

Quantum Machine Learning

TQCI Seminar

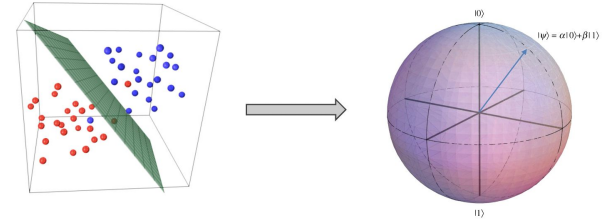
Jonas Landman

Postdoctoral Research Associate - University of Edinburgh / LIP6

Why Quantum Machine Learning?

Can quantum algorithms solve machine learning problems?

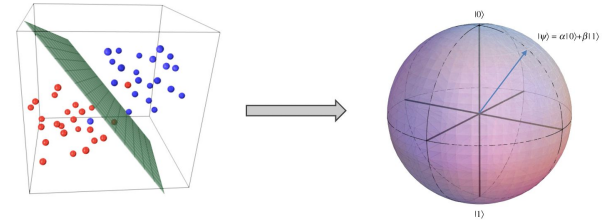
Provable/comparable **guarantees**?
Speedup or any other **advantage**?
Control over **quantum effects**?



Why Quantum Machine Learning?

Can quantum algorithms solve machine learning problems?

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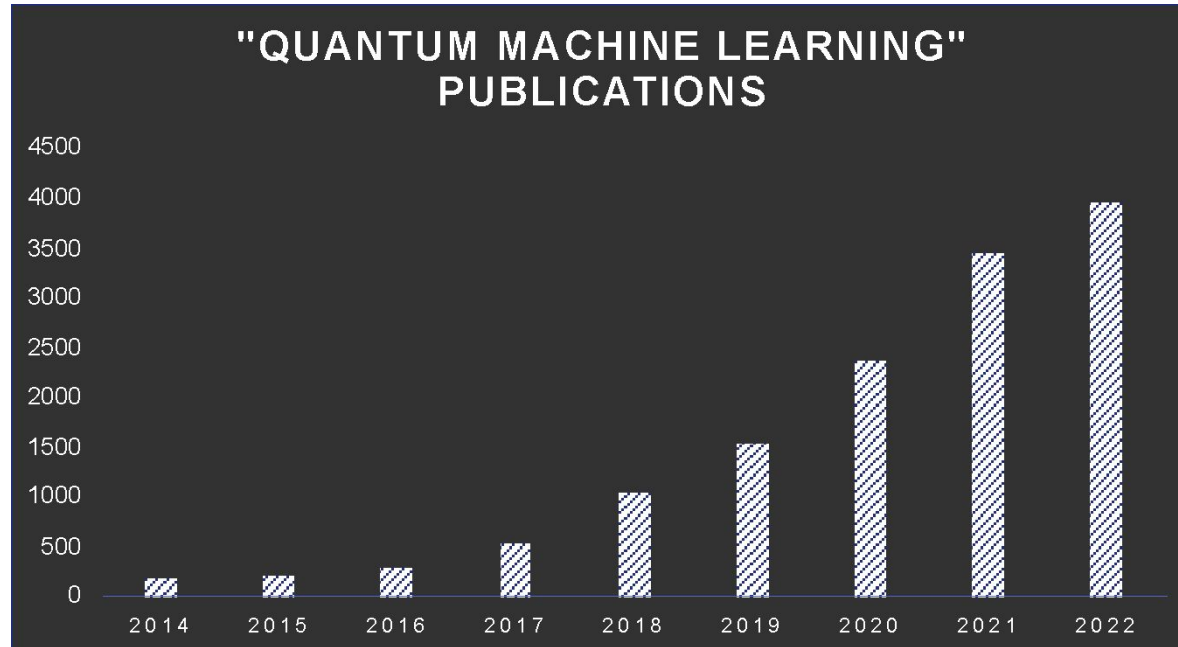


There is a strong link between ML and QC : **Linear Algebra**

There are different approaches to QML : **Long Term & Short Term**

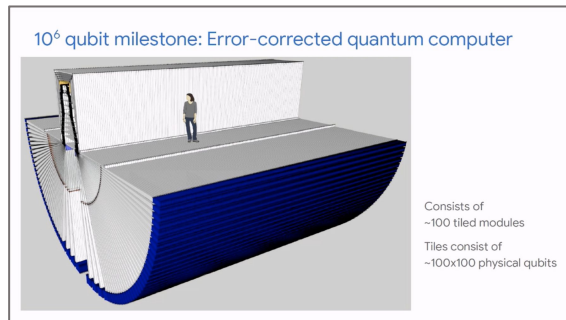
A lot of theory is still needed to understand **Advantages** and **Caveats**

Research publications



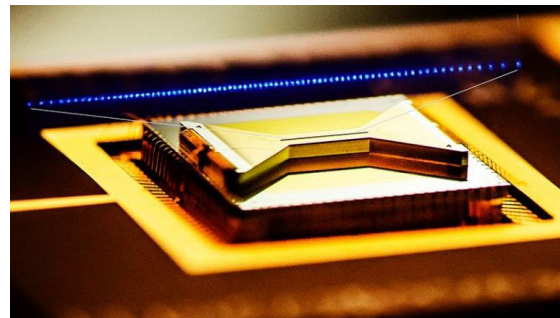
Long Term vs Near Term

Long Term



Google Quantum[®]

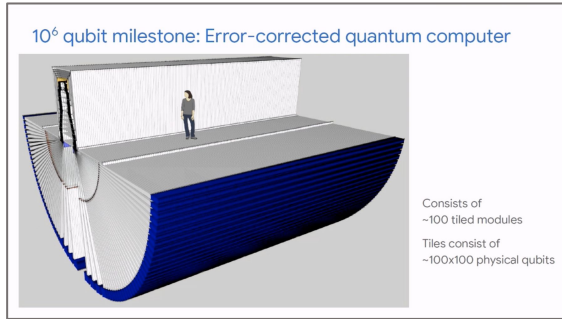
Near Term



IonQ[®]

