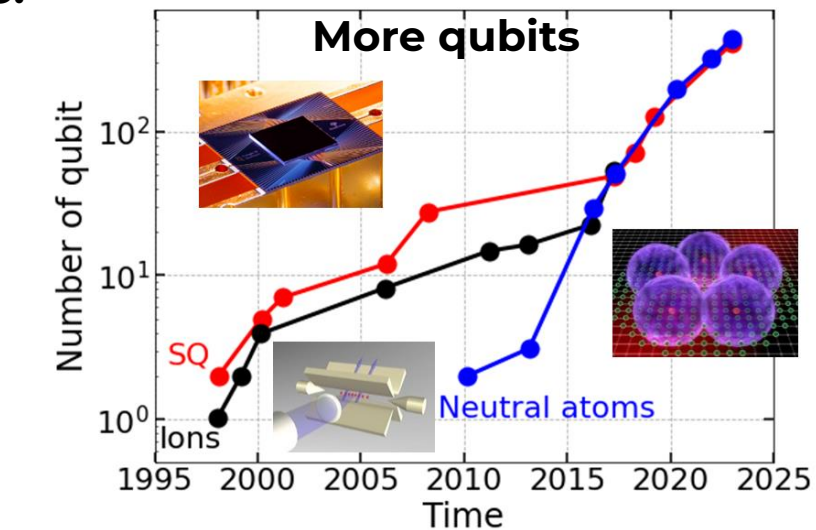


NO!

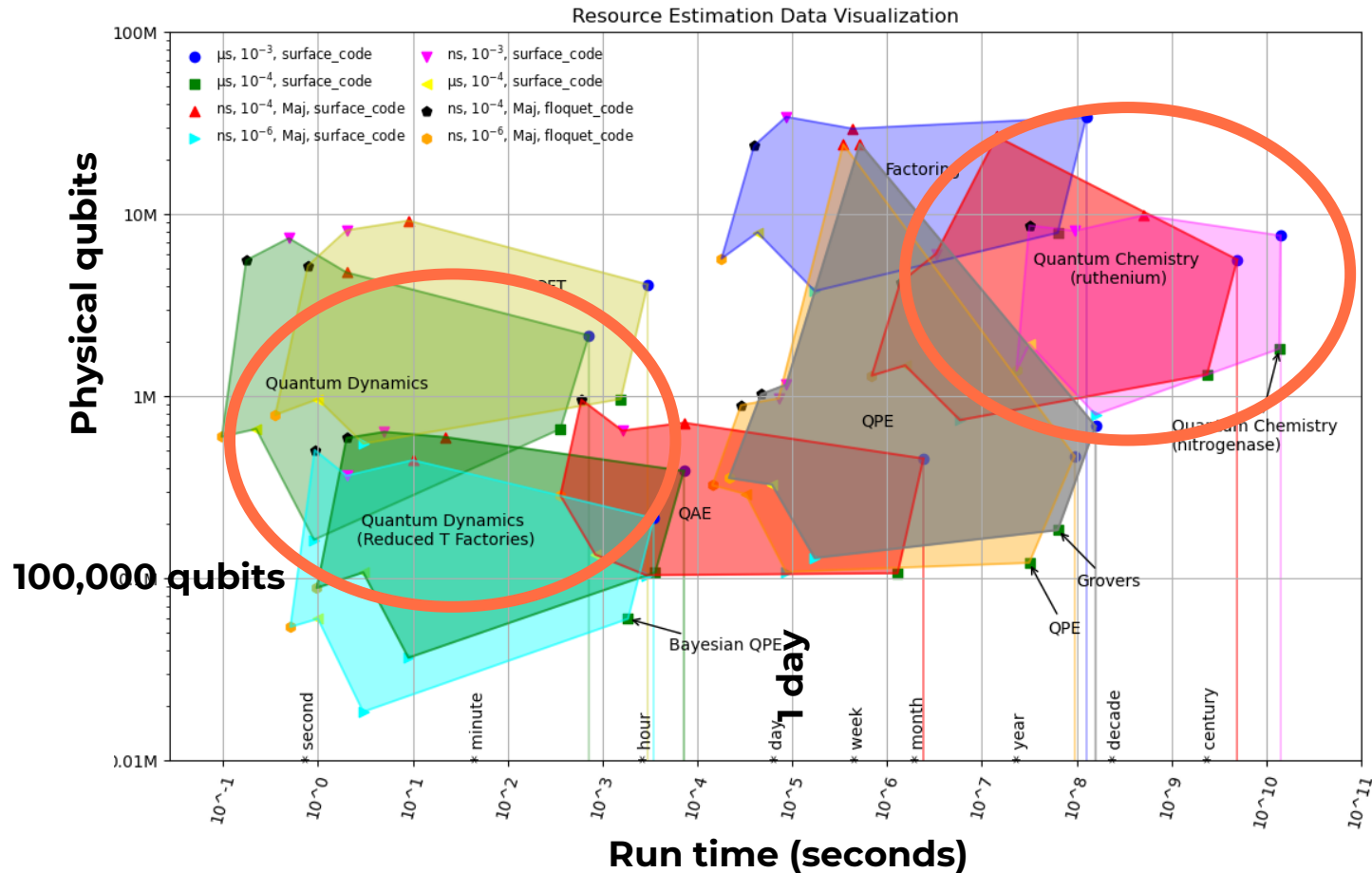


Should we directly turn to error-corrected QCs?