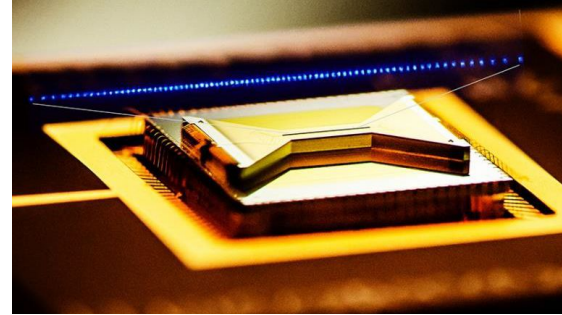
Long Term vs Near Term

Long Term



Google Quantum[®]

Near Term



IonQ[®]

In the long term, Quantum provide a theoretical advantage

- **Matrix Inversion** ($Ax = b$)
- **Linear Algebra** (SVD, projections, inner product)
- **Topology** (distance estimation) *etc.*

Quantum Machine Learning will be provably faster

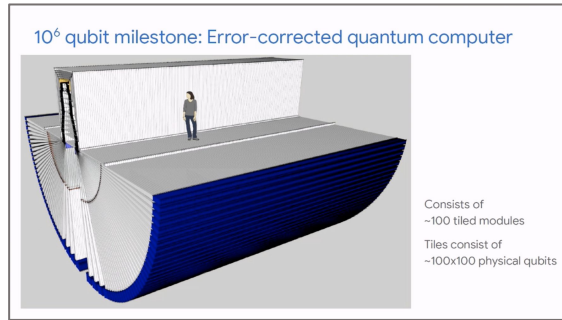
- **Clustering, Neural Networks**
- **Recommendation Systems, SVM, etc.**

Many Requirements

- **Loading Data (QRAM), Error Correction, De-quantization**

Long Term vs Near Term

Long Term



Google Quantum[®]

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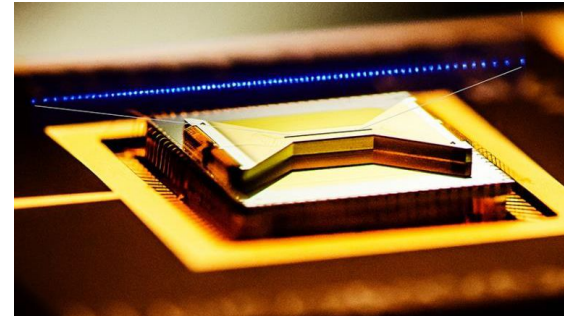
Quantum Machine Learning will be provably faster

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Many Requirements

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Near Term



IonQ[®]

In the near term, several approaches exist

Variational Quantum Circuits are used

- Require **classical optimization** of quantum gates
- Project data in **large feature space**
- **Not many proof** of advantage
- **Gradients** are vanishing
- **Expressivity** could be reproduced classically

Easy to implement

Unclear Scaling

Harder to interpret

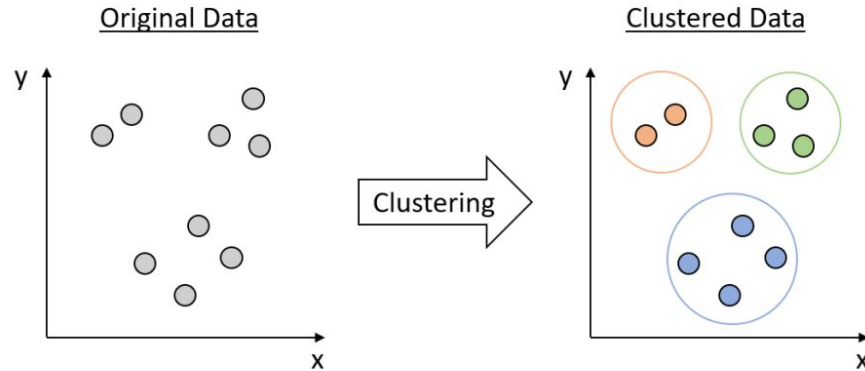
Long Term QML

Long Term QML : A Recipe



Long Term QML : A Recipe

- Choose your favorite classical ML algorithm



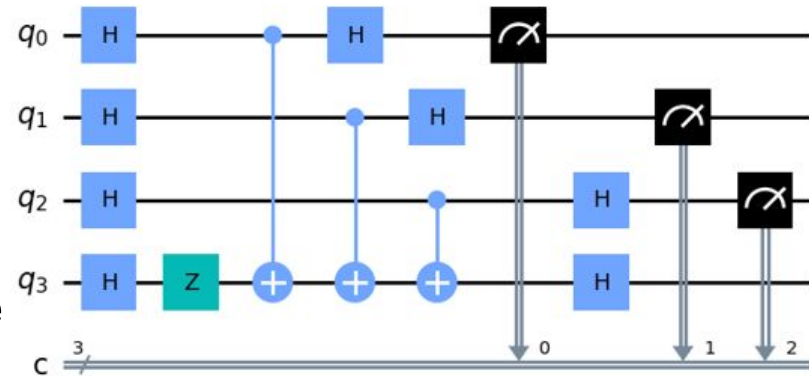
Long Term QML : A Recipe

- Choose your favorite classical ML algorithm
- Understand it at the linear algebra level

```
Input: The data set  $Y = \{y_s\}_{s=1}^S \subset \mathbb{R}^M$   
Input: Number of clusters :  $K$   
Output: Clusters:  $\{Y_k^{(i)}\}_{k=1}^K$   
Output: Cluster labels array:  $L[1 : K]$   
// Initialization  
 $i \leftarrow 0$ ; // Iteration counter  
foreach  $k \in \{1, \dots, K\}$  do  
| // for  $k$ -th cluster  
| Initialize  $\mu_k^{(0)}$  and  $\Sigma_k^{(0)}$  suitably ; Set  $Y_k^{(0)}$  to empty set ;  
end  
repeat  
| // Segmentation:  
| foreach  $y_s \in Y$  do  
| |  $L(k) \leftarrow l \leftarrow \arg \min_{k=1, \dots, K} \|y_s - \mu_k^{(i)}\|_{\Sigma_k^{(i)}}^2$ ; assign  $y_s$  to  
| |  $Y_l^{(i+1)}$  ;  
| end  
| // Estimation:  
| foreach  $k \in \{1, \dots, K\}$  do  
| |  $\mu_k^{(i+1)} \leftarrow \text{mean}(Y_k^{(i+1)})$ ;  
| |  $\Sigma_k^{(i+1)} \leftarrow \text{cov}(Y_k^{(i+1)})$ ;  
| end  
 $i \leftarrow i + 1$  ;  
until the segmentation has stopped changing;
```

Long Term QML : A Recipe

- Choose your favorite classical ML algorithm
- Understand it at the linear algebra level
- Imagine a quantum circuit that
 - Loads the **data**
 - Perform the **same operations**
 - **Retrieve** the results from the Q state



*Assuming many qubits
+ large depth circuits
+ error correction !*

Long Term QML : A Recipe

- Choose your favorite classical ML algorithm
- Understand it at the linear algebra level
- Imagine a quantum circuit that
 - Loads the **data**
 - Perform the **same operations**
 - **Retrieve** the results from the Q state
- Compare “speed” of C vs. Q
 - If good : Claim “**Q Advantage**” but be honest about all the issues

arXiv > quant-ph > arXiv:1812.03584

Quantum Physics

[Submitted on 10 Dec 2018 (v1), last revised 11 Dec 2018 (this version, v2)]

q-means: A quantum algorithm for unsupervised machine learning

lordanis Kerenidis, Jonas Landman, Alessandro Luongo, Anupam Prakash

Quantum machine learning is one of the most promising applications of a full-scale quantum computer. Over the past few algorithms have been proposed that can potentially offer considerable speedups over the corresponding classical algorithm. The q-means algorithm is a new quantum algorithm for clustering which is a canonical problem in unsupervised machine learning. The q-means algorithm guarantees similar to k-means, and it outputs with high probability a good approximation of the k cluster centroids like k d -dimensional vectors v_i (seen as a matrix $V \in \mathbb{R}^{N \times d}$) stored in QRAM, the running time of q-means is $\tilde{O}\left(kd \frac{\kappa(V)}{\delta} \kappa(\mu)\right)$ where $\kappa(V)$ is the condition number, $\mu(V)$ is a parameter that appears in quantum linear algebra procedures and $\eta = \max_i \|v_i\|_2$. For clusterable datasets, the running time becomes $\tilde{O}\left(k^2 d \frac{\eta^2}{\delta^2} + k^{2.5} \frac{\eta}{\delta}\right)$ per iteration, which is linear in the number of features d , the maximum square norm η and the error parameter δ . Both running times are only polylogarithmic in the number of datapoints N compared to the classical k-means algorithm that runs in time $O(kdN)$ per iteration, particularly for the case of low dimensionality data.

Subjects: Quantum Physics (quant-ph); Machine Learning (cs.LG)

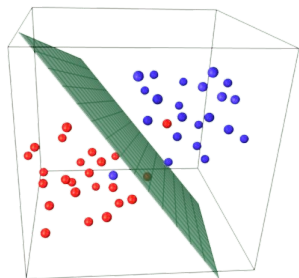
Cite as: arXiv:1812.03584 [quant-ph]
(or arXiv:1812.03584v2 [quant-ph] for this version)
<https://doi.org/10.48550/arXiv.1812.03584>

Journal reference: Advances in Neural Information Processing Systems 32 (NeurIPS 2019)

Long Term QML

Where does the advantage come from?

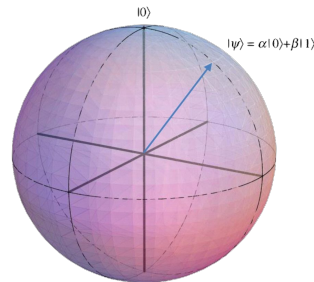
1) Load data via Amplitude Encoding



$$x \in \mathbb{R}^d$$



QRAM



$$|x\rangle = \frac{1}{\|x\|} \sum_{j=0}^{d-1} x_j |j\rangle$$

computational basis $|x\rangle = x_1|0 \dots 01\rangle + x_2|0 \dots 11\rangle + \dots + x_d|11 \dots 1\rangle$

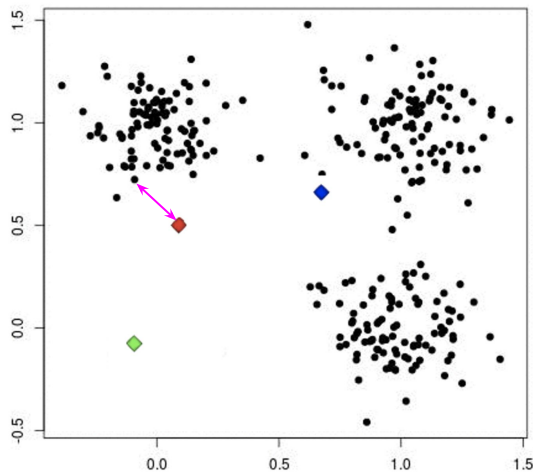
Exponentially small !

$\log(d)$ qubits

Long Term QML

Where does the advantage come from?