YES!



NO!



EVIDEN

Courtesy of L.P Henry & L. Henriet @Pasqal

GQI Quantum Resource Estimator Playbook
(Azure Quantum Resource Estimator)

Even if we had enough good qubits...

Orthogonality catastrophe in quantum phase estimation

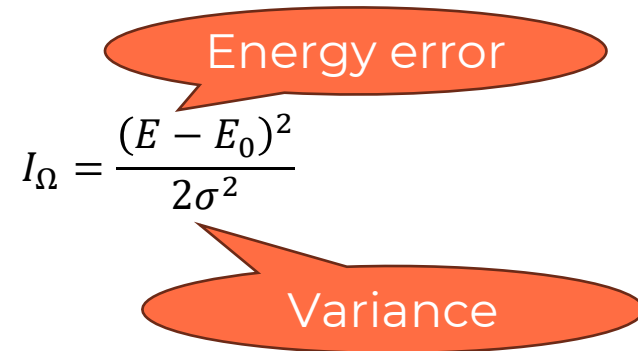
QPE run time: $\propto 1/\Omega$

with Ω : overlap of input state with solution

Estimate of Ω :

$$\Omega \approx e^{-I_\Omega}$$

with

$$I_\Omega = \frac{(E - E_0)^2}{2\sigma^2}$$


The diagram shows the equation $I_\Omega = \frac{(E - E_0)^2}{2\sigma^2}$ with two orange callout boxes. The top callout box, labeled "Energy error", points to the numerator $(E - E_0)^2$. The bottom callout box, labeled "Variance", points to the denominator $2\sigma^2$.

Even if we had enough good qubits...

Orthogonality catastrophe in quantum phase estimation

QPE run time: $\propto 1/\Omega$

with Ω : overlap of input state with solution

Estimate of Ω :

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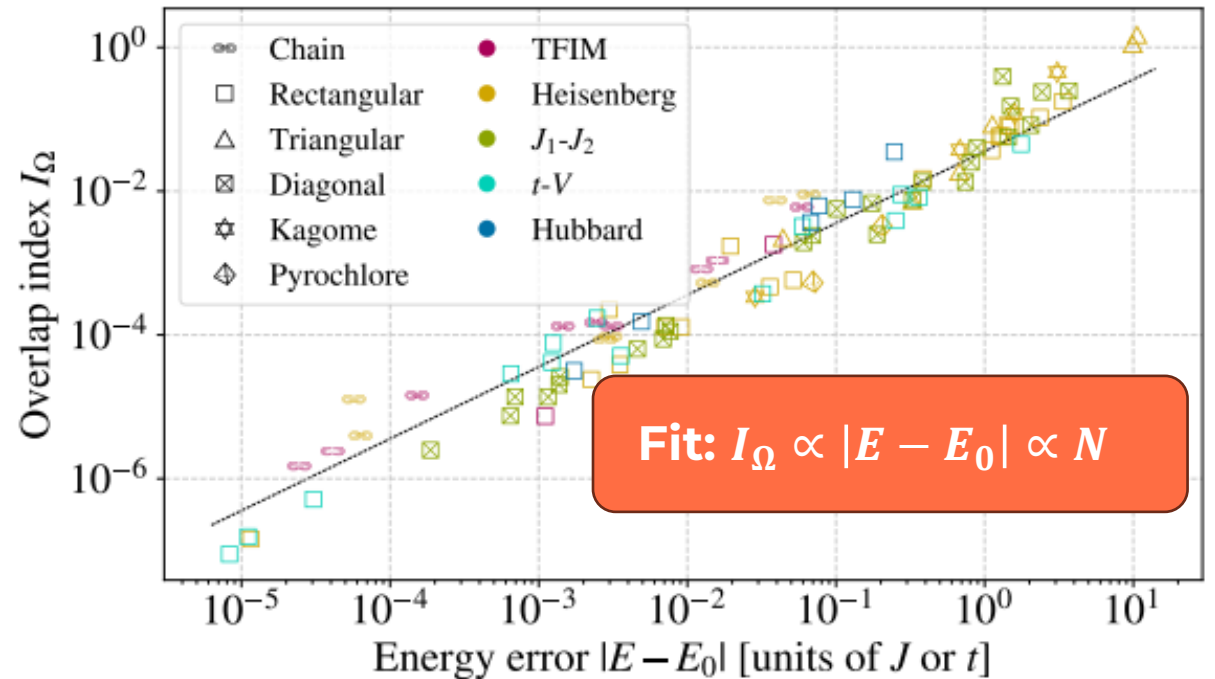
with

$$I_\Omega = \frac{(E - E_0)^2}{2\sigma^2}$$

Energy error

Variance

Test on state-of-the-art classical methods:



Therefore: $\Omega \approx e^{-\alpha N}$

- Better inputs?
- Better phase estimation algorithms?