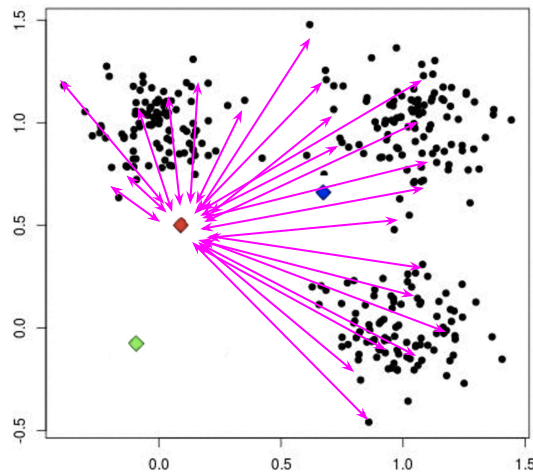
2) Compute in parallel



$d_1, d_2, d_3,$
 d_4, \dots, d_N

Classical values

C: Repeat N times



$|d_1\rangle + |d_2\rangle + |d_3\rangle +$
 $|d_4\rangle + \dots + |d_N\rangle$

Quantum state

Q: All in 1 time

Long Term QML : Main Issues

- 1) Loading the data in the quantum state is harder than you think
- 2) Extract the result from a quantum state is harder than you think
- 3) Quantum processes are random by nature, are you ok with it ?



The image shows a screenshot of a webpage article. At the top, there is a blue horizontal bar with the word "commentary" in white text. Below this, the title "Read the fine print" is displayed in a large, bold, black font. Underneath the title, the author's name "Scott Aaronson" is written in a smaller blue font. The main text of the article begins with "New quantum algorithms promise an exponential speed-up for machine learning, clustering and finding patterns in big data. But to achieve a real speed-up, we need to delve into the details." The article is divided into three columns of text. The first column starts with a large blue letter 'F' and discusses the challenges of quantum computing. The second column starts with "HHL attacks one of the most basic problems in all of science: solving a system of linear equations..." and discusses the HHL algorithm. The third column starts with "of interest, and then carefully analyses the resulting performance against that of the best-known classical algorithm for that case." and continues to discuss the implications of the HHL algorithm.

commentary

Read the fine print

Scott Aaronson

New quantum algorithms promise an exponential speed-up for machine learning, clustering and finding patterns in big data. But to achieve a real speed-up, we need to delve into the details.

For twenty years, quantum computing has been catnip to science journalists. Not only would a quantum computer harness the notorious weirdness of quantum mechanics, but it would do so for a practical purpose: solving certain problems exponentially faster than we know how to solve them with any existing computer. But,

HHL attacks one of the most basic problems in all of science: solving a system of linear equations. Given an $n \times n$ real matrix, A , and a vector, \mathbf{b} , the goal of HHL is to (approximately) solve the system $A\mathbf{x} = \mathbf{b}$ for \mathbf{x} , and to do so in an amount of time that scales only logarithmically with n , the number of equations and unknowns. Classically, this

of interest, and then carefully analyses the resulting performance against that of the best-known classical algorithm for that case. To my knowledge, so far there have been two attempts to work out potential applications of the HHL template from start to finish. Clader, Jacobs, and Sprouse⁵ argued that HHL could be used to speed up

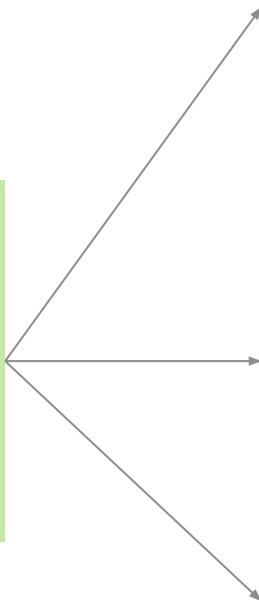
Long Term QML

Matrix Multiplication / Inversion
Eigenvalues estimation
Amplitude Amplification
Distance Estimation
...

ML:
Unsupervised Learning
Neural Networks
Graph Computations
...

Chemistry
...

Optimization
...



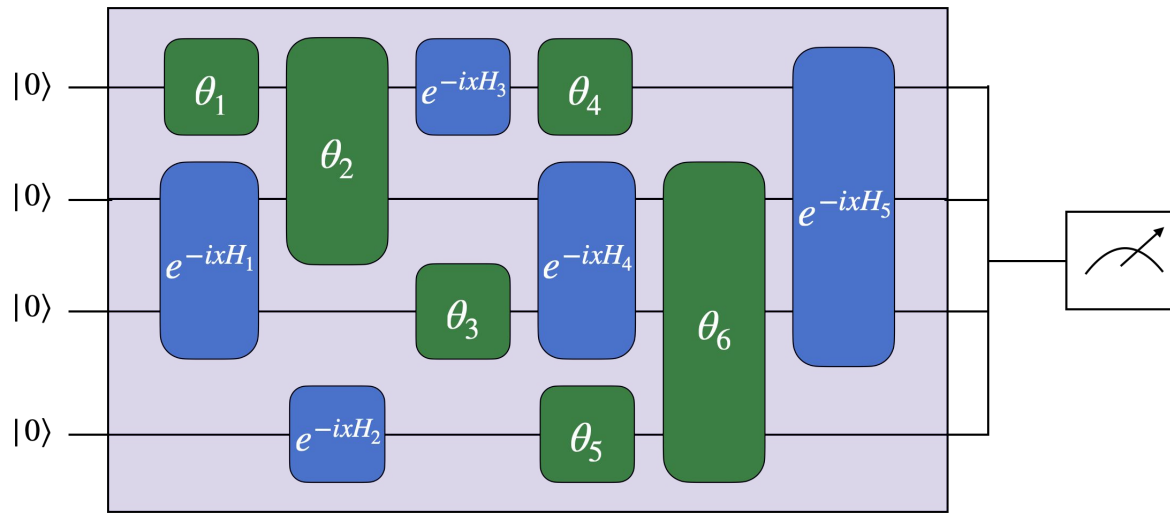
Near Term QML

Near Term QML : A Recipe



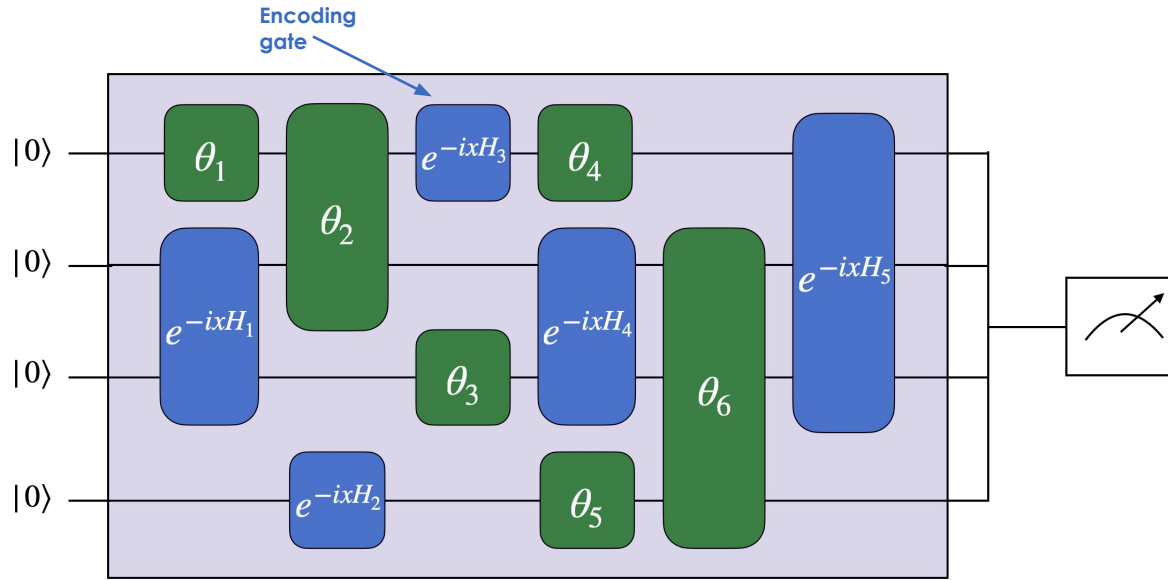
Near Term QML : A Recipe

- Take a *variational* quantum circuit that looks like this



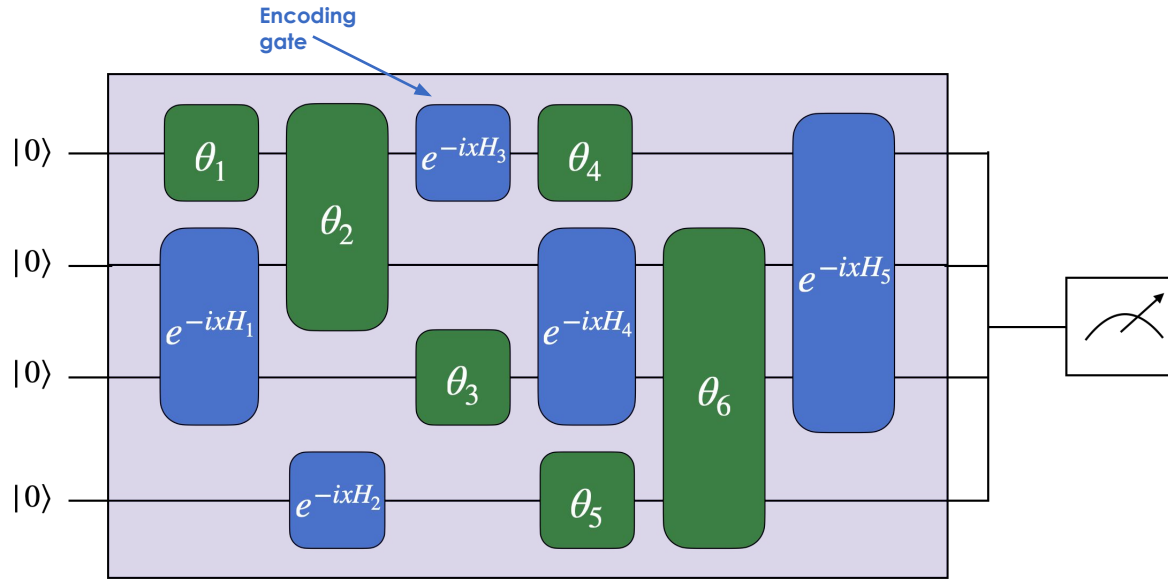
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- Take a *variational* quantum circuit that looks like this
- Input your data (x) as parameters of some gates



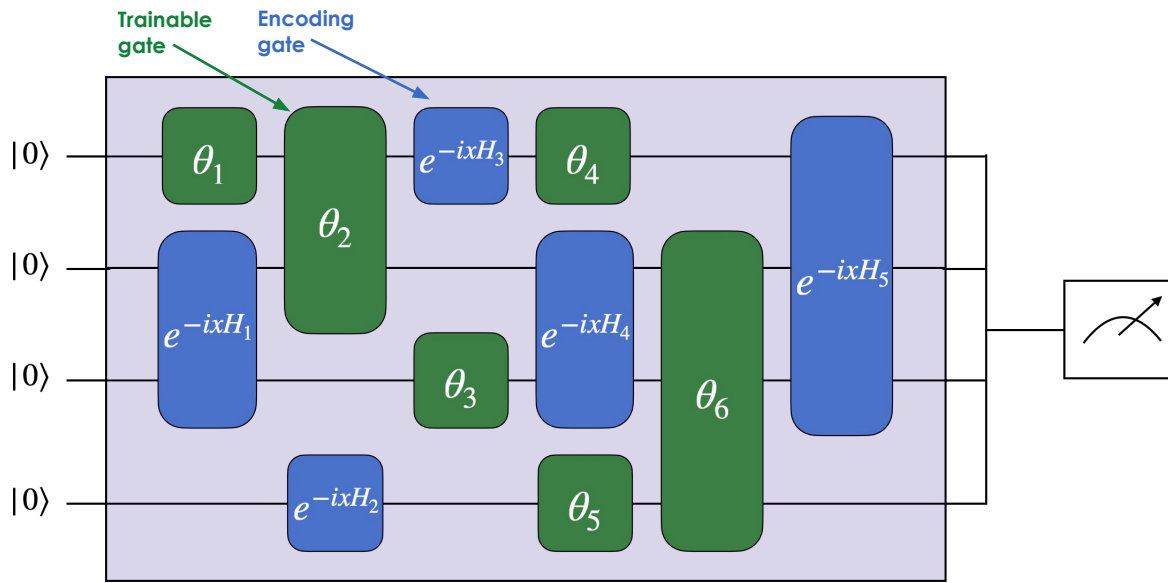
Near Term QML : A Recipe

- Take a *variational* quantum circuit that looks like this
- Input your data (x) as parameters of some gates
- Hope that what you measure at the end is the right answer

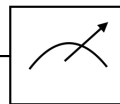
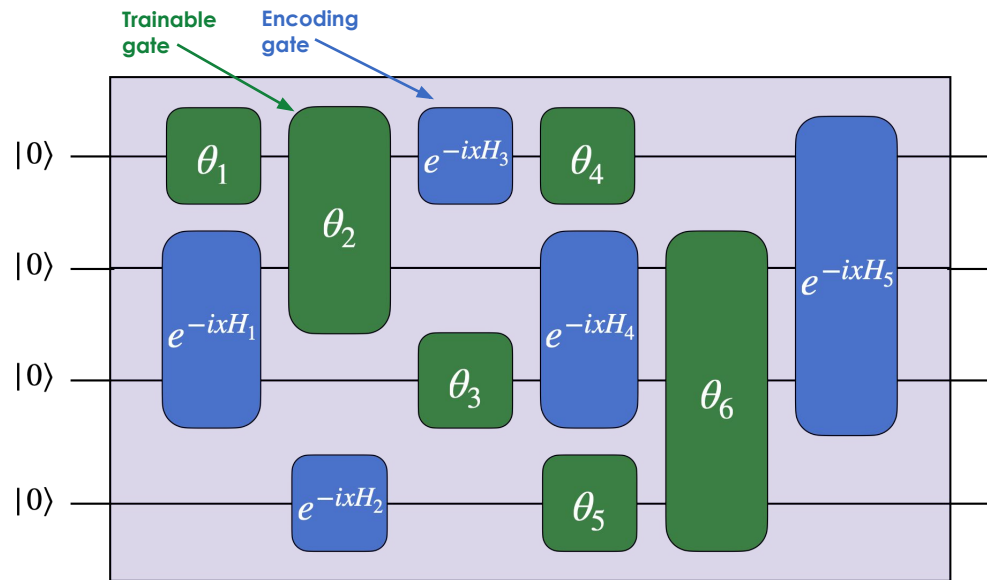


Near Term QML : A Recipe

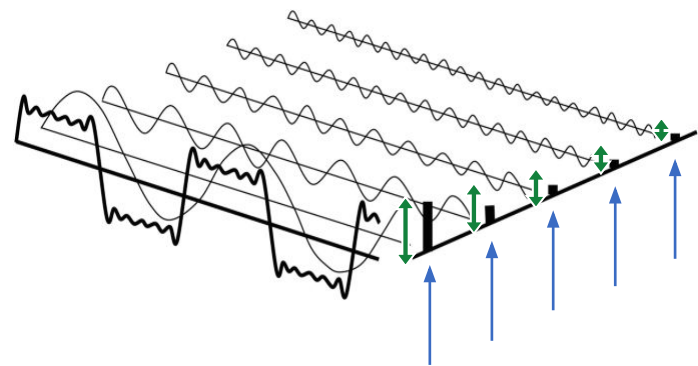
- Take a *variational* quantum circuit that looks like this
- Input your data (x) as parameters of some gates
- Hope that what you measure at the end is the right answer
- Tune the trainable gates (θ) until your hope becomes true



Near Term QML : What is going on?



$$f(x; \theta) = \sum_{\omega \in \Omega} c_{\omega}(\theta) e^{i\omega x}$$



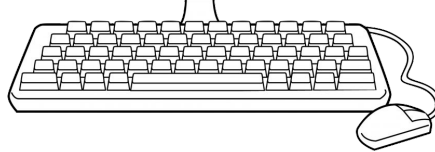
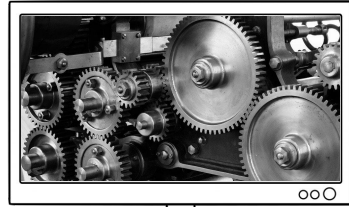
It learns (exponentially large) Fourier Series

Near Term QML : What is going on?

Learning in Exponentially Large Spaces



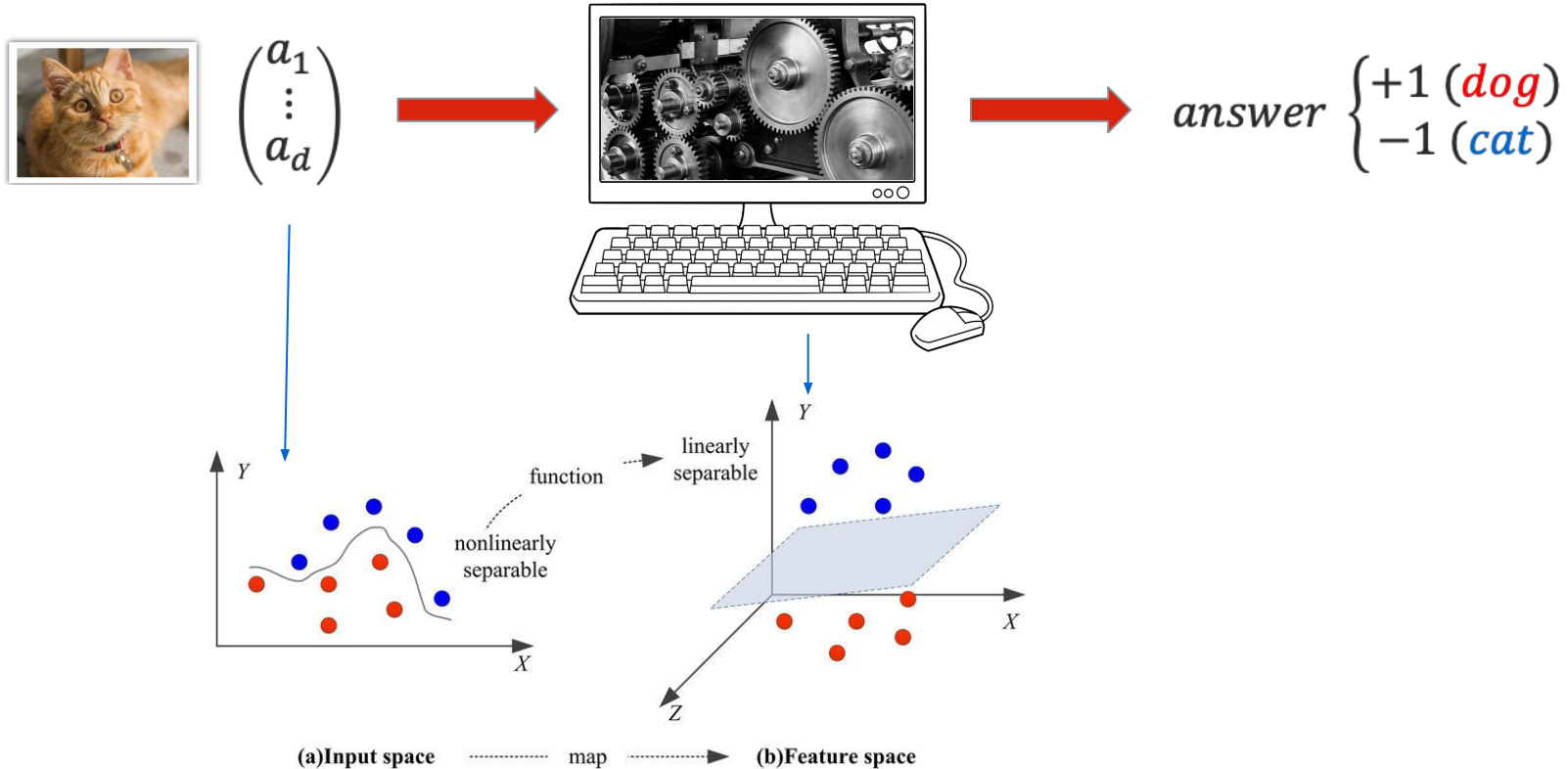
$$\begin{pmatrix} a_1 \\ \vdots \\ a_d \end{pmatrix}$$



$$answer \begin{cases} +1 (dog) \\ -1 (cat) \end{cases}$$

Near Term QML : What is going on?

Learning in Exponentially Large Spaces



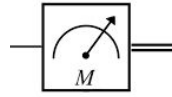
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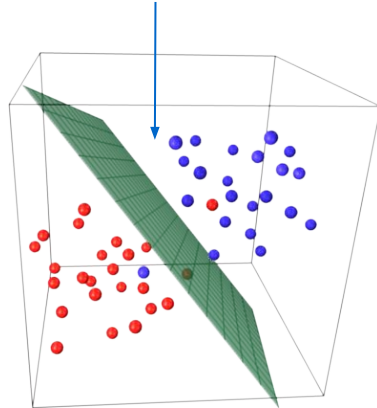
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loader →



→

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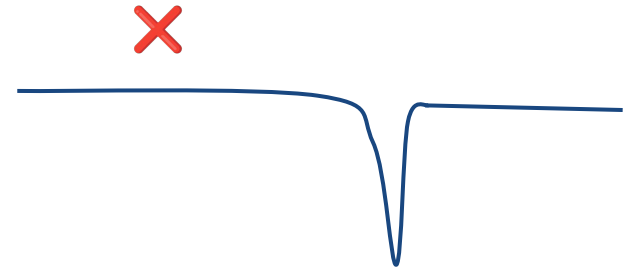
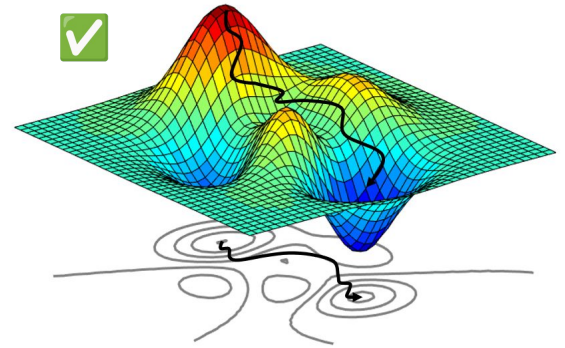
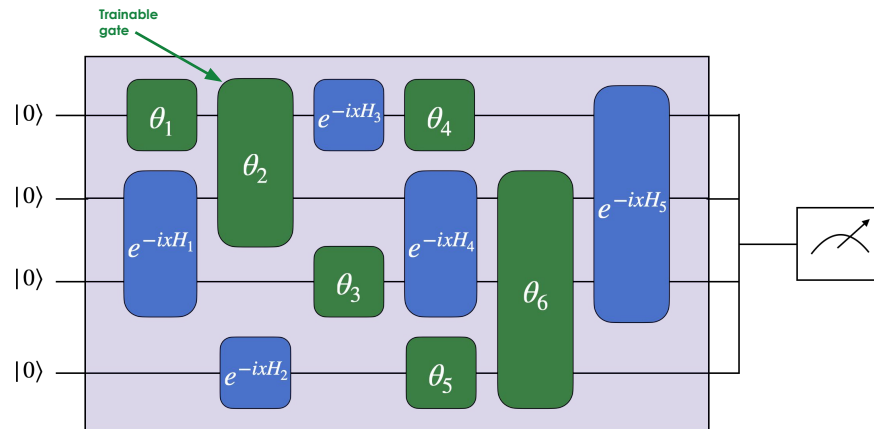
#Dimensions : Exponential

Near Term QML : Main Issues

- Barren Plateaus: impossibility to train

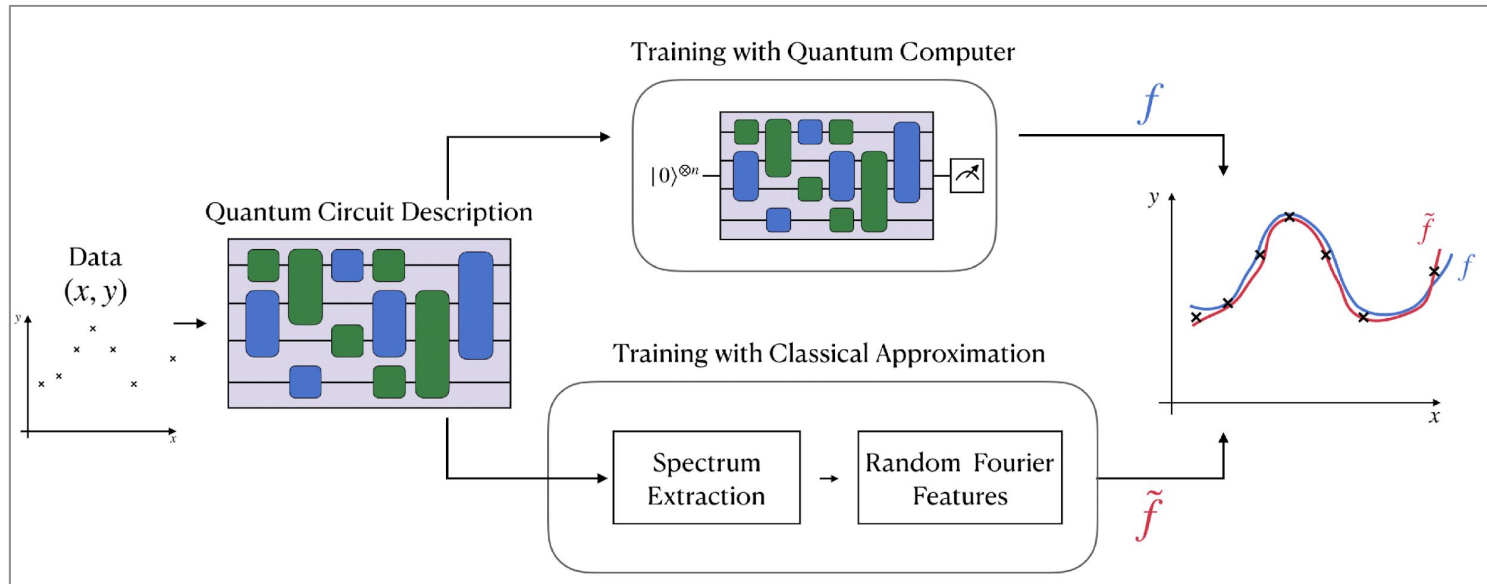
$$\theta_{t+1} = \theta_t - \eta \nabla \mathcal{L}(\theta)$$

Exponentially small value!



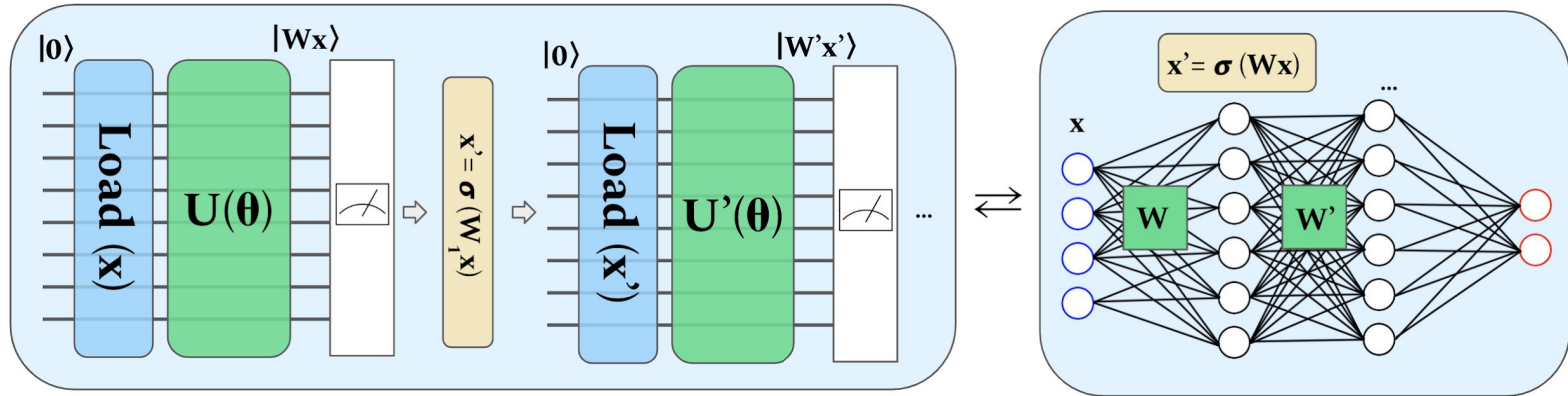
Near Term QML : Main Issues

- Barren Plateaus: impossibility to train
- Classical Approximations



Alternative: Subspace Preserving QML

- Variational, low depth q circuits
- Reproduce Neural Networks rigorously
- Does not explore exponentially large spaces



Trade off between:

- Loaders Feasibility
- Classical Approximations
- Barren Plateau

Qonqlusion

- QML is not so simple to implement
- Near / Long term are very different approaches
- Devil is in the details
- We might be surprise when Q Computers will be big enough
- Meanwhile: keep doing research !

Quantum Machine Learning

TQCI Seminar

Jonas Landman

Postdoctoral Research Associate - University of Edinburgh / LIP